

## Chapter 4. Exercises

1. If  $\psi$  happens to be an eigenfunction of an operator  $\hat{A}$  with the eigenvalue  $a$ , evaluate the expectation value  $\langle A \rangle$ .
2. Discuss why the noncommutativity of observables is not generally significant in everyday life. For example, why can we simultaneously measure the instantaneous position and momentum of a pitched baseball with confidence?
3. Evaluate the commutator  $[x, p_x]$  used to derive the Heisenberg uncertainty principle. Hint: First compute the quantity  $x\hat{p}_x f(x) - \hat{p}_x x f(x)$ , where  $f(x)$  is an arbitrary function.
4. Convince yourself of the correctness of the commutation relation

$$[L_x, L_y] = i\hbar L_z$$

5. Can you measure simultaneously a particle's  $y$  position coordinate and  $x$ -component of momentum?