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Control of Natural Gas Catalytic Partial Oxidation for Hydrogen Generation in Fuel Cell Applications

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Abstract

A fuel processor that reforms natural gas to hydrogen-rich mixture to feed the anode field of fuel cell stack is considered. The first reactor that generates the majority of the hydrogen in the fuel processor is based on catalytic partial oxidation of the methane in the natural gas. We present a model-based control analysis and design for a fuel processing system that manages natural gas flow and humidified atmospheric air flow in order to regulate (i) the amount of hydrogen in the fuel cell anode and (ii) the temperature of the catalytic partial oxidation reactor during transient power demands from the fuel cell.

Linear feedback analysis and design is used to identify the limitation of a decentralized controller and the benefit of a multivariable controller. Further analysis unveils the critical controller cross-coupling term that contributes to the superior performance of the multivariable controller.

Keywords

Fuel Cell, Fuel Processor, Hydrogen Generation, Multivariable Feedback, Linear Control, Dynamics.

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I. Introduction

Fuel Cells are considered for stationary (residential and commercial) and mobile (automotive and portable) power generation due to their high efficiency and environmental friendliness. Inadequate infrastructure for hydrogen refueling, distribution, and storage makes the fuel processor technology an important part of the fuel cell system for both stationary and mobile applications. For residential applications, fueling the fuel cell system using natural gas is often preferred because of its wide availability and extended distribution system [1]. Common methods of converting natural gas to hydrogen include steam reforming and partial oxidation. The most common method, steam reforming, which is endothermic, is well suited for steady-state operation and can deliver a relatively high concentration of hydrogen [2], but it suffers from a poor transient operation [3]. On the other hand, the partial oxidation offers several other advantages such as compactness, rapid-startup, and responsiveness to load changes [1], but delivers lower conversion efficiency.

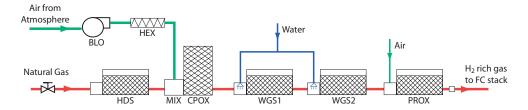


Fig. 1. FPS components

A schematic of a typical partial oxidation-based FPS is shown in Figure 1. The majority of hydrogen is generated in a catalytic partial oxidation reactor (CPOX) where natural gas (mostly methane CH₄) is combined with oxygen (in air) over a solid catalyst bed [4]. The two main factors that affect CH₄ to H₂ conversion efficiency of the CPOX are the catalyst bed temperature and the ratio of the reactants (CH₄ and O₂) [5]. At proper CPOX operating temperature, the amount of hydrogen created depends on the supply rate of CH₄ and the CPOX air to fuel ratio, more specifically, the oxygen to carbon ratio. This oxygen to carbon ratio also influences the amount of heat generated in the CPOX, which then affects the CPOX catalyst bed temperature. Carbon monoxide (CO), which poisons the fuel cell catalyst, is also created in the CPOX along with H₂ and thus additional processing is needed to remove the CO. The typical CO removal process involves two reactors: water

gas shift (WGS) and preferential oxidation (PROX) [6], which are represented, in this study, as if they perfectly remove the CO with the introduction of water and air. More details on the FPS chemical reactions are given in Section II.

During changes in the stack current, the fuel processor needs to (i) quickly regulate the amount of hydrogen in the fuel cell stack (anode) to avoid starvation or wasted hydrogen [7] and (ii) maintain a desired temperature of the CPOX catalyst bed for high conversion efficiency [8]. Accurate control and coordination of the fuel processor reactant flows can prevent both large deviation of hydrogen concentration in the anode and large excursion of CPOX catalyst bed temperature. A control-oriented nonlinear model of the natural gas fuel processing system is developed in Section III with a focus on the dynamic behaviors associated with the flows and pressure in the FPS and also the temperature of the CPOX. The two main performance variables are the anode hydrogen mole fraction [9] and the CPOX catalyst bed temperature [5]. The two control actuators are the fuel (CH₄) valve command and the CPOX air blower command. The control problem is formulated in Section IV and a linearized model derived in Section V is used in the control analysis and design.

Typical fuel processing systems rely on a decentralized (single-input single-output) control of the air blower command to control CPOX temperature and of the fuel valve command to control the anode hydrogen concentration. In Section VI, an analysis using the relative gain array method confirms the appropriateness of the traditional input-output pairs for the decentralized control. The study also shows large interactions between the two loops at high frequencies and different operating conditions. These interactions can be more efficiently handled with multivariable control which is studied in Section VIII. The linear quadratic optimal control method is used to design the controller (LQR) and the state estimator (LQG) that achieves a significant improvement in the CPOX temperature regulation as compared to the decentralized controller. It is shown in Section IX that the regulation of the anode H_2 mole fraction depends strongly on the speed of the fuel valve command while the improvement in the CPOX temperature regulation is due to the coordination of both inputs.

