

How to Falsify a Dark Energy Paradigm

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[On sabbatical at MPA and Excellence Cluster, Jan-Aug 2015]

Key Collaborators:

Eduardo Ruiz, Dan Shafer (grad students, Michigan)

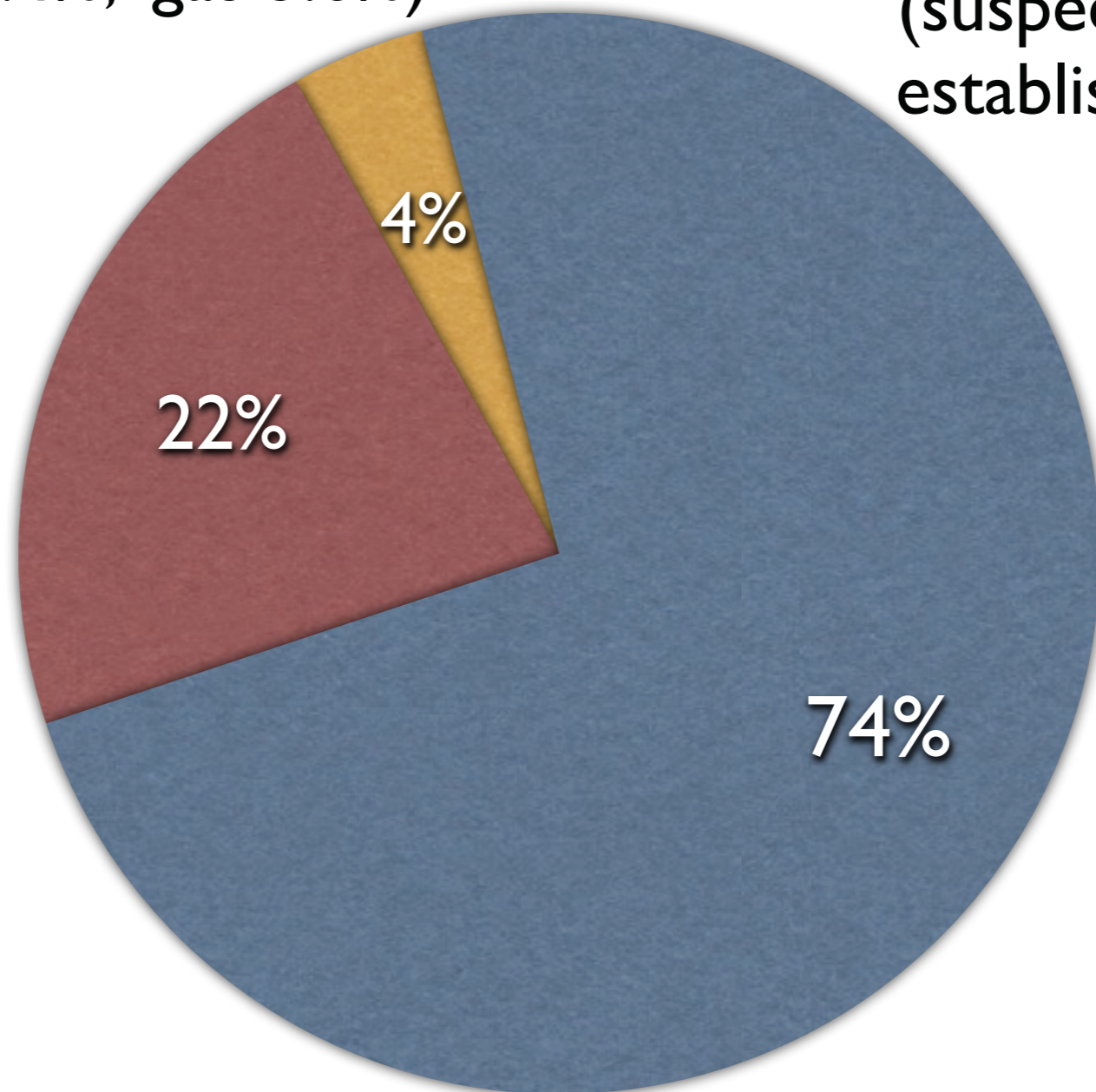
Makeup of universe **today**

Visible Matter
(stars 0.4%, gas 3.6%)

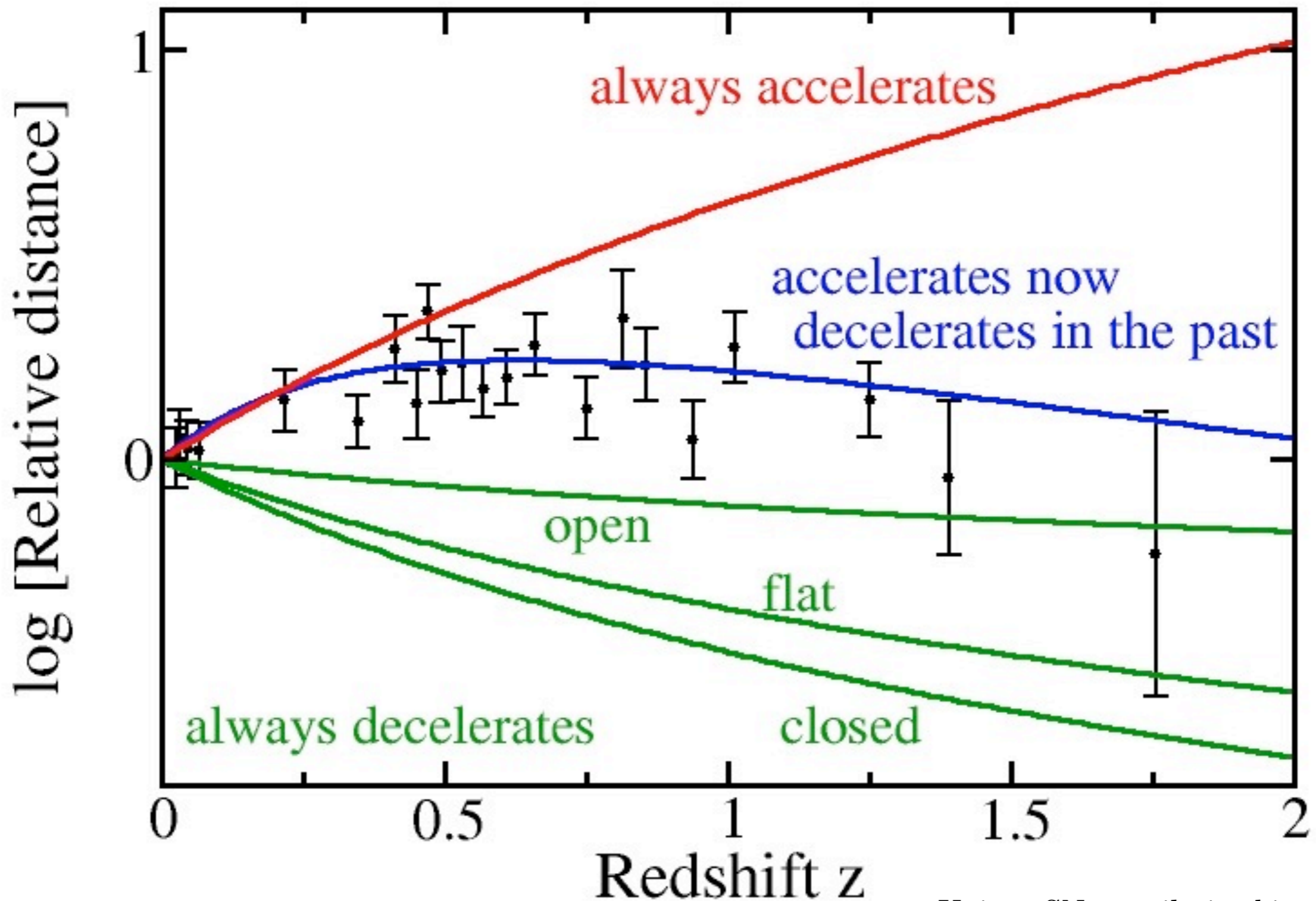
Dark Energy
(suspected since 1980s
established since 1998)

Dark Matter
(suspected since 1930s
established since 1970s)

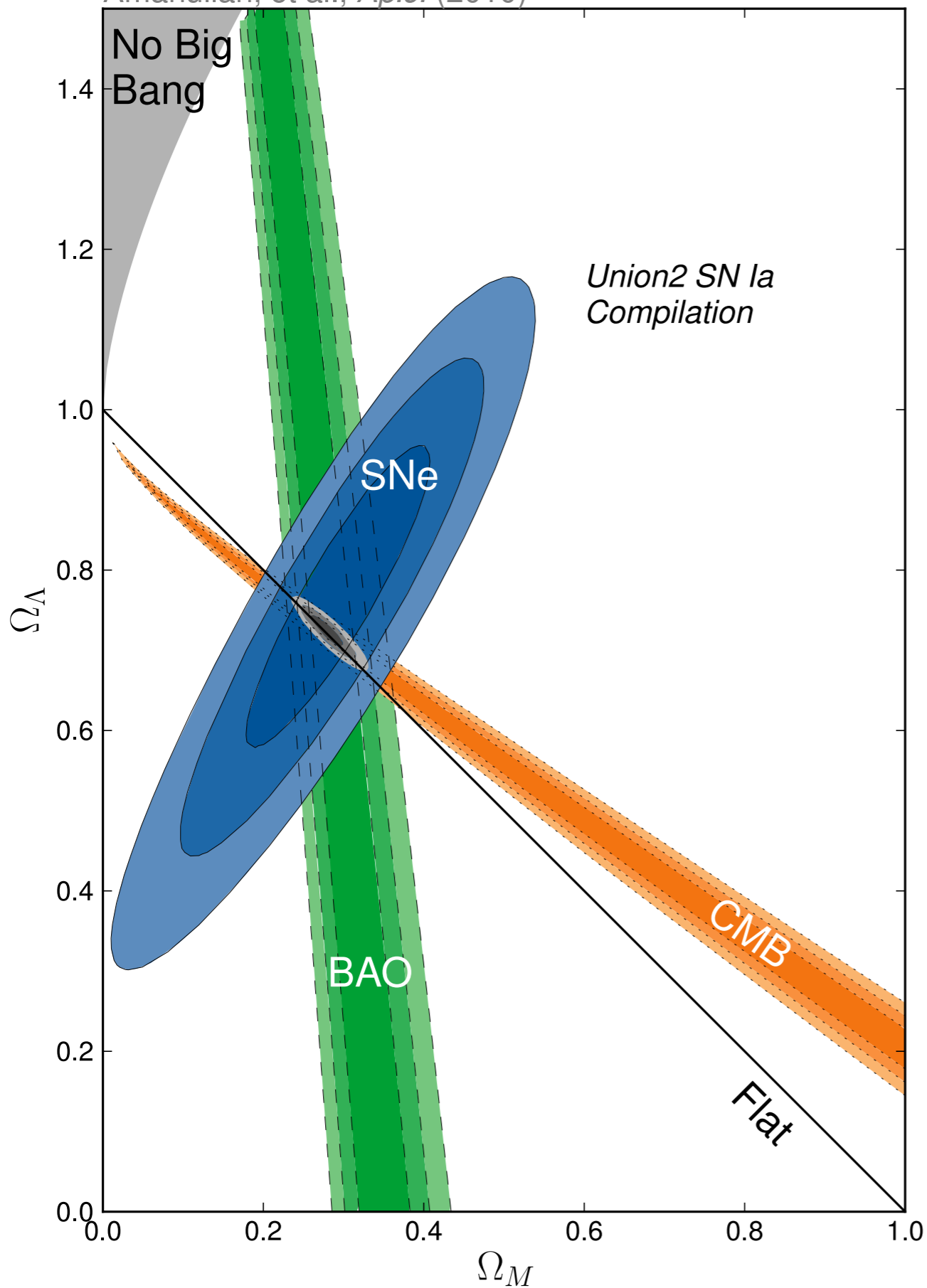
Also:
radiation (0.01%)