II. Fuel Processing System (FPS)

Figure 1 illustrates the components in a natural gas fuel processing system (FPS) [10]. Natural gas (mostly methane CH₄) is supplied to the FPS from either a high-pressure tank or a high-pressure pipeline. The main air flow is supplied to the system by a blower (BLO) which draws air from the atmosphere. The air is then heated in the heat exchanger (HEX). The hydro-desulfurizer (HDS) is used to remove sulfur present in the natural gas stream [1], [11]. The de-sulfurized natural gas stream is then mixed with the heated air flow in the mixer (MIX). The mixture is then passed through the catalyst bed inside the catalytic partial oxidizer (CPOX) where CH₄ reacts with oxygen to produce H₂. There are two main chemical reactions taking place in the CPOX: partial oxidation (POX) and total oxidation (TOX) [5], [12]:

$$(POX)$$
 $CH_4 + \frac{1}{2}O_2 \to CO + 2H_2$ (1)

$$(TOX)$$
 $CH_4 + 2O_2 \to CO_2 + 2H_2O$ (2)

Heat is released from both reactions. However, TOX reaction releases more heat than POX reaction. The difference in the rates of the two reactions depends on the selectivity, S, defined as

$$S = \frac{\text{rate of CH}_4 \text{ reacting in POX}}{\text{total rate of CH}_4 \text{ reacting}}$$
(3)

The selectivity depends strongly on the oxygen to carbon ratio (O_2 to CH_4), denoted by λ_{O2C} , entering the CPOX [5]. Hydrogen is created only in POX reaction and, therefore, it is preferable to promote this reaction in the CPOX. However, the heat generated from POX reaction is not sufficient to maintain CPOX temperature. Thus, promoting TOX reaction is also required. Carbon monoxide (CO) is also created along with H_2 in the POX reaction as can be seen in (1). Since CO poisons the fuel cell catalyst, it is eliminated using both the water gas shift converter (WGS) and the preferential oxidizer (PROX). As illustrated in Figure 1, there are typically two WGS reactors operating at different temperatures [3], [6]. In the WGS, water is injected into the gas flow in order to promote a water gas shift reaction:

$$(WGS) CO + H_2O \rightarrow CO_2 + H_2 (4)$$

Note that even though the objective of WGS is to eliminate CO, hydrogen is also created from the WGS reaction. The level of CO in the gas stream after WGS is normally still high for fuel cell operation and thus oxygen is injected (in the form of air) into the PROX reactor to react with the remaining CO:

$$(PROX) 2CO + O_2 \rightarrow 2CO_2 (5)$$

The amount of air injected into the PROX is typically twice the amount that is needed to maintain the stoichiometric reaction in (5) [3], [13].

III. CONTROL-ORIENTED FPS MODEL

The FPS model is developed with a focus on the dynamic behaviors associated with the flows and pressures in the FPS and also the temperature of the CPOX.

Several assumptions are made in order to simplify the FPS model. Since the control of WGS and PROX reactants are not studied, the two components are lumped together as one volume and the combined volume is called WROX (WGS+PROX). It is also assumed that both components are perfectly controlled to obtain desired conversion and operating temperatures. Furthermore, because the amount of H₂ created in WGS is proportional to the amount of CO that reacts in WGS (Reaction (4)), which in turn, is proportional to the amount of H₂ generated in CPOX (Reaction (1)), it is assumed that the amount of H₂ generated in the WGS is always a fixed percentage of the amount of H₂ produced in the CPOX. The de-sulfurization process in the HDS is not modeled and thus the HDS is viewed as a storage volume. It is assumed that the pressures and compositions of the air entering the blower and of the natural gas entering the HDS are constant. Natural gas is considered as pure methane CH₄. Additionally, any temperature other than the CPOX temperature is assumed constant and the effect of temperature changes on the pressure dynamics is assumed negligible. The volume of CPOX is relatively small and its dynamics are captured in the mixer. It is also assumed that all reactions are fast and reach equilibrium before the flow exit the reactors. Finally, all gases obey the ideal gas law and all gas mixtures are perfect mixtures. Figure 2 illustrates the simplified system and state variables used in the model.

The dynamic states in the model, shown also in Figure 2, are blower speed, ω_{blo} , heat

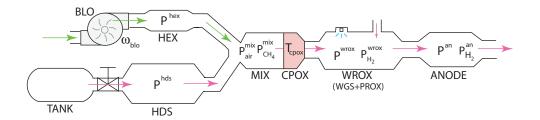


Fig. 2. FPS dynamic model

exchanger pressure, p^{hex} , HDS pressure, p^{hds} , mixer CH₄ partial pressure, $p^{mix}_{CH_4}$, mixer air partial pressure, p^{mix}_{air} , CPOX temperature, T_{cpox} , WROX (combined WGS and PROX) volume pressure, p^{wrox} , WROX hydrogen partial pressure, $p^{wrox}_{H_2}$, anode pressure, p^{an} , and anode hydrogen partial pressure, $p^{an}_{H_2}$. We provide here a brief outline of the model. Although, we use the linearized model for the control analysis and design, the physical interpretation of the states helps in the control design and in interpreting the results.

The speed of the blower, ω_{blo} , is modeled as a first-order dynamic system with time constant τ_b . The governing equation is

$$\frac{d\omega_{blo}}{dt} = \frac{1}{\tau_b} \left(\frac{u_{blo}}{100} \omega_0 - \omega_{blo} \right) \tag{6}$$

where u_{blo} is the blower command signal (range between 0 and 100) and ω_0 is the maximum blower speed (3600rpm). The gas flow rate through the blower is modeled, $W_{blo} = f(\omega_{blo}, \frac{p_{hex}}{p_{atm}})$, using a blower map. Mass conservation with the ideal gas law through the isothermal assumption is used to model the pressure dynamics of the gas in all component volumes considered in the system. In any volume that does not involve any reaction, mixture composition is unchanged and the total pressure of the gas is used as the state $(p_{hex}$ in HEX and p_{hds} in HDS). On the other hand, gas compositions in MIX, WROX and fuel cell anode (AN) changes due to reactions involved. The changes in gas composition in these volumes are described with additional partial pressures of the important species. In general, the pressure dynamics of a gas n in a volume m is governed by

$$\frac{dp_n^m}{dt} = \frac{RT_m}{M_n V_m} (W_{n,in}^m - W_{n,out}^m) \tag{7}$$

where R is the universal gas constant, V_m is the component gas volume, M_n is the molar mass of species n, and T_m is the temperature of the gas in the volume. The mass flow rate

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 $W_{n,in}^m$ is the rate (in (kg/s)) of the species n going into the volume m which includes the species flow into the volume and the species produced (from the reaction) in the volume. The flow rate $W_{n,out}^m$ are the rate of species n going out of the volume including the species flow rate exiting the volume and the rate of species reacted in the reaction.

The total flow rate, W, between two volumes is, in general, calculated from pressure differential, $p_1 - p_2$, using the orifice equation with a turbulent flow assumption

$$W = W_0 \sqrt{\frac{p_1 - p_2}{\Delta p_0}} \tag{8}$$

where W_0 and Δp_0 are the nominal air flow rate and the nominal pressure drop of the orifice, respectively. The flow rate of a constituent species n between the volumes is a function of the total gas flow and the mole fraction of the species n in the upstream volume. The flow rate of fuel (natural gas) into HDS, $W_{hds,in}$, is, in addition, a function of the valve input, u_{valve} ,

$$W_{hds,in} = \left(\frac{u_{valve}}{100}\right) W_{0,valve} \sqrt{\frac{p^{tank} - p^{hds}}{\Delta p_{0,valve}}}$$

$$\tag{9}$$

where p^{tank} is the fuel tank or supply line pressure.

The conversion of the gases in CPOX is based on the reactions in (1) and (2) and the selectivity defined in (3), which is a function of the oxygen to carbon ratio in MIX, λ_{O2C} :

$$\lambda_{O2C} = y_{O_2}^{atm} \frac{p_{air}^{mix}}{p_{CH_4}^{mix}} \tag{10}$$

where $y_{O_2}^{atm}$ is the oxygen mole fraction of the atmospheric air. The energy conservation principle is used to model the changes in CPOX temperature.

$$m^{cpx}C_P^{cpx}\frac{dT_{cpox}}{dt} = \begin{bmatrix} \text{inlet en-} \\ \text{thalpy} \\ \text{flow} \end{bmatrix} - \begin{bmatrix} \text{outlet} \\ \text{en-} \\ \text{thalpy} \\ \text{flow} \end{bmatrix} + \begin{bmatrix} \text{heat} \\ \text{from re-} \\ \text{actions} \end{bmatrix}$$
(11)

where m^{cpx} (kg) and C_P^{cpx} (J/kg·K) are mass and specific heat capacity of the catalyst bed, respectively. The terms on the right hand side of (11) are determined based on the reactants and products gas of the CPOX reactions. Further details of the model are presented in [14].

IV. CONTROL PROBLEM FORMULATION

As previously discussed, the main objectives of the FPS controller are (i) to protect the stack from damage due to H₂ starvation (ii) to protect CPOX from overheating and (iii) to keep overall system efficiency high, which includes high stack H₂ utilization and high FPS CH₄-to-H₂ conversion. Objectives (ii) and (iii) are related since maintaining the desired CPOX temperature during steady-state implies proper regulation of the oxygen-to-carbon ratio which corresponds to high FPS conversion efficiency.

Two performance variables that need to be regulated are the anode hydrogen mole fraction, $y_{{\scriptscriptstyle H_2}},$

$$y_{H_2} = \frac{p_{H_2}^{an}}{p^{an}} \tag{12}$$

calculated based on (7) and the CPOX temperature, T_{cpox} , calculated based on (11). They are chosen based on the following rationale. High T_{cpox} can cause the catalyst bed to be overheated and be permanently damaged. Low T_{cpox} results in a low CH₄ reaction rate in the CPOX [5] and potential methane slip. Large deviations of y_{H_2} are undesirable. On one hand, a low value of y_{H_2} means anode H₂ starvation [9], [15] which can permanently damage the fuel cell structure. On the other hand, a high value of y_{H_2} means small hydrogen utilization which results in a waste of hydrogen.

In this control study, we assume that all CH₄ that enters the CPOX reacts without any methane slip. Note that these assumptions reduce the validity of the model for large T_{cpox} deviations. The effect of the modeling error due to these assumptions can degrade the performance of the model-based controller. However, achieving one of the control goals, which is the regulation of T_{cpox} , will ensure that this modeling error remains small.