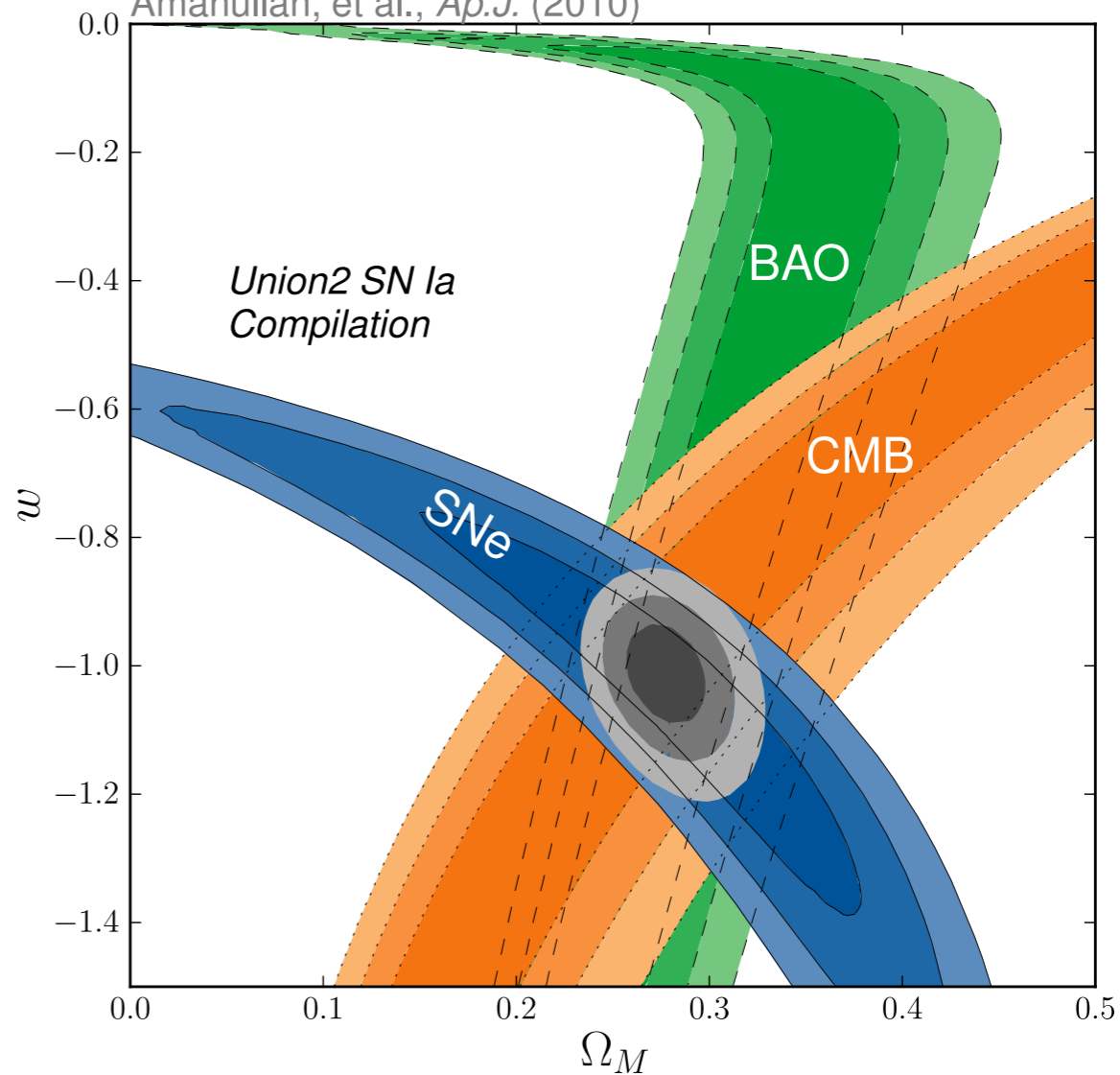
Evidence for Dark energy from type Ia Supernovae



Supernova Cosmology Project
 Amanullah, et al., *Ap.J.* (2010)



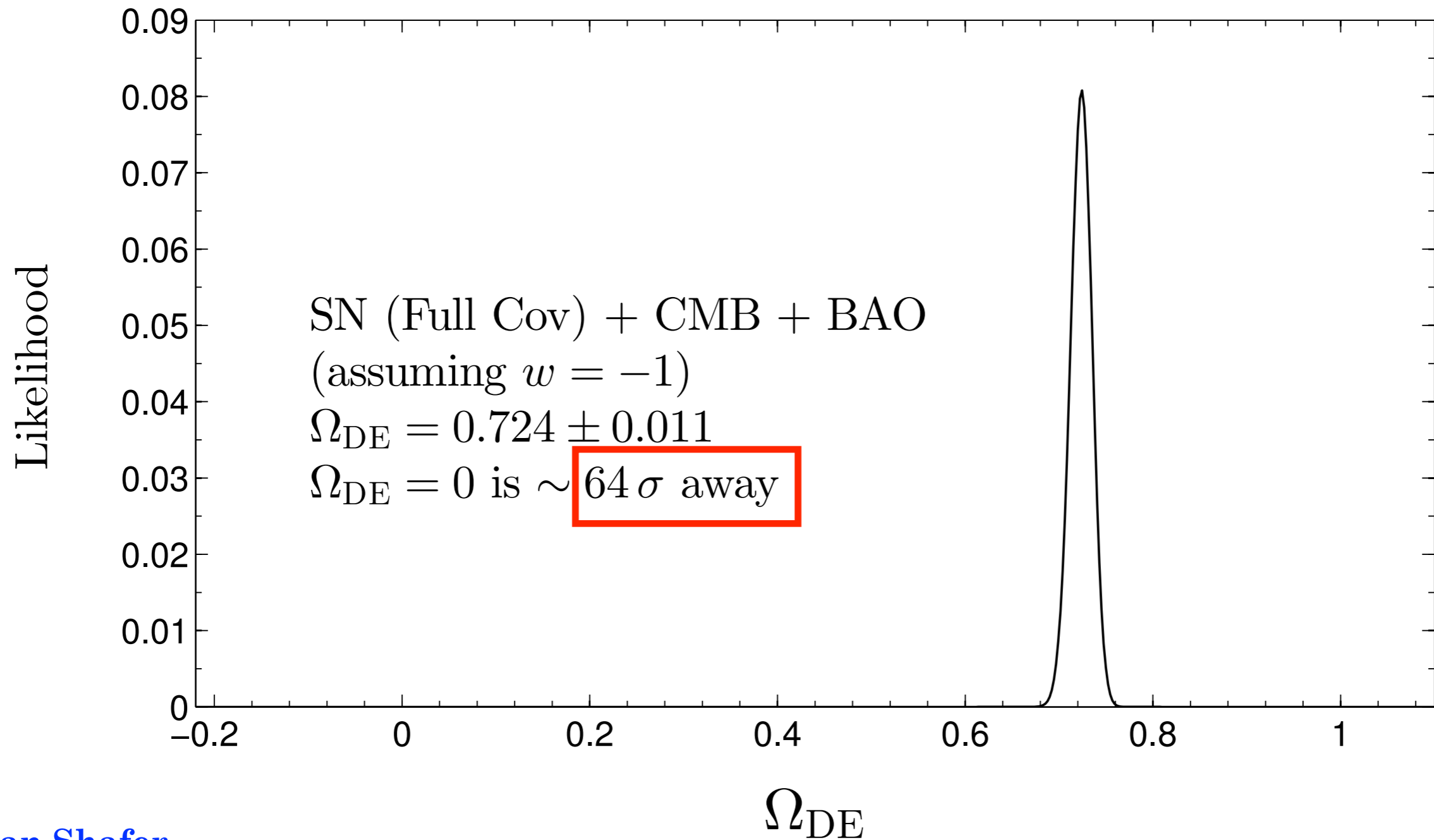
Supernova Cosmology Project
 Amanullah, et al., *Ap.J.* (2010)



$$\Omega_{\text{DE}} \equiv \frac{\rho_{\text{DE}}}{\rho_{\text{crit}}}$$

$$w \equiv \frac{p_{\text{DE}}}{\rho_{\text{DE}}}$$

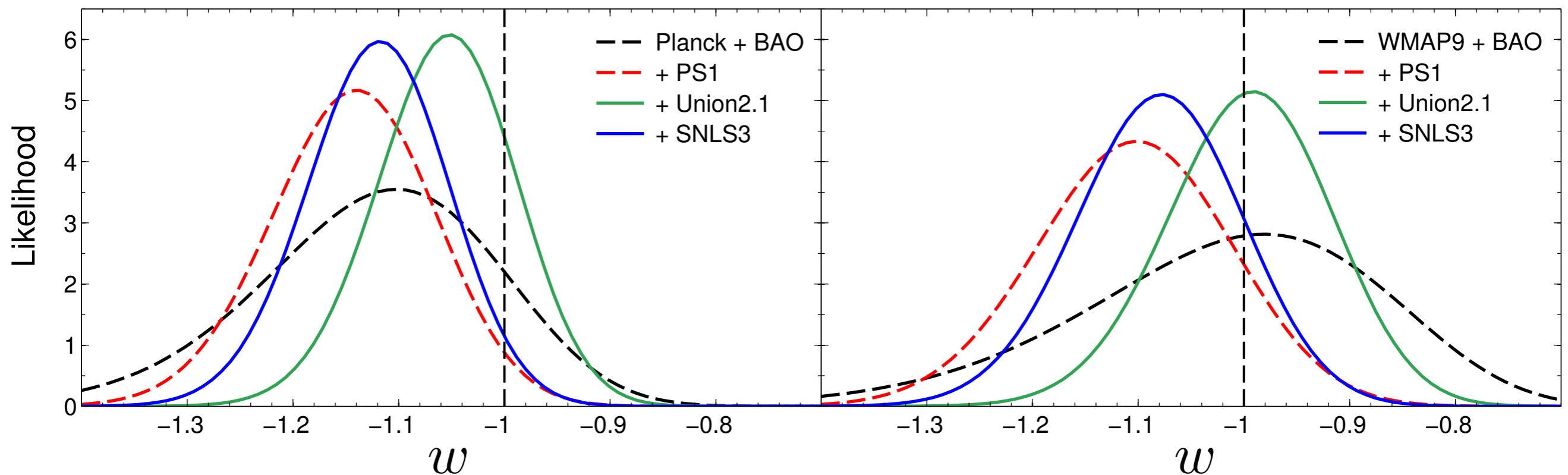
Current evidence for dark energy is impressively strong



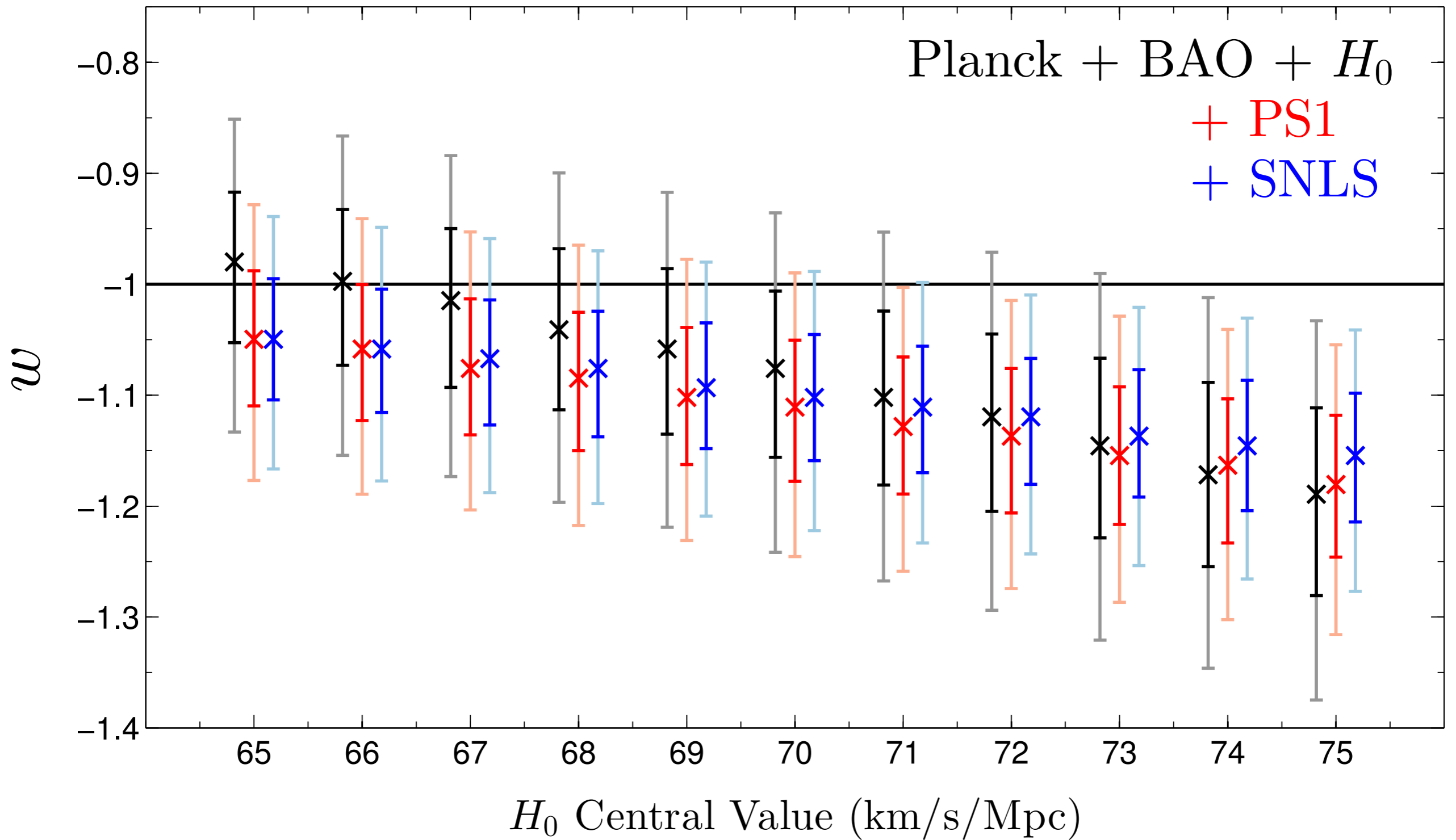
Hints that $w < -1$??