The H₂ valve actuator dynamics are ignored. The stack current, I_{st} , is considered as an exogenous input that is measured. Since the exogenous input is measured, we consider a two degrees of freedom (2DOF) controller based on feedforward and feedback, as shown in Figure 3. The two control inputs, u, are the air blower signal, u_{blo} , and the fuel valve signal, u_{valve} . The feedforward terms that provide the valve and the blower signals that reject the steady-state effect of current to the outputs are integrated in the plant: $u^*(I_{st}) = \begin{bmatrix} u^*_{blo}(I_{st}) & u^*_{valve}(I_{st}) \end{bmatrix}^T$. The value of u^* is obtained by nonlinear simulation and can be implemented with a lookup table. The performance variable are the CPOX

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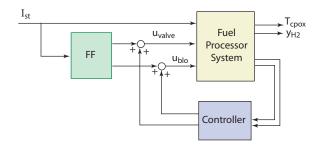


Fig. 3. Feedback control study

temperature, T_{cpox} , and the anode exit hydrogen mole fraction, y_{H_2} .

V. Analysis of Linearized Models

A linear model of the FPS is obtained by linearizing the nonlinear model. In this study, the desired steady-state is selected at stack H₂ utilization U_{H_2} =80% [13] and CPOX oxygen-to-carbon ratio $\lambda_{O2C} = 0.6$. This condition results in the value of CPOX temperature, $T_{cpox} = 972$ K (corresponds to $\lambda_{O2C} = 0.6$), and the value of anode hydrogen mole fraction, $y_{H_2} = 8.8\%$ (corresponds to $U_{H_2} = 80\%$). The control objective is therefore to regulate T_{cpox} at 972 K and y_{H_2} at 0.088. This desired value of T_{cpox} also agrees with the value published in the literature [16]. Static feedforward terms (illustrated in Figure 3) are included in the linear plant so that the steady-state T_{cpox} and y_{H_2} are maintained at nominal value during changes in stack current. The linearization of the plant is denoted by

$$\dot{x} = Ax + B_u u + B_w w$$

$$z = C_z x + D_{zu} u + D_{zw} w \tag{13}$$

where the state, x, input, u, disturbance, w, and performance variables, z, are

$$x = \begin{bmatrix} T_{cpox} & p_{H_2}^{an} & p^{an} & p^{hex} & \omega_{blo} & p^{hds} & p_{CH_4}^{mix} & p_{air}^{mix} & p_{H_2}^{wrox} & p^{wrox} \end{bmatrix}^T$$

$$w = I_{st} \qquad u = \begin{bmatrix} u_{blo} & u_{valve} \end{bmatrix}^T \qquad z = \begin{bmatrix} T_{cpox} & y_{H_2} \end{bmatrix}^T \qquad (14)$$

The matrices in (13) are given in the Appendix. All variables in the linear plant above are perturbations from the nominal. The current input is in Ampere. The blower and the valve signals, u_{blo} and u_{valve} , vary between 0 and 100. The outputs are the CPOX

temperature in Kelvin and the anode hydrogen mole fraction in percent. In the transfer function form, we can represent the plant as

$$z = \left[\begin{array}{cc} G_w & G \end{array} \right] \left[\begin{array}{c} w \\ u \end{array} \right] \tag{15}$$

The nonlinear plant model is linearized at three different current (load) levels that correspond to the 30%, 50%, and 80% of the plant power level. The Bode plots and step responses of the linear plants that are obtained from different system power levels are shown in Figures 4 and 5. For clarity, the units of current is (×10 Amp). Note first that the static feedforward controller does well in rejecting the effect from I_{st} to y_{H_2} and T_{cpox} in steady-state. The H₂ recovery using feedforward is, however, relatively slow. A feedback controller is, thus, needed to speed up the system behavior and to reduce the sensitivity introduced by modeling uncertainties.

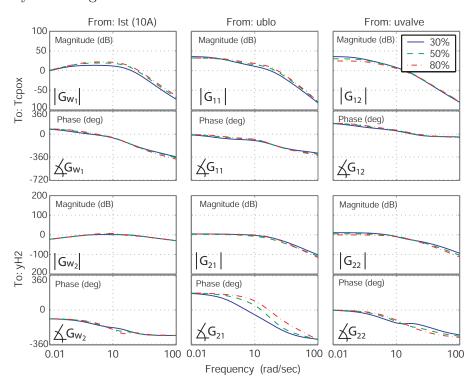


Fig. 4. Bode plot of linearized models at 30%, 50%, and 80% power

The responses of the output due to step changes in the actuator signals, in Figure 5, show a strongly coupled system. The fuel dynamics are slower than the air dynamics, primarily due to the large HDS volume. Note that a right half plane (RHP) zero exists in

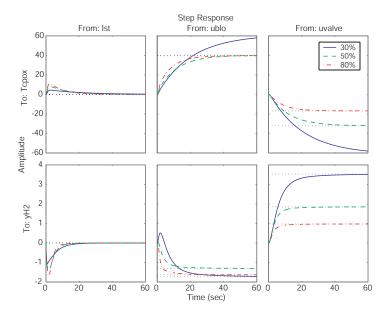


Fig. 5. Step responses of linearized models at 30%, 50%, and 80% power

the path $u_{blo} \to y_{H_2}$ can be easily detected from the initial inverse response of the y_{H_2} due to a step change in u_{blo} . Moreover, as can be seen in the step responses from u_{blo} to y_{H_2} , the RHP zero that causes the non-minimum phase behavior moves closer to the imaginary axis and causes larger initial inverse response at low power level (30%). The linearization of the system at the 50% power level is used in the control study in the following sections.