Planck+BAO+SN

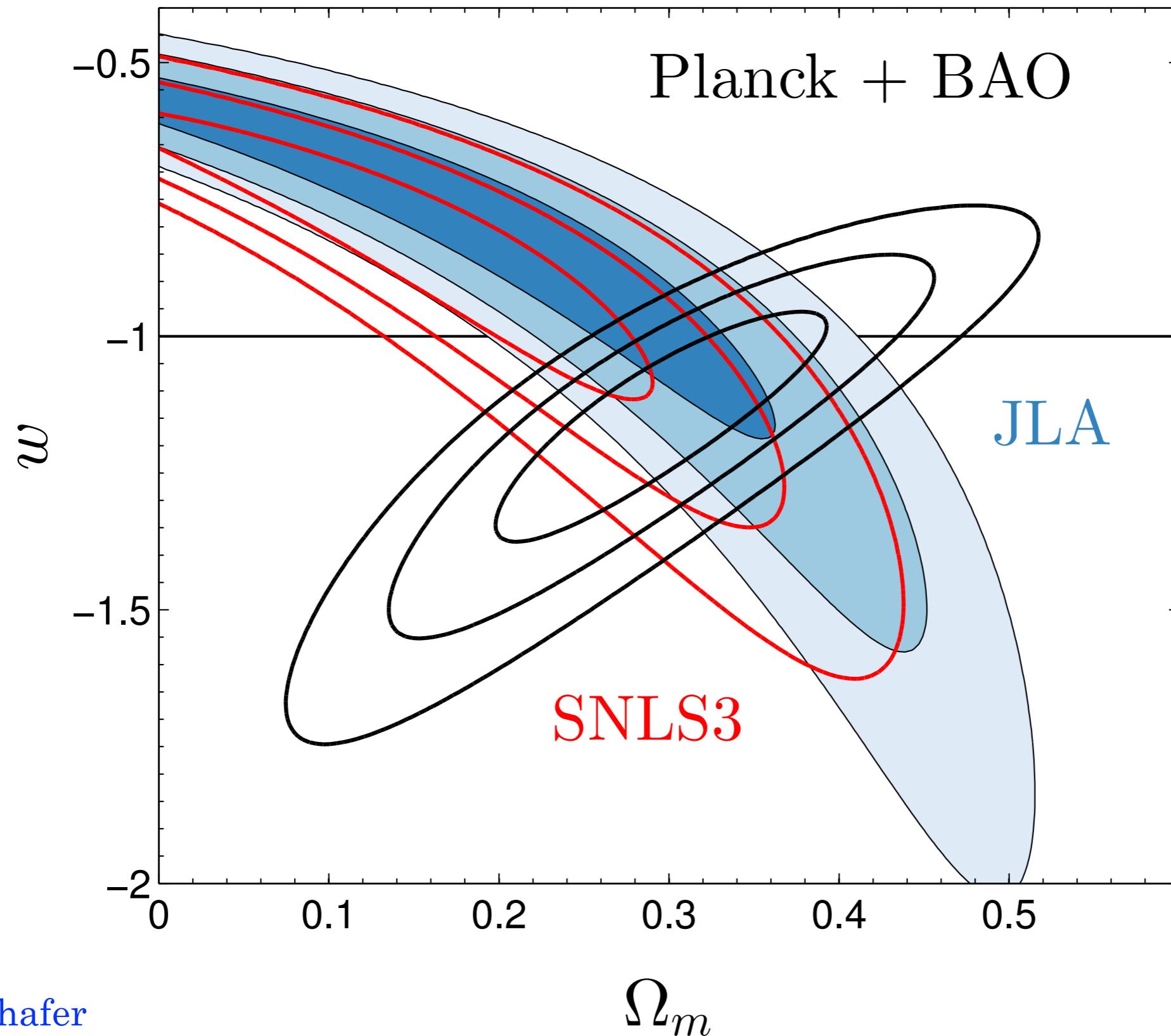
WMAP+BAO+SN



Only if $H_0 \approx 71$ and Planck assumed



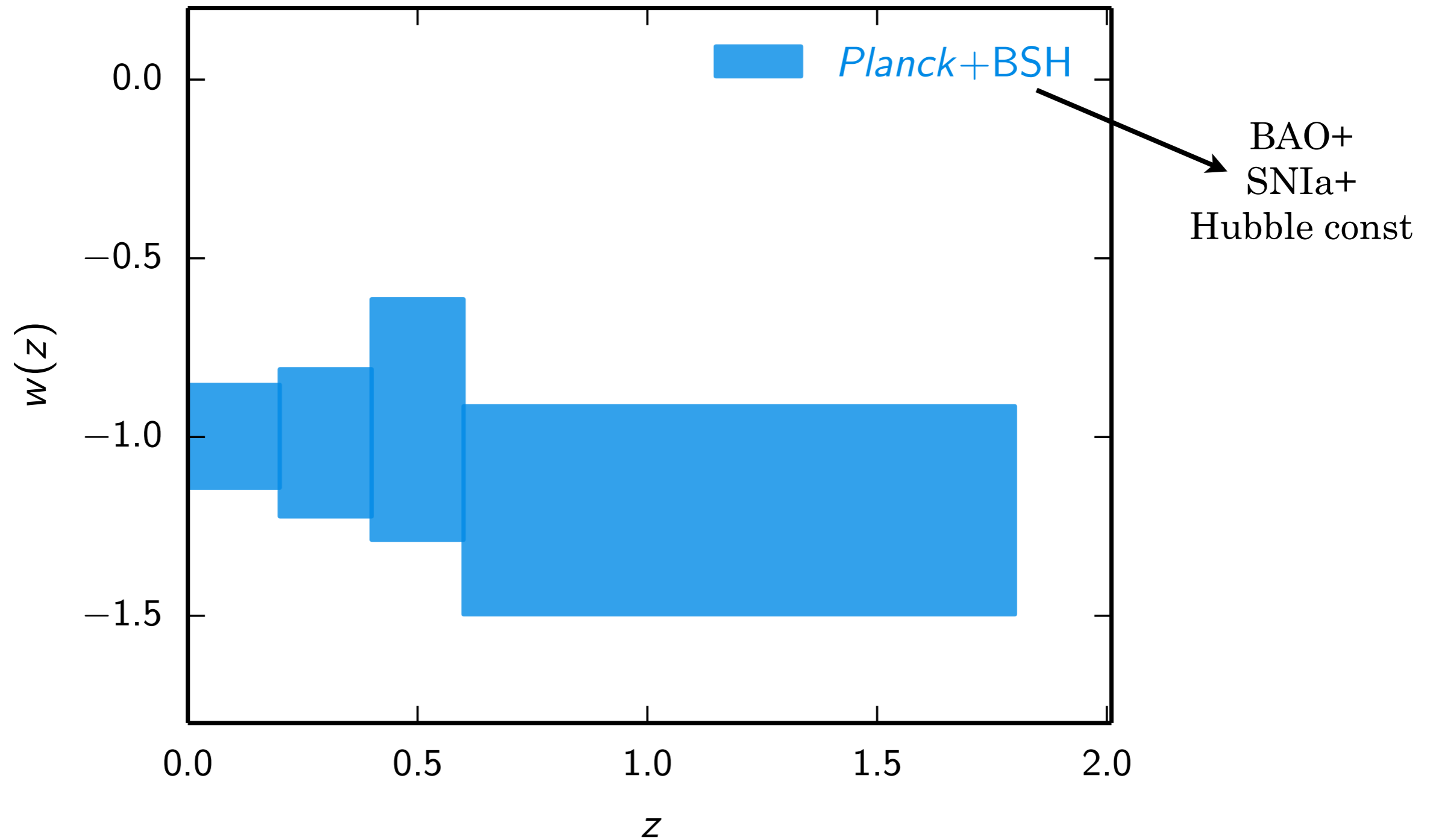
SN datasets and dark energy constraints



Big questions

1. Is DE something other than vacuum energy?
2. Does GR self-consistently describe cosmic acceleration?

Current constraints on $w(z)$: largely from geometrical measures



Remainder of talk

Part I: testing DE with geometry and growth

Part II: making predictions for DE observables

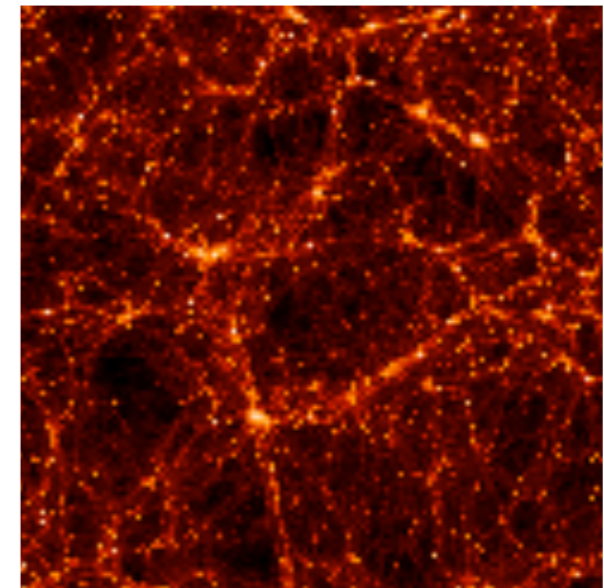
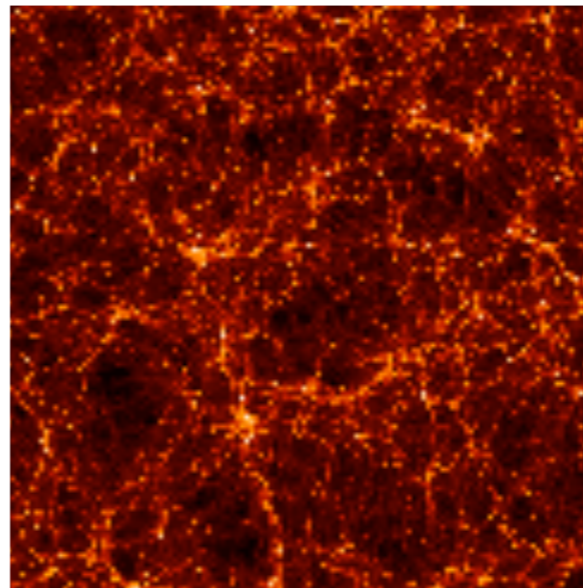
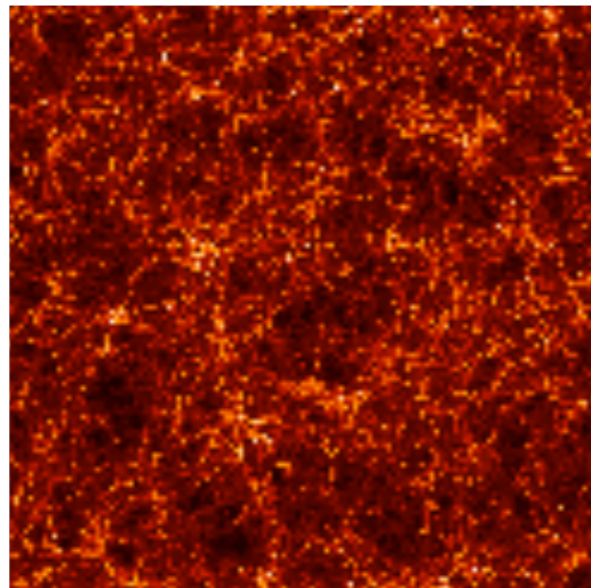
Dark Energy **suppresses** the growth of density fluctuations

($a=1/4$ or $z=3$)
1/4 size of today

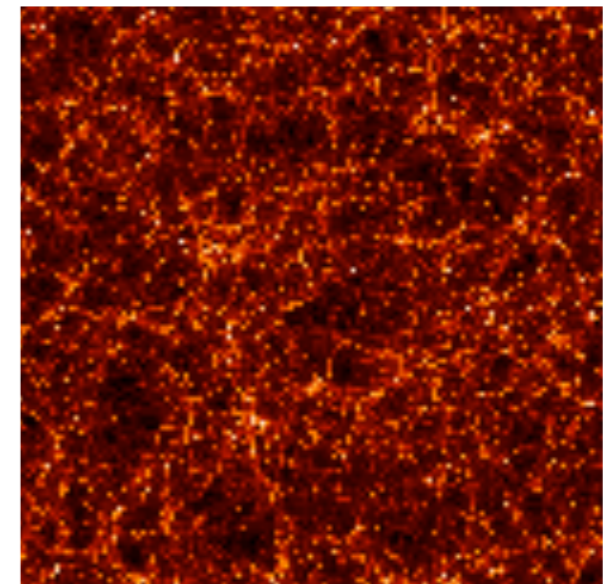
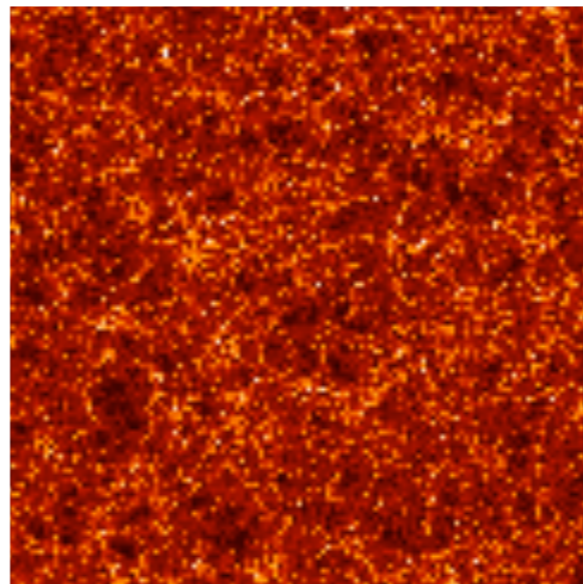
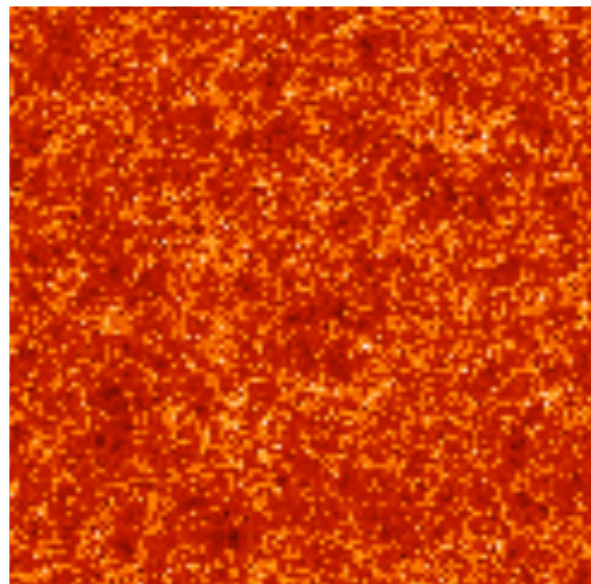
($a=1/2$ or $z=1$)
1/2 size of today

($a=1$ or $z=0$)
Today

with DE



without
DE



Idea: compare geometry and growth

e.g. Wang, Hui, May & Haiman 2007

Our approach:

Double the standard DE parameter space

($\Omega_M=1-\Omega_{DE}$ and w):

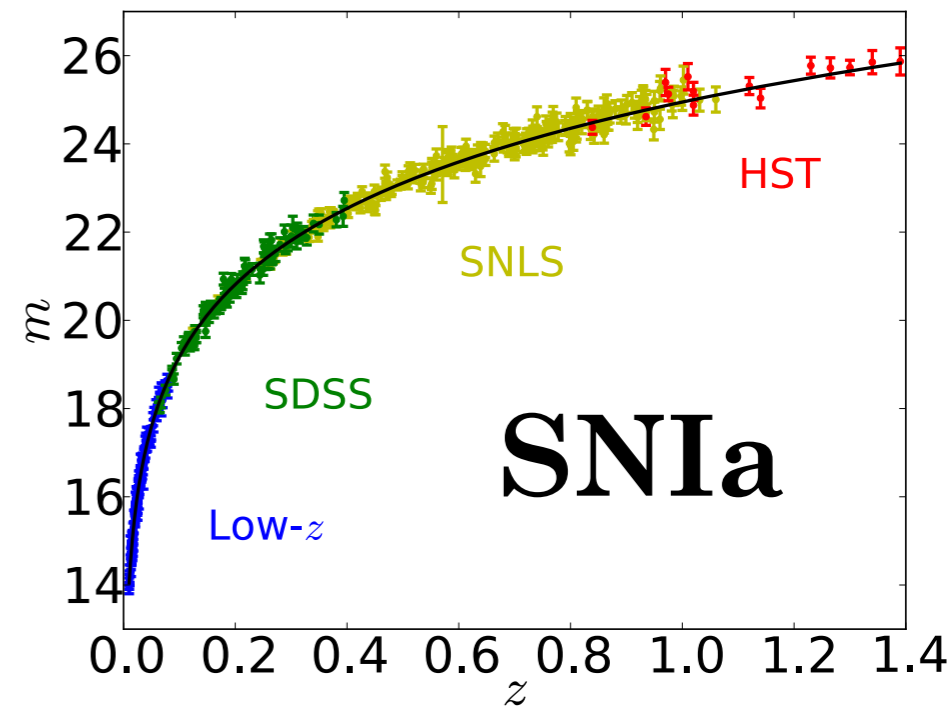
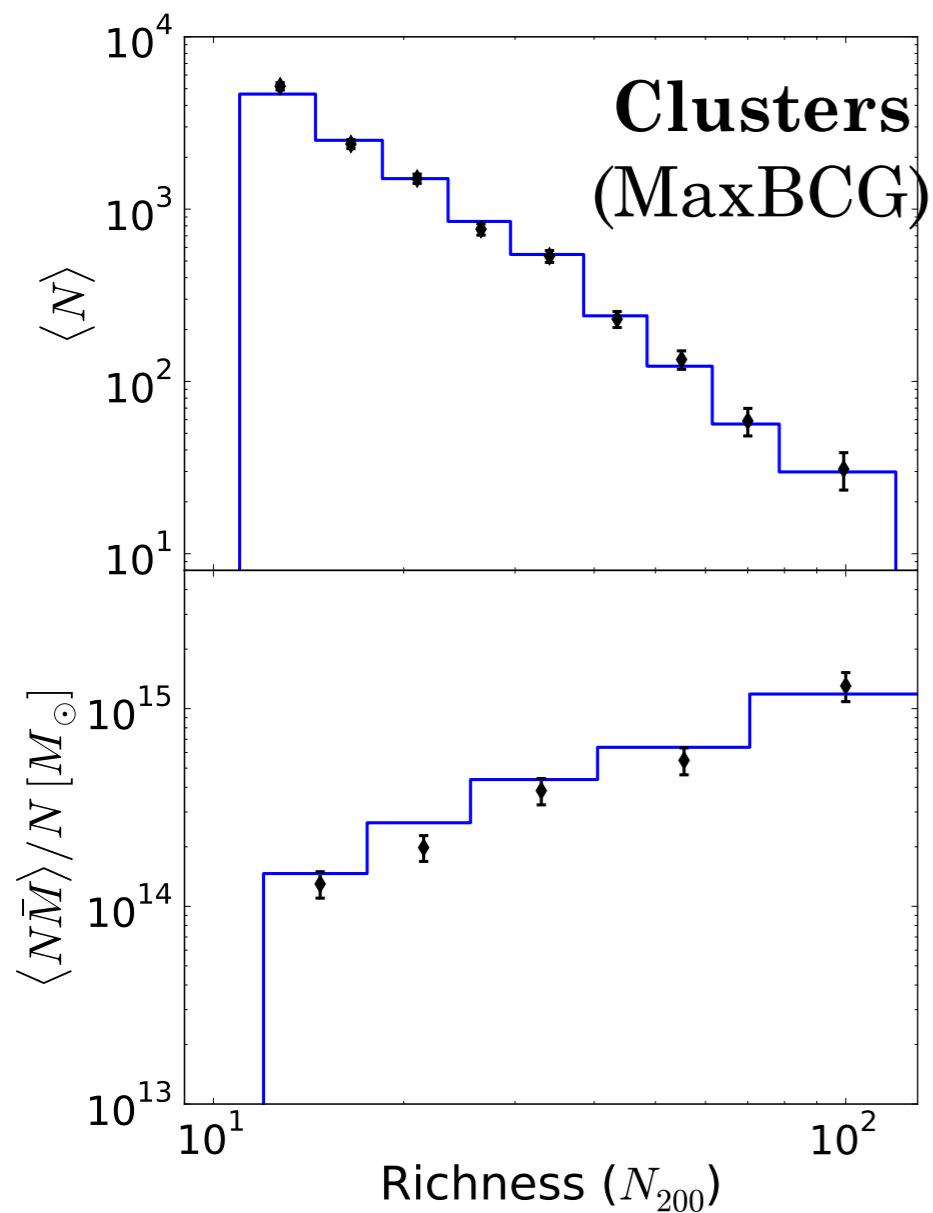
$\Rightarrow \Omega_M^{\text{geom}}, w^{\text{geom}} \quad \Omega_M^{\text{grow}}, w^{\text{grow}}$

[In addition to other:

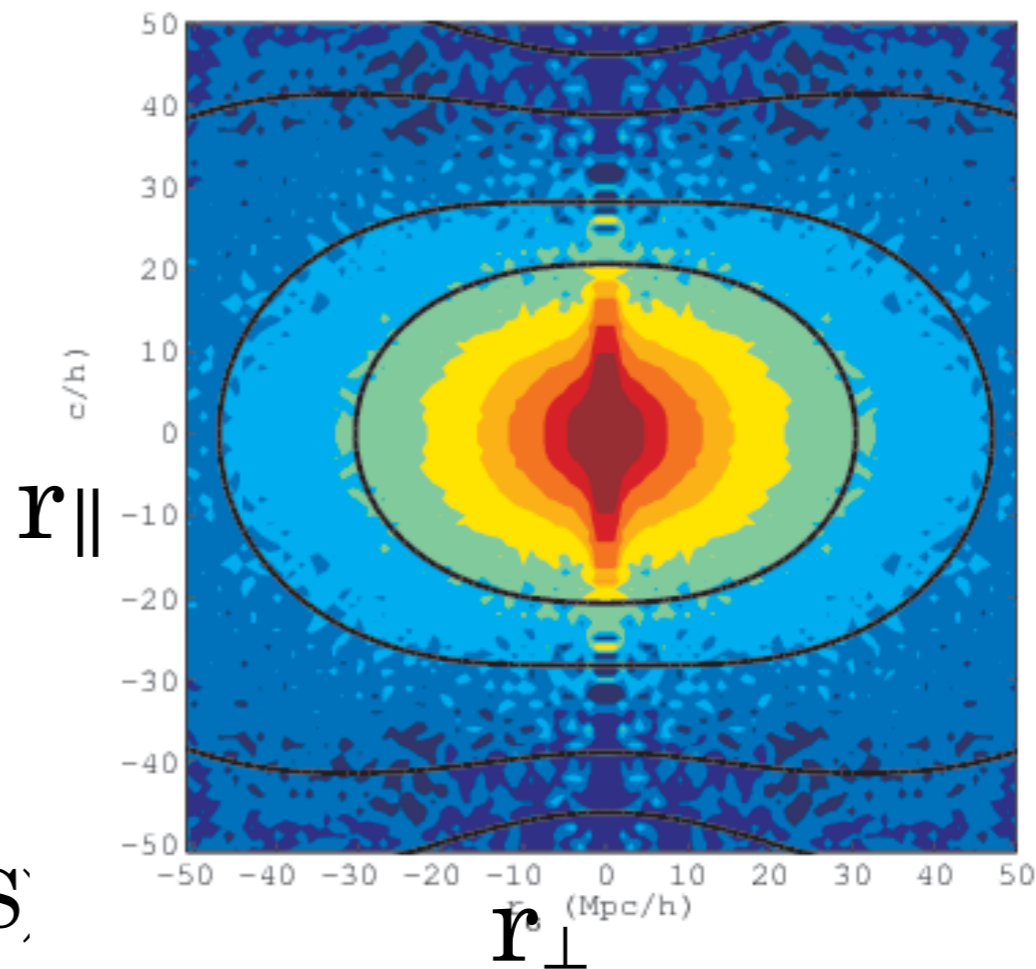
standard parameters: $\Omega_M h^2$ $\Omega_B h^2$, n_s , A)

nuisance parameters: probe-dependent]

(Current) Data used



RSD



CMB (Planck peak location)

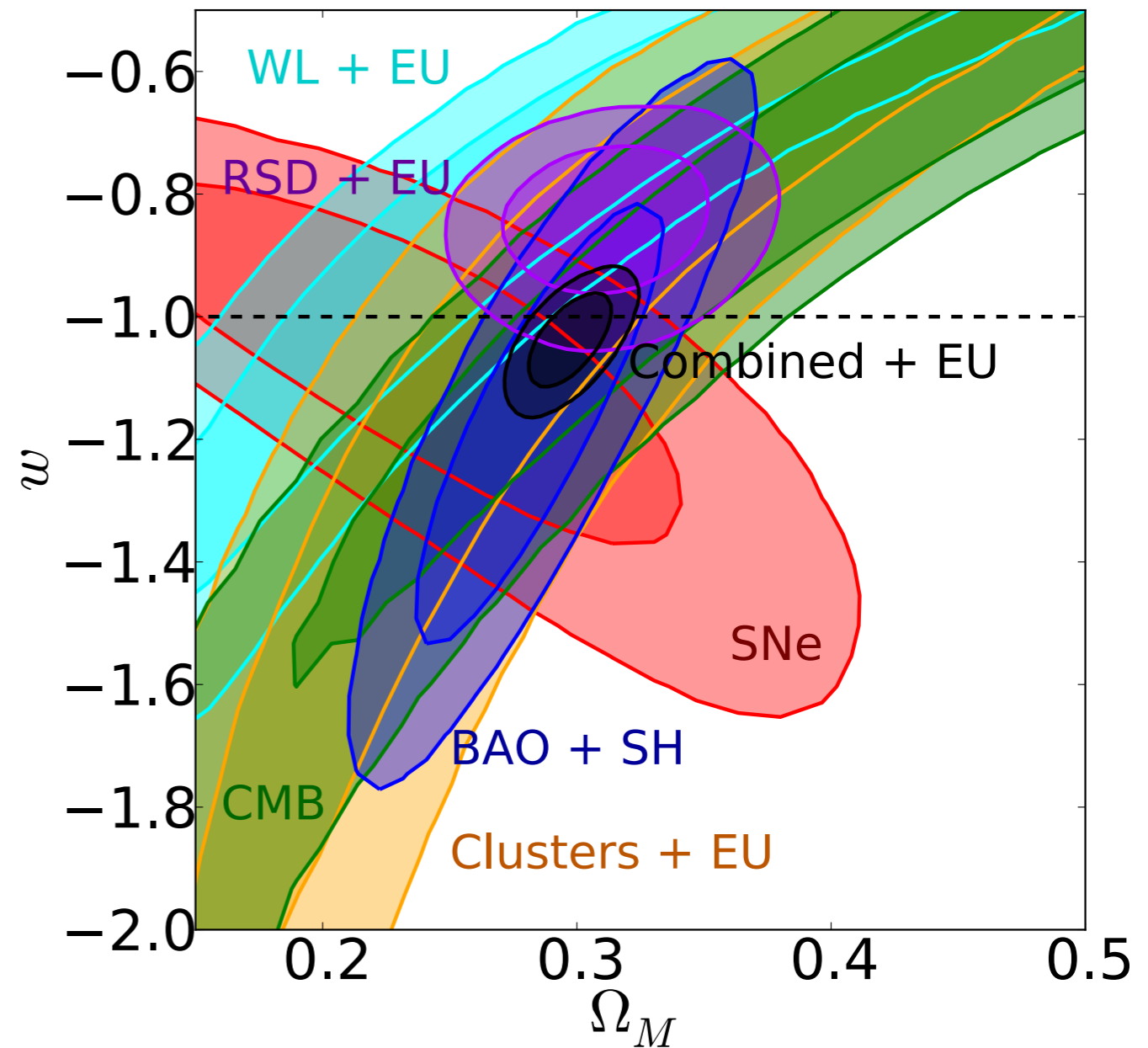
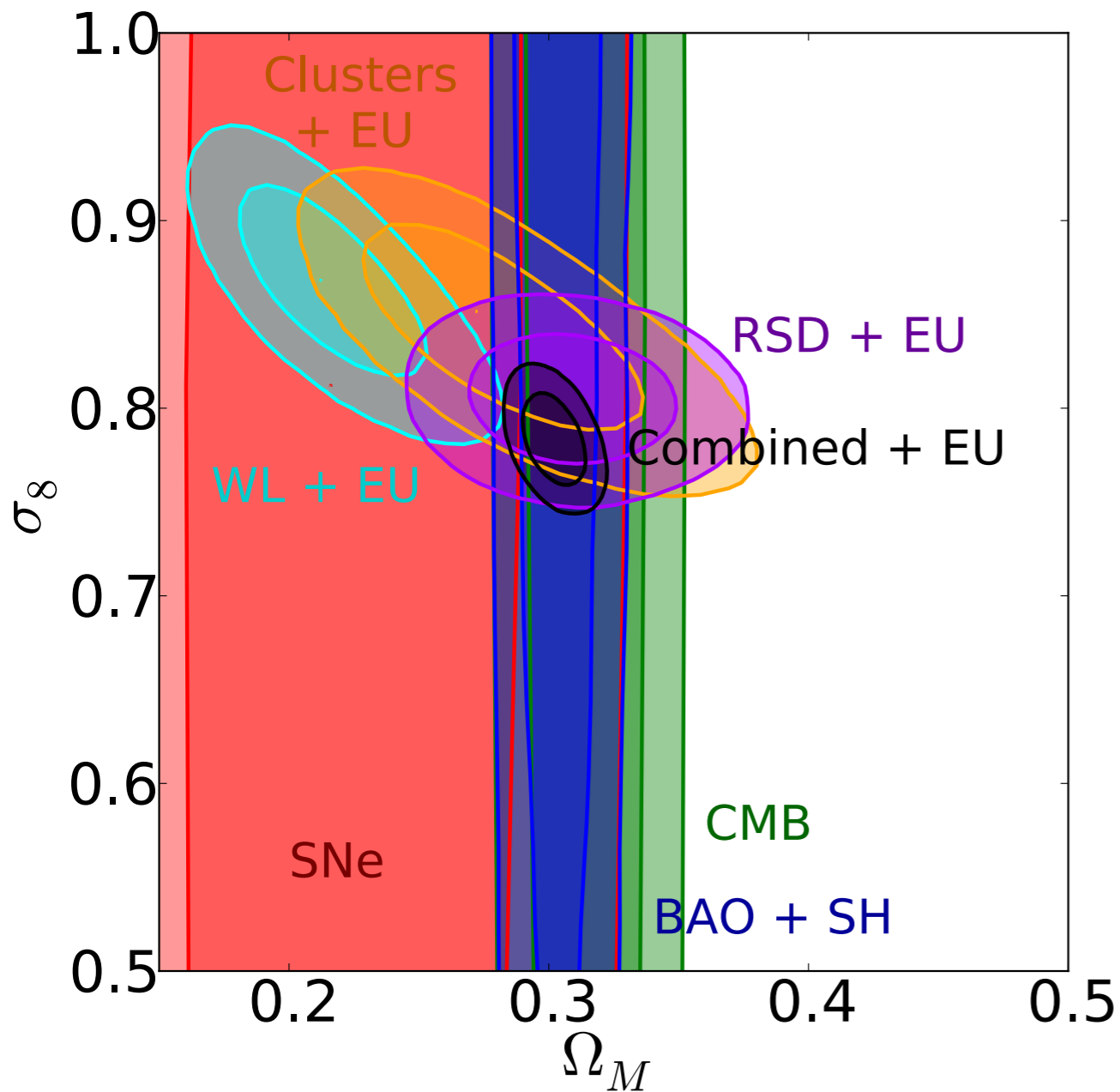
Weak Lensing (CFHTLenS)