VI. INPUT-OUTPUT PAIRING

One of the most common approaches to controlling a multi-input multi-output (MIMO) system is to use a diagonal controller, which is often referred to as a decentralized controller. The decentralized control works well if the plant is close to diagonal which means that the plant can be considered as a collection of individual single-input single-output (SISO) sub-plants with no interaction among them. In this case, the controller for each sub-plant can be designed independently. If the interaction between the loops is large, then the performance of the decentralized controller may be poor.

Due to the non-minimum phase zero in the $u_{blo} \to y_{H_2}$ transfer function, the preferred pairing choices are $u_{blo} \to T_{cpox}$ pair and $u_{valve} \to y_{H_2}$ pair. This pairing choice is also confirmed by the relative gain array (RGA) matrix [17] of G,

$$RGA = G \times (G^{-1})^T \tag{16}$$

at zero frequency is

$$RGA(0 \text{ rad/s}) = \begin{bmatrix} 2.302 & -1.302 \\ -1.302 & 2.302 \end{bmatrix}$$
 (17)

The RGA can also be used to assess the loop interactions. Large off-diagonal elements of the RGA matrix indicates large loop interactions. A plot of the magnitude difference between the diagonal and off-diagonal elements of the RGA matrices in Figure 6 shows that the interactions increase at high frequencies [18], [17]. At low power levels, the values of the off-diagonal elements of the RGA matrix are even higher than the diagonal elements ($|RGA_{11}| - |RGA_{12}| < 0$), indicating large coupling. At these frequencies, we can expect poor performance from a decentralized controller.

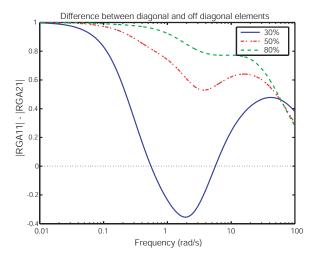


Fig. 6. Difference between diagonal and off-diagonal elements of the RGA matrix at different frequencies for three power setpoints

VII. DECENTRALIZED CONTROL

To illustrate the effect of the interactions, we design several PI controllers for the two single-input single-output (SISO) systems that correspond to the diagonal subsystem of G, i.e., $u_{blo} \to T_{cpox}$ (G(1,1)), and $u_{valve} \to y_{H_2}$ (G(2,2)). The diagram in Figure 7 shows the decentralized controller.

The gains of the PI controllers, K11 and K22, are chosen after iterations to achieve the best performance subject to actuator activity. Since fast response of y_{H_2} is more critical, the PI controller in the fuel loop $(u_{valve} \rightarrow y_{H_2})$ is tuned first to achieve fast

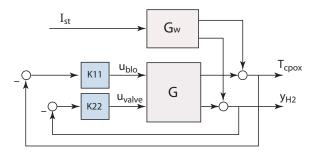


Fig. 7. Decentralized Control

response of y_{H_2} without saturating the valve. Then, to achieve fast regulation of T_{cpox} , we also tune the second PI for fast air loop while avoiding blower saturation. Figure 8 shows the response using fast controllers in both loops in dashed line, for the system at medium power (50%). Due to the large interaction as RGA predicted, the performance of the decentralized controller with fast controller in both loops degrades significantly when the system operate at low power as shown in Figure 9. One way to compensate for the interaction is to create a bandwidth separation between the two loops. Since designing the air loop to be faster than the fuel loop is not feasible with a PI controller due to blower magnitude constraints, the air loop is detuned to be slower than the fuel loop. Figures 8 and 9 also show the performance of the decentralized controller that has bandwidth separation. It can be seen that the speed of T_{cpox} regulation has to be sacrificed to prevent the degradation effect of the system interactions on the decentralized controller. The PI controllers chosen are given in Table II.

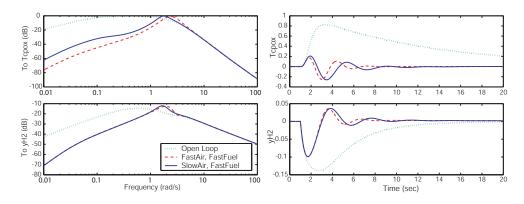


Fig. 8. Bode magnitude and unit step response of model at 50% power

Note that more complex decentralized controllers can be used (high-order or PID, for

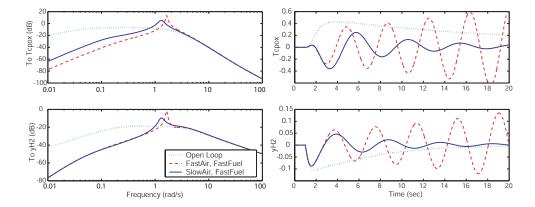


Fig. 9. Bode magnitude and unit step response of model at 30% power

example). The PI controller tuning here is used only to illustrate the effect of plant interactions and difficulties in tuning the PI controllers without systematic MIMO control tools. The conclusion from this section is that the large plant interactions illustrated by Figure 6 must be considered in the control design.

An interesting point is that, for the decentralized PI controller, the bandwidth of the air loop needs to be smaller than the bandwidth of the fuel loop. This was the only way to achieve a bandwidth separation within the blower saturation constraints. However, if a higher order controller is allowed, a higher closed loop bandwidth can be achieved. Indeed, as we show later in Section IX, a high-order decentralized controller using the diagonal terms of a full MIMO controller achieves a decade higher bandwidth than the fuel loop without saturating the blower.