BAO (6dF, SDSS LRG, BOSS CMASS)

Sensitivity to geometry and growth

Cosmological Probe	Geometry	Growth
SN Ia	$H_0 D_L(z)$	—
BAO	$\left(\frac{D_A^2(z)}{H(z)}\right)^{1/3} / r_s(z_d)$	—
CMB peak loc.	$R \propto \sqrt{\Omega_m H_0^2} D_A(z_*)$	—
Cluster counts	$\frac{dV}{dz}$	$\frac{dn}{dM}$
Weak lens 2pt	$\frac{r^2(z)}{H(z)} W_i(z) W_j(z)$	$P \left(k = \frac{\ell}{r(z)} \right)$
RSD	$F(z) \propto D_A(z) H(z)$	$f(z) \sigma_8(z)$

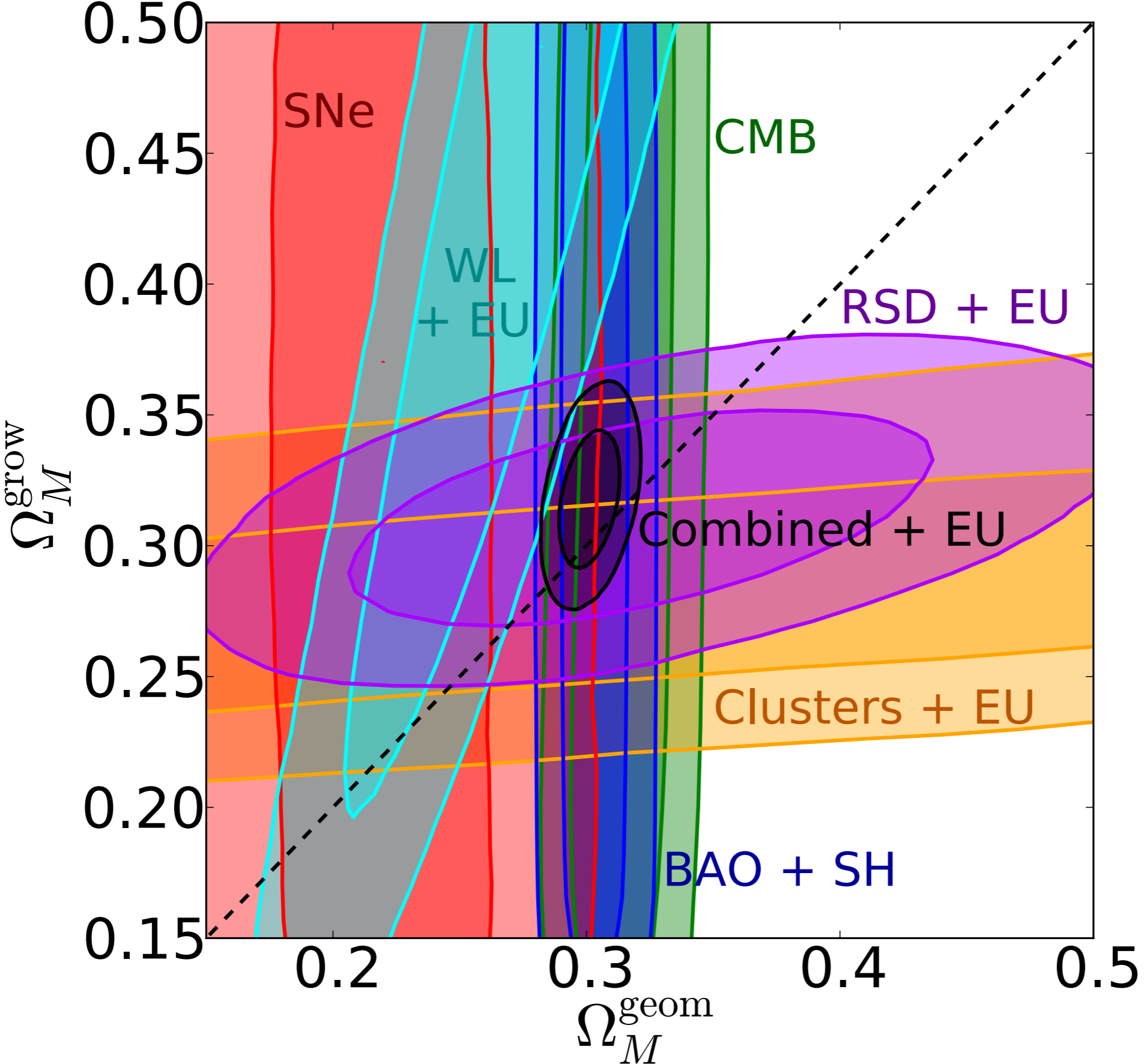
Standard parameter spaces



EU = Early Universe prior from Planck ($\Omega_{\text{M}}h^2$, $\Omega_{\text{B}}h^2$, n_s , A)

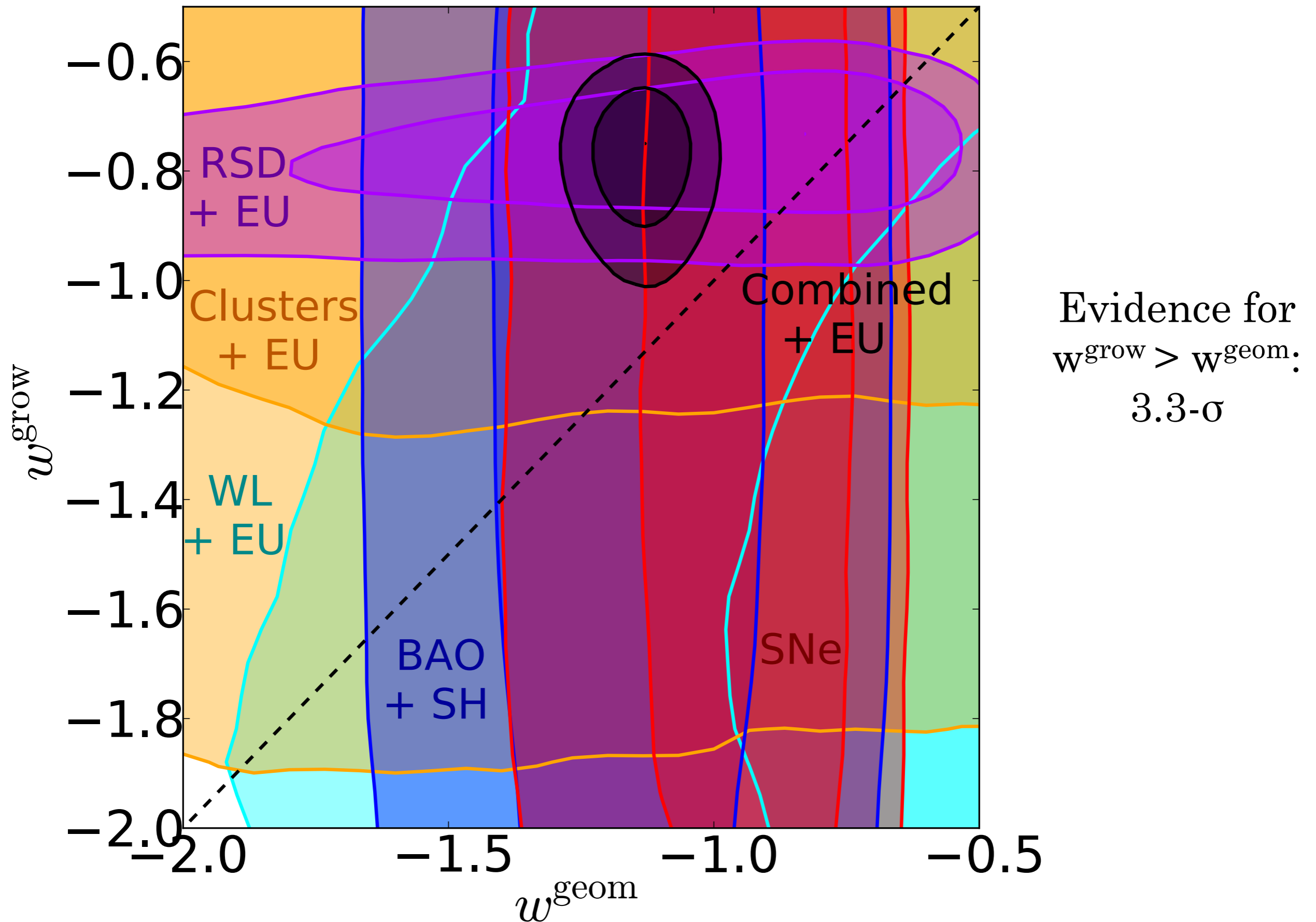
SH = Sound Horizon prior from Planck ($\Omega_{\text{M}}h^2$, $\Omega_{\text{B}}h^2$)

Omega matter: geometry vs. growth

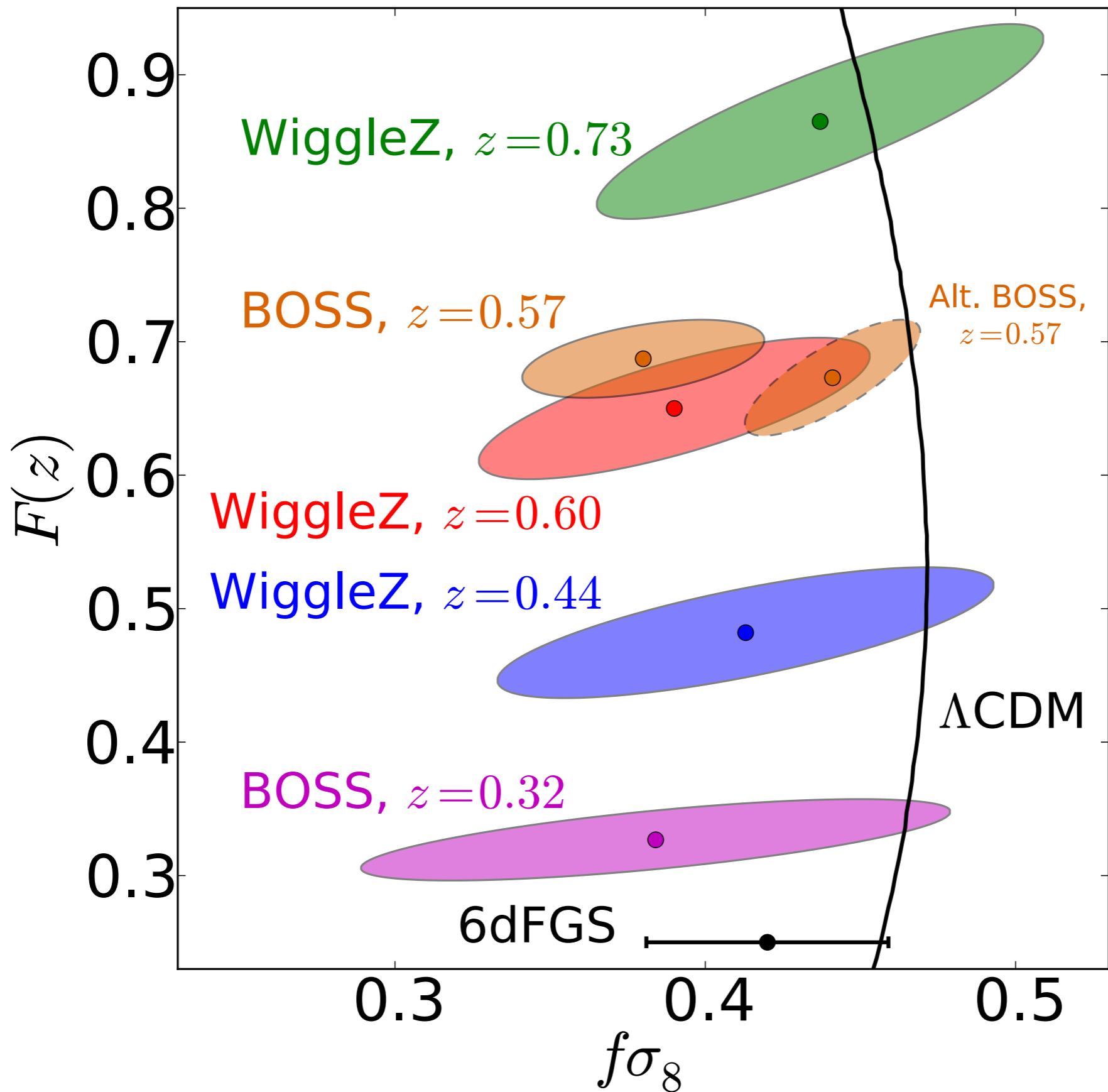


* SN not the recalibrated JLA compilation - need to update; will move Ω_M^{grow} up

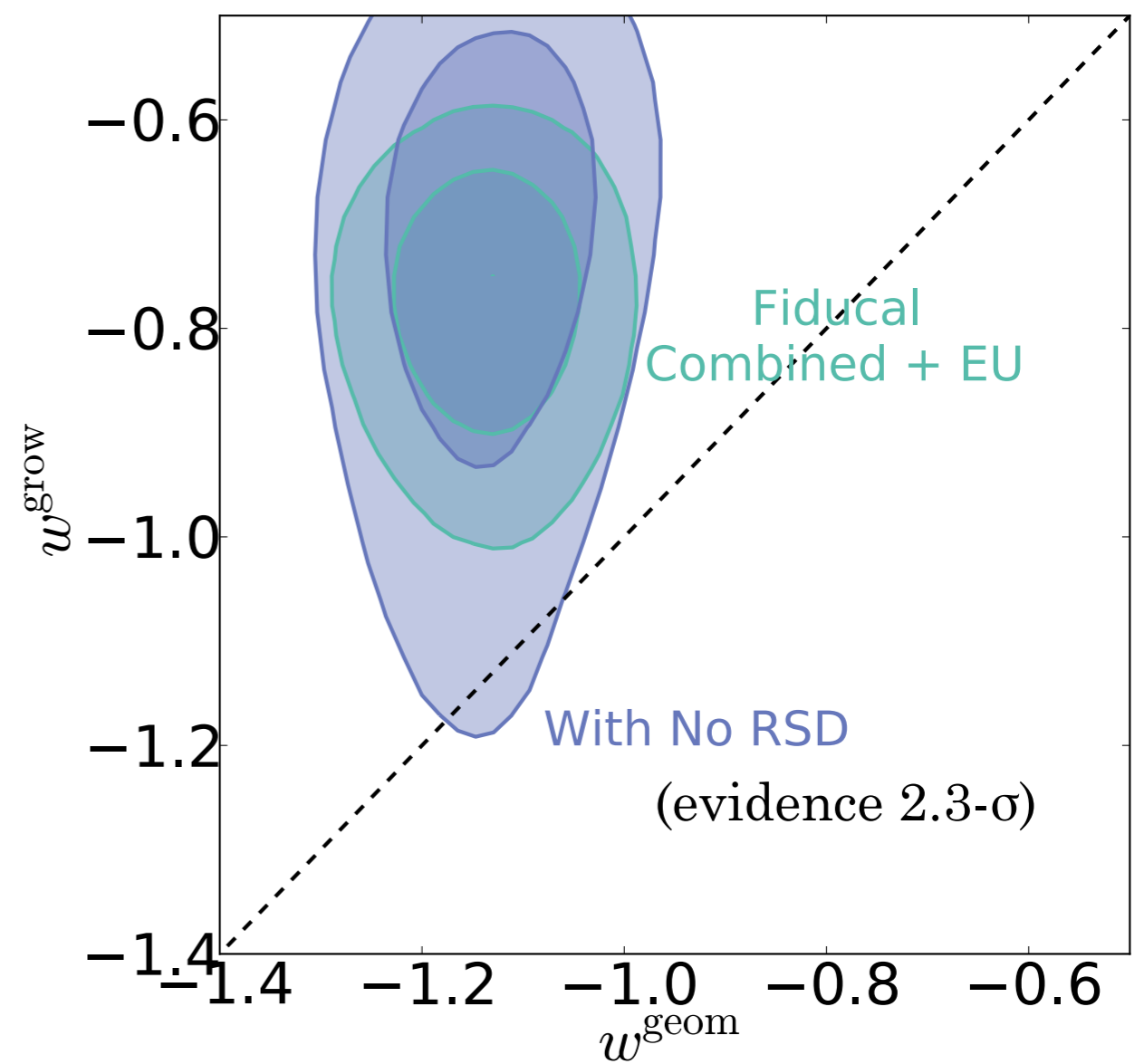
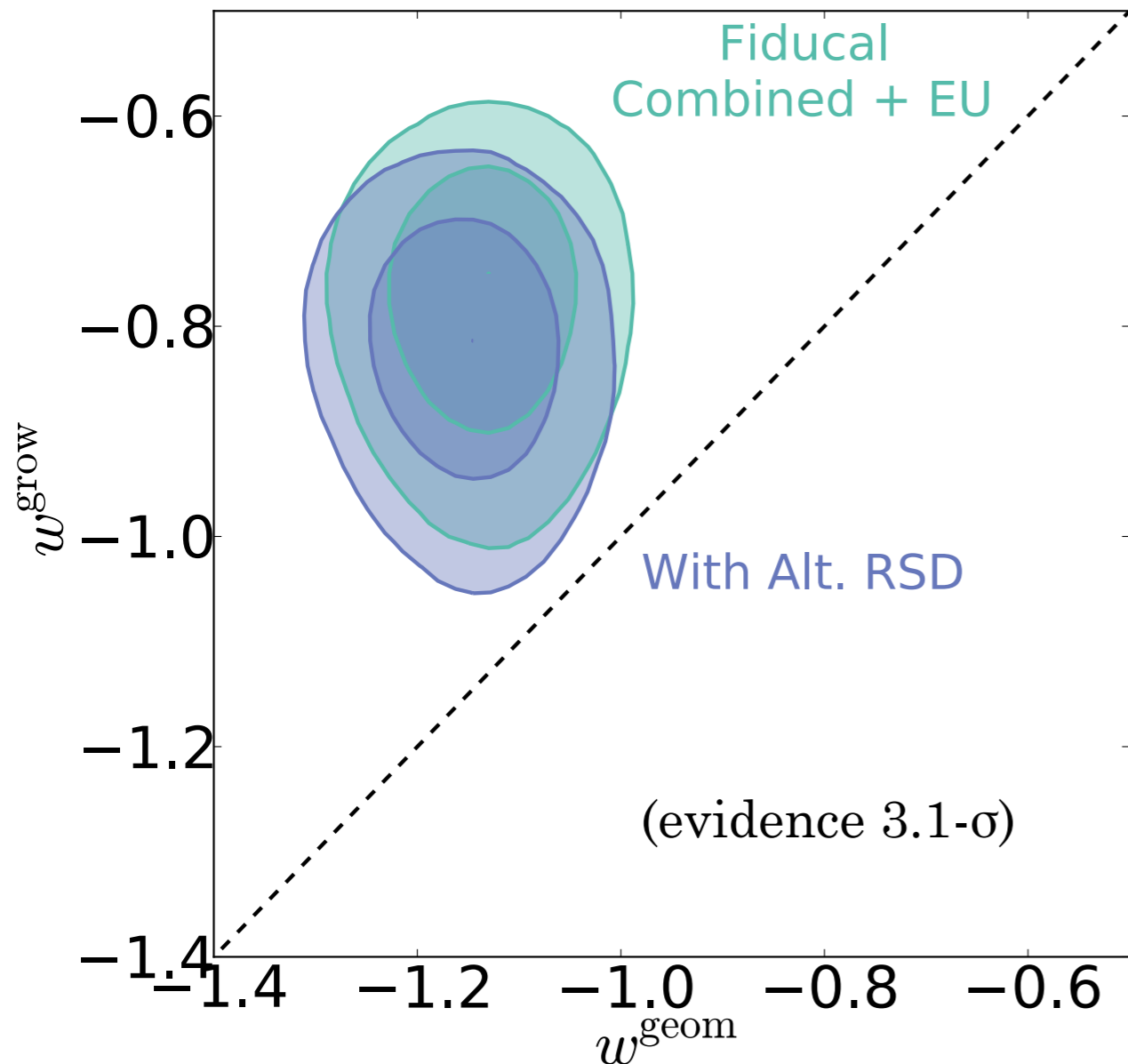
w (eq of state of DE): geometry vs. growth



Redshift Space Distortion data



RSD prefer $w^{\text{grow}} > -1$ (slower growth than in LCDM)