VIII. Multivariable Control

We show in the previous section that the interactions in the plant limit the performance of the decentralized controller. In this section, we assess the improvement gained by a controller developed using a multivariable and model-based control design techniques. The controller is designed using linear quadratic (LQ) methodology.

To eliminate steady-state error, we add to the controller the integrators on the two performance variables, T_{cpox} and y_{H_2} . Note that, we assume that these two variables can

be directly and instantaneously measured. The state equations of the integrators are

$$\frac{d}{dt} \begin{bmatrix} q_1 \\ q_2 \end{bmatrix} = \begin{bmatrix} T_{cpox}^{ref} - T_{cpox} \\ y_{H_2}^{ref} - y_{H_2} \end{bmatrix}$$
(18)

where $T_{cpox}^{ref} = 972$ K and $y_{H_2}^{ref} = 8.8$ % are the desired values of T_{cpox} and y_{H_2} , respectively. In the linear domain, the desired deviation from the reference values is thus zero for all current commands. The controller is designed with the objective of minimizing the cost function

$$J = \int_0^\infty z^T Q_z z + q^T Q_I q + u^T R u \, dt \tag{19}$$

where Q_z , Q_I , and R are weighting matrices on the performance variables, z, integrator state, q, and control input, u, respectively.

The control law that minimizes (19) is in the form

$$u = -K_P(\hat{x} - x_d) - K_I q = -K \begin{bmatrix} (\hat{x} - x_d) \\ q \end{bmatrix}$$
 (20)

where K is the control gain and \hat{x} is the estimate of plant state. The values of K_P and K_I are given in Table III in the Appendix. Variable x_d in (20) is a function of I_{st} and can be viewed as the desired values of the states that give the desired value of z = 0. In other words, the term $K_p x_d$ is an additional feedforward term that compensates for the changes in the output steady-state value due to the feedback. As a result, this additional feedforward term is a function of the feedback gain, K_p . The value of x_d can be found by simulation or by the linear plant matrices (13). As it is based on the linear model, the value of x_d calculated will be different from the actual desired state in the nonlinear plant. The error in x_d definitely influences the steady-state error of the performance variables, T_{cpox} and y_{H_2} . The integral control implemented through the augmented integrators (18) then becomes more critical. The fact that x_d is not accurate must be taken into account when choosing the weighting between Q_z and Q_I . Large integrator gain slows down the response, thus relatively small Q_I shows a better (faster) performance in linear design. However, the response in nonlinear simulation with small Q_I gives poor steady-state performance since the performance is based heavily on the proportional part of the controller and therefore suffers from the error in x_d . Thus, if a more accurate value of x_d can not be obtained,

the transient performance must be compromised in order to get satisfactory steady-state performance of the controller through the integral part. Alternatively, a more accurate x_d can be obtained by numerically solving the nonlinear simulation and stored in a lookup table.

The estimate of the plant state, \hat{x} , can be determined using the dynamic model of the plant together with the available performance measurements. The observer state equations are

$$\dot{\hat{x}} = A\hat{x} + B_u u + B_w w + L(z - \hat{z})$$

$$\hat{z} = C_z \hat{x} + D_{zu} u + D_{zw} w$$
(21)

where \hat{x} is the estimator state vector and L is the estimator gain (Table III) determined based on LQG methodology.

The nonlinear simulation of the system with the decentralized PI feedback and with the output observer-based feedback is shown in Figure 10. The output feedback gives satisfactory performance in both y_{H_2} and T_{cpox} regulations.

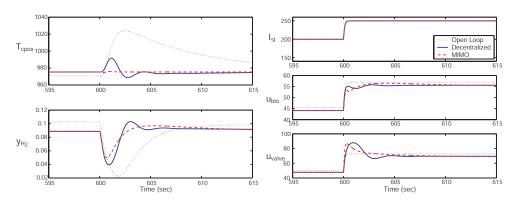


Fig. 10. Comparison of decentralized PI controller and observer feedback in nonlinear simulation

IX. Insight Gained by the Multivariable Design

The combination of the state feedback control (20) and the state observer (21) results in a model-based multivariable output-feedback controller. In transfer function form, the controller can be written as

$$u = C_w w + Cz = \begin{bmatrix} C_{w1} \\ C_{w2} \end{bmatrix} w + \begin{bmatrix} C_{11} & C_{12} \\ C_{21} & C_{22} \end{bmatrix} z$$
 (22)

The Bode plot of each element of the controller is shown in Figure 11.

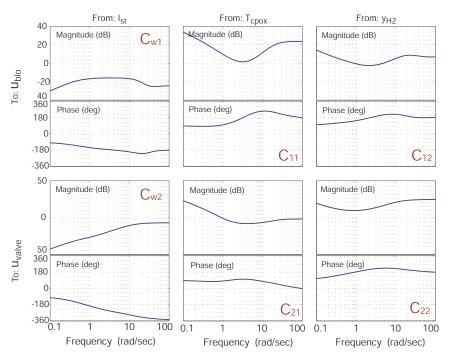


Fig. 11. Frequency response of the controller

In an effort to simplify the feedback controller for gain scheduling and implementation purposes, we investigate which cross-coupling term of the feedback contributes to the improvement by the MIMO controller. By zeroing out the cross-coupling term and plotting the closed loop frequency and time responses in Figures 12 and 13, we can see that the performance of the full controller is maintained when $C_{21} = 0$ (triangular MIMO controller). However, the performance degrades when $C_{12} = 0$ (diagonal MIMO controller). Thus it is clear that the C_{12} term is the critical cross-coupling term that provides the MIMO control improvement. This analysis gives a different result, however, if the air loop bandwidth is allowed to be higher, for example, by using a more powerful and faster blower. We can then lower the LQ weight on u_{blo} in the state feedback design. There is more actuator activity (high bandwidth controller) of u_{blo} and the diagonal controller ($C_{12} = C_{21} = 0$) performs similarly to the full multivariable controller.

The importance of C_{12} is interpreted as follows. Following Figure 14, the current disturbance, I_{st} , affects more y_{H_2} than T_{cpox} during fast transient as can be seen by the large high-frequency magnitude of the transfer function from I_{st} to y_{H_2} (Figure 15) for the plant

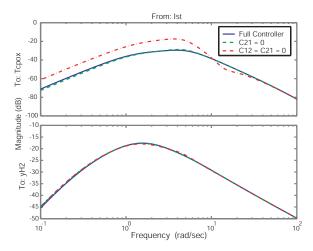


Fig. 12. Closed-loop frequency response for analysis of elements in the feedback controllers

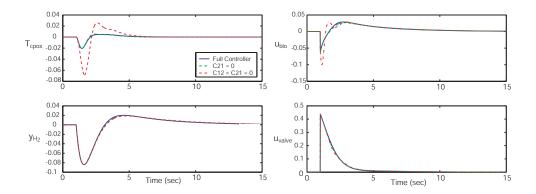


Fig. 13. Closed-loop time response for analysis of elements in the feedback controllers

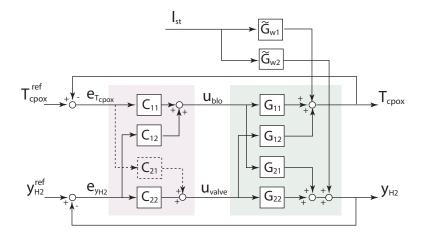


Fig. 14. Block Diagram of FPS plant and simplified controller

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with feedforward control: $\tilde{G}_w = G_w + GC_w$. The valve signal, u_{valve} , tries to reject the

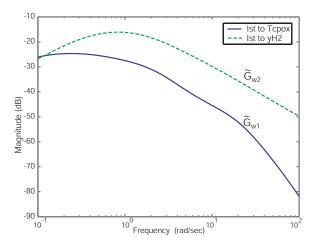


Fig. 15. Frequency magnitude plot of the plant with dynamic feedforward part of the controller \tilde{G}_{zw} in (IX)

effect of $\tilde{G}_{w2}I_{st}$ to y_{H_2} (see Figure 14) by using the feedback C_{22} term through G_{22} . The blower signal, on the other hand, cannot reject the $\tilde{G}_{w2}I_{st}$ to y_{H_2} through $G_{21}C_{12}$ because of the non-minimum phase zero of G_{21} ($z_{NMP}=3.07$).

$$\frac{\tilde{G}_{w2}I_{st}}{1 + G_{21}C_{12} + G_{22}C_{22}} \simeq \frac{\tilde{G}_{w2}I_{st}}{1 + G_{22}C_{22}}$$

Indeed, Figure 11 shows that the magnitude of C_{12} is low at frequencies close to that of the NMP zero. Meanwhile, the valve that tries hard to reject the $\tilde{G}_{w2}I_{st}$ to y_{H_2} causes disturbances to T_{cpox} through the plant G_{12} interaction. The controller cross-coupling term C_{12} is thus needed to compensate for the effect of u_{valve} to T_{cpox} by partially cancelling $G_{12}C_{22}$ by $G_{11}C_{12}$ at certain frequencies.

$$T_{cpox} = \frac{G_{12}C_{22} + G_{11}C_{12}}{1 + G_{11}C_{11}} e_{y_{H_2}} \approx 0 \Rightarrow C_{12} \approx -G_{11}^{-1}G_{12}C_{22}$$

Note that this partial cancellation involves the plant elements G_{11} and G_{12} that do not change significantly for different power levels, as compared to G_{21} (see Figure 4). Thus the benefit of the controller cross-coupling term C_{12} is maintained in full range of operating power. If the air loop has high bandwidth, the $G_{11}C_{11}$ term can reject the disturbance by itself and, then, controller C_{12} is not needed to cancel the interaction from the valve to T_{cpox} .

Figure 11 also verifies that C_{21} does not contribute to the overall MIMO controller. The magnitude of C_{21} is, in fact, relatively smaller than other feedback terms. At high frequencies where the effect of $\tilde{G}_{w2}I_{st}$ to y_{H_2} is large, the term C_{21} is not used to help regulating y_{H_2} because the deviation in y_{H_2} is not reflected in T_{cpox} measurement ($\tilde{G}_{w1}I_{st}$ is small). At low frequencies where I_{st} affects T_{cpox} , C_{21} may be used to help reduce T_{cpox} error but will cause disturbance to the well-behaved fuel loop, thus C_{21} is also insignificant at low frequencies.

By comparing the response of decentralized PI controller in Figure 10 and that of the diagonal MIMO controller in Figure 13, we can see that the diagonal controller derived from the MIMO controller outperforms the decentralized PI controller. This is achieved as shown in Figure 16 because of the higher closed loop bandwidth of the air loop when compared with the one of the PI-based controller. As seen in Figure 11, the high-order C_{11} term can have high bandwidth without having high gain and thus avoids blower saturation. This can not be achieved using a PI controller. Indeed, Figure 11 verifies that the gain of C_{11} is low at the frequencies where loop-interaction is large (see Figure 6 for the loop interactions).

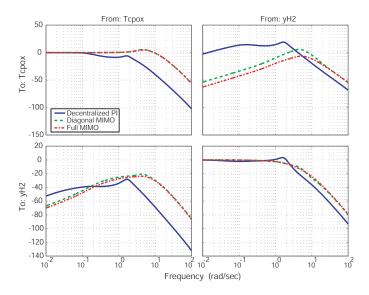


Fig. 16. Frequency (magnitude in dB) response from reference signal of closed loop system with MIMO controller

In summary, the MIMO controller achieves a superior performance in comparison with the decentralized PI controller due to two factors. First, the MIMO controller achieves a

high bandwidth on the air loop without saturating the actuator by achieving high bandwidth without high gain. This is only feasible with high-order controllers. In hindsight of the success of the C_{11} term of the MIMO controller, one can design a PID or a PI + lead-lag controller that reproduces similar gain and phase to be used in the decentralized controller.

Second, the MIMO controller achieves better coordination between the two actuators by utilizing a cross-coupling term. The cross-coupling term acts in a "feedforward" sense and changes the blower command based on how the fuel valve behaves. This partially cancels the interaction between the fuel valve to the air loop. This partial cancellation, luckily, involves plant elements that do not change significantly for different power levels. Thus, without having explicitly designed for robustness, the MIMO controller maintains its performance at all power levels.

X. CONCLUDING REMARKS

The control problem of hydrogen generation using catalytic partial oxidation and prevention of fuel cell stack starvation is studied. The two-input two-output control problem has the air blower and the fuel valve as inputs and the CPOX temperature and the anode hydrogen mole fraction (anode starvation) as performance variables.

We show that tuning two PI controllers for the air and the fuel loops is difficult. Moreover, the closed loop performance is adversely affected by the intrinsic interaction between the two loops. One way to prevent the performance degradation is to have bandwidth separation between the two control loops. This introduces a compromise of the air-temperature closed loop response in favor to the fuel-hydrogen loop.

On the other hand, a model-based high-order controller designed using linear multivariable methodologies, LQR-LQG in our case, can achieve very good response for a wide range of operating conditions. Our analysis shows that the multivariable controller can be simplified to a lower triangular controller where the blower command depends on both errors in T_{cpox} and y_{H_2} (or, equivalently, fuel valve). If the multivariable controller is further simplified to a diagonal controller (no cross-coupling between control inputs and errors in the performance variables), the closed loop performance degrades with respect to the full multivariable controller but it still outperforms the two PI-based closed loop performance.

Apart from these application specific recommendations, our analysis demonstrated that the improvement of the MIMO controller exists for fundamental and physically motivated reasons. This understanding made the non-control engineers involved in this project appreciate the complexity in the model-based control design and support the next phase of experimental validation.

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APPENDIX

TABLE I FPS LINEAR MODEL SYSTEM MATRICES

Α										Bu		B_W
-0.074	0	0	0	0	0	-3.53	1.0748	0	1E-06	0	0	0
0	-1.468	-25.3	0	0	0	0	0	2.5582	13.911	0	0	-0.328
0	0	-156	0	0	0	0	0	0	33.586	0	0	-0.024
0	0	0	-124.5	212.63	0	112.69	112.69	0	0	0	0	0
0	0	0	0	-3.333	0	0	0	0	0	0.12	0	0.0265
0	0	0	0	0	-32.43	32.304	32.304	0	0	0	0.1834	0.0504
0	0	0	0	0	331.8	-344	-341	0	9.9042	0	0	0
0	0	0	221.97	0	0	-253.2	-254.9	0	32.526	0	0	0
0	0	2.0354	0	0	0	1.8309	1.214	-0.358	-3.304	0	0	0
0.0188	0	8.1642	0	0	0	5.6043	5.3994	0	-13.61	0	0	0
C_{Z}										D_{zu}		D_{ZW}
1	0	0	0	0	0	0	0	0	0	0	0	0
0	0.994	-0.088	0	0	0	0	0	0	0	0	0	0

TABLE II DECENTRALIZED PI CONTROLLERS

Controller	Transfer Function
K11	$0.0135 \frac{(5.6s+1)}{s}$
K22	$0.165 \frac{(21s+1)}{s}$

TABLE III FPS CONTROLLER GAINS

K_{P}									
1.4054	0.18237	0.02904	1.0661	39.04	-6.6114	-0.70528	0.60367	0.76664	0.93881
-0.13028	1.1503	-0.13157	-0.24436	-8.422	6.1105	0.61755	-0.13879	3.787	0.12691
K_{l}									
-1.2071	-0.16911								
0.18907	-0.89972								
L									
469.67	138.59								
5.6245	818.34								
-93.622	-12.759								
-742.29	-99.077								
-30.245	-4.7928								
-795.89	-104.2								
-2149.2	-392.69								
1400.7	294.09								
1559.8	3547.1								
-430.89	-58.728								