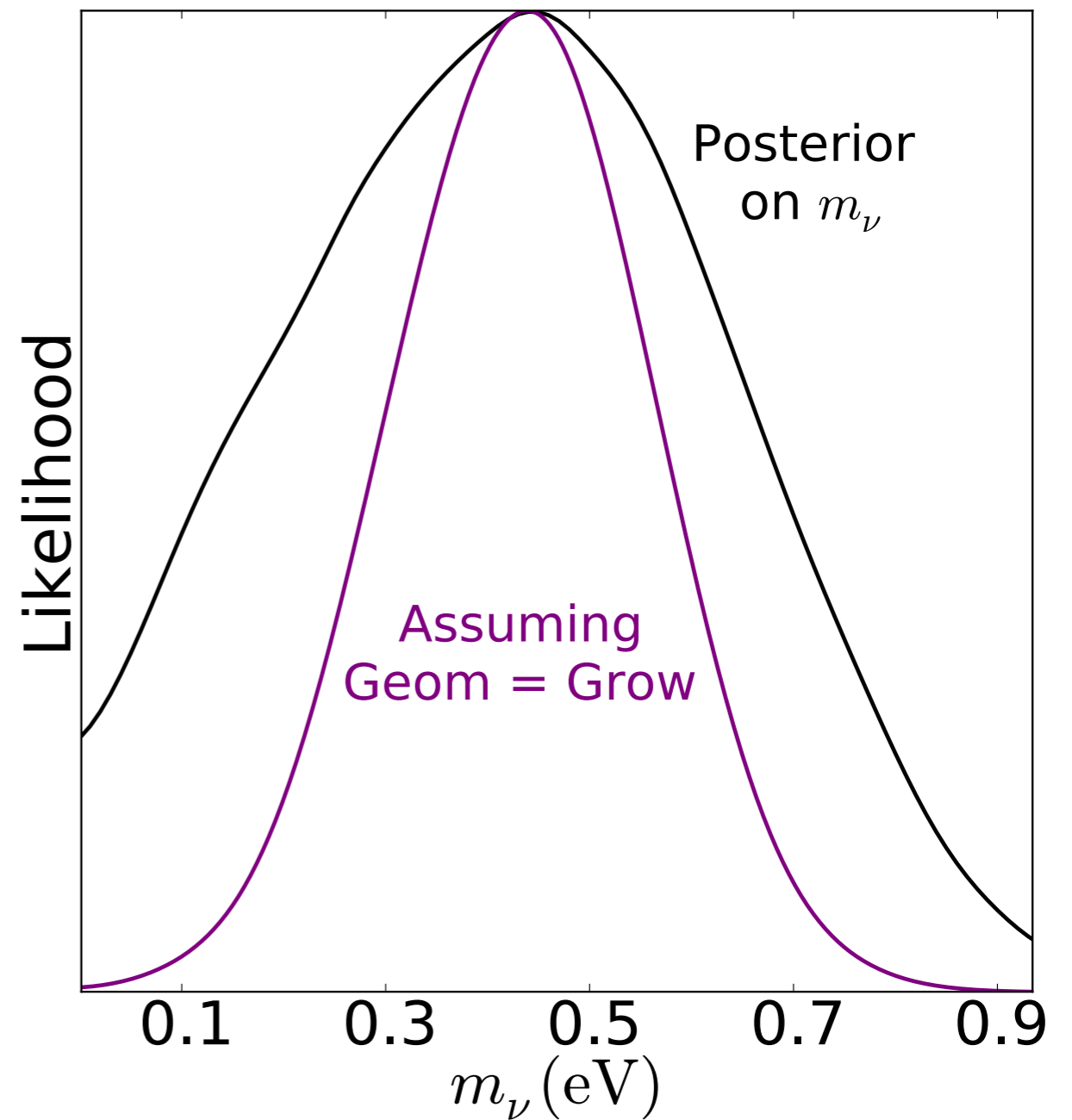
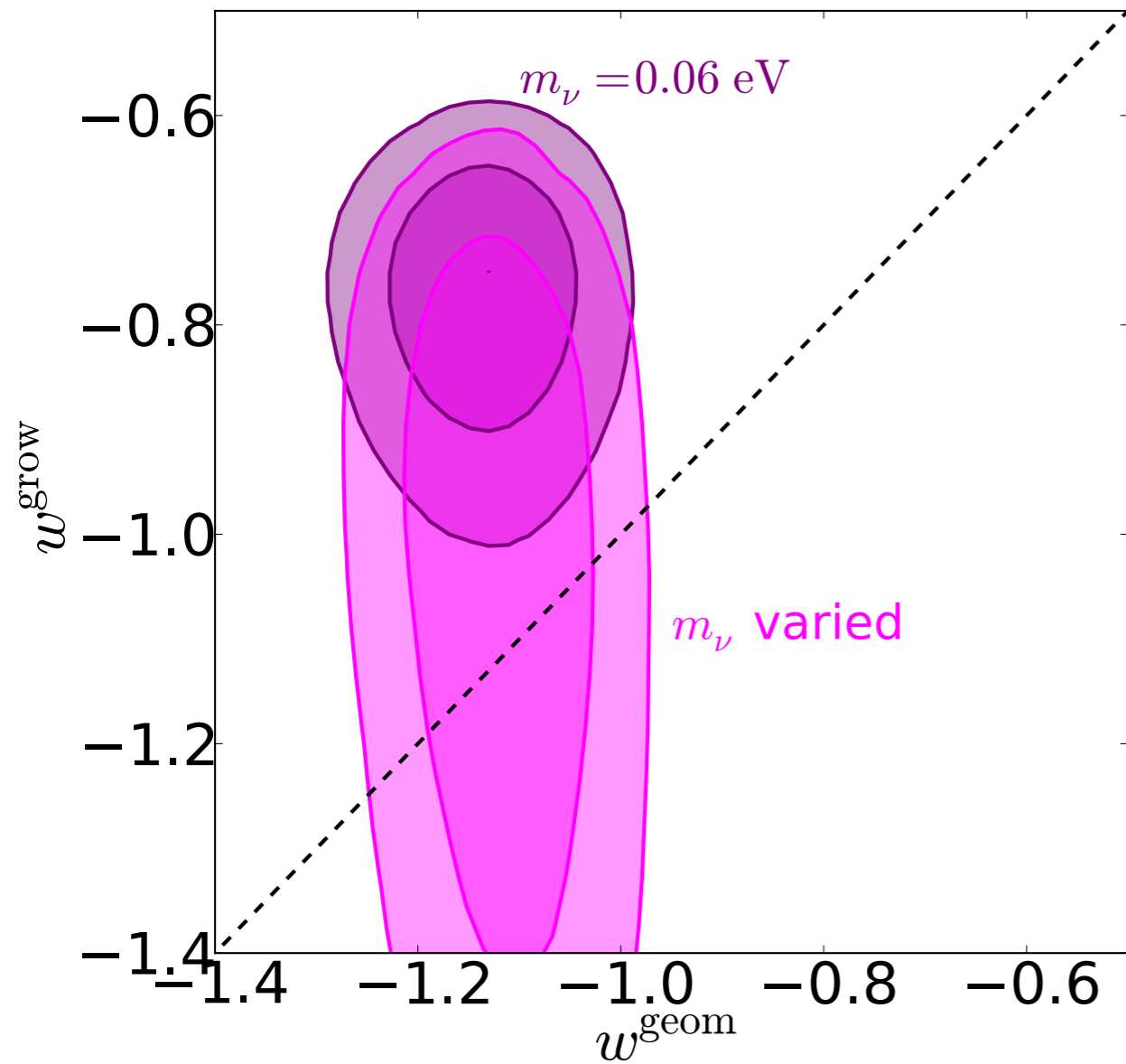


All growth probes (i.e. also clusters, WL) show
“Are there cracks in the Cosmic Egg?”

see also e.g. [M. Costanzi et al, arXiv:1407.8338](#),

[S. Bocquet et al, arXiv:1407.2942](#),
Michael Turner, Aspen, summer 2014

(Pretty high) neutrino mass can relieve the tension



Remainder of talk

Part I: testing DE with geometry and growth

Part II: making predictions for DE observables

Falsifying DE Paradigms

Underlying Philosophy:

- For any given class of DE models, current data **predict** the possible range in fundamental cosmological functions $D(z)$, $H(z)$, $G(z)$, etc ...
- ... which therefore provide **'target' quantities (in redshift)** for ruling out classes of DE models with upcoming data

Methodology

1. Start with the parameter set:

$$\Omega_M, \Omega_K, H_0, w(z), w_\infty$$

2. Use either the current data or future data

$$\begin{aligned} \text{(current} &= \text{Union2 SN} + \text{WMAP} + \text{BAO}_{z=0.35} + H_0 \\ \text{future} &= \text{Planck} + \text{Space DE)} \end{aligned}$$

3. Employ the likelihood machine

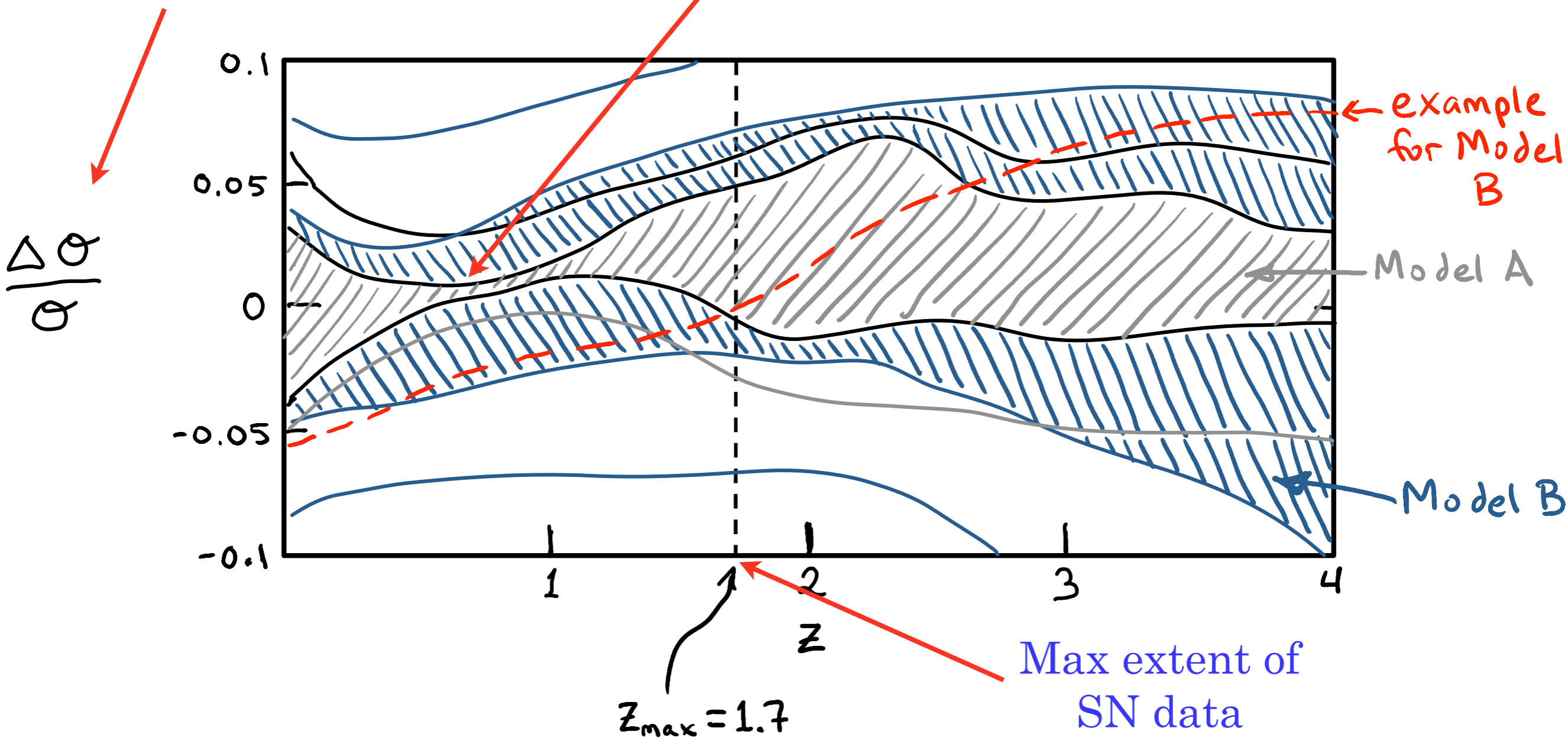
Markov Chain Monte Carlo likelihood calculation,
between ~ 2 and ~ 15 parameters constrained

4. Compute predictions for $D(z)$, $G(z)$, $H(z)$ (and $\gamma(z)$, $f(z)$)

Structure of graphs to follow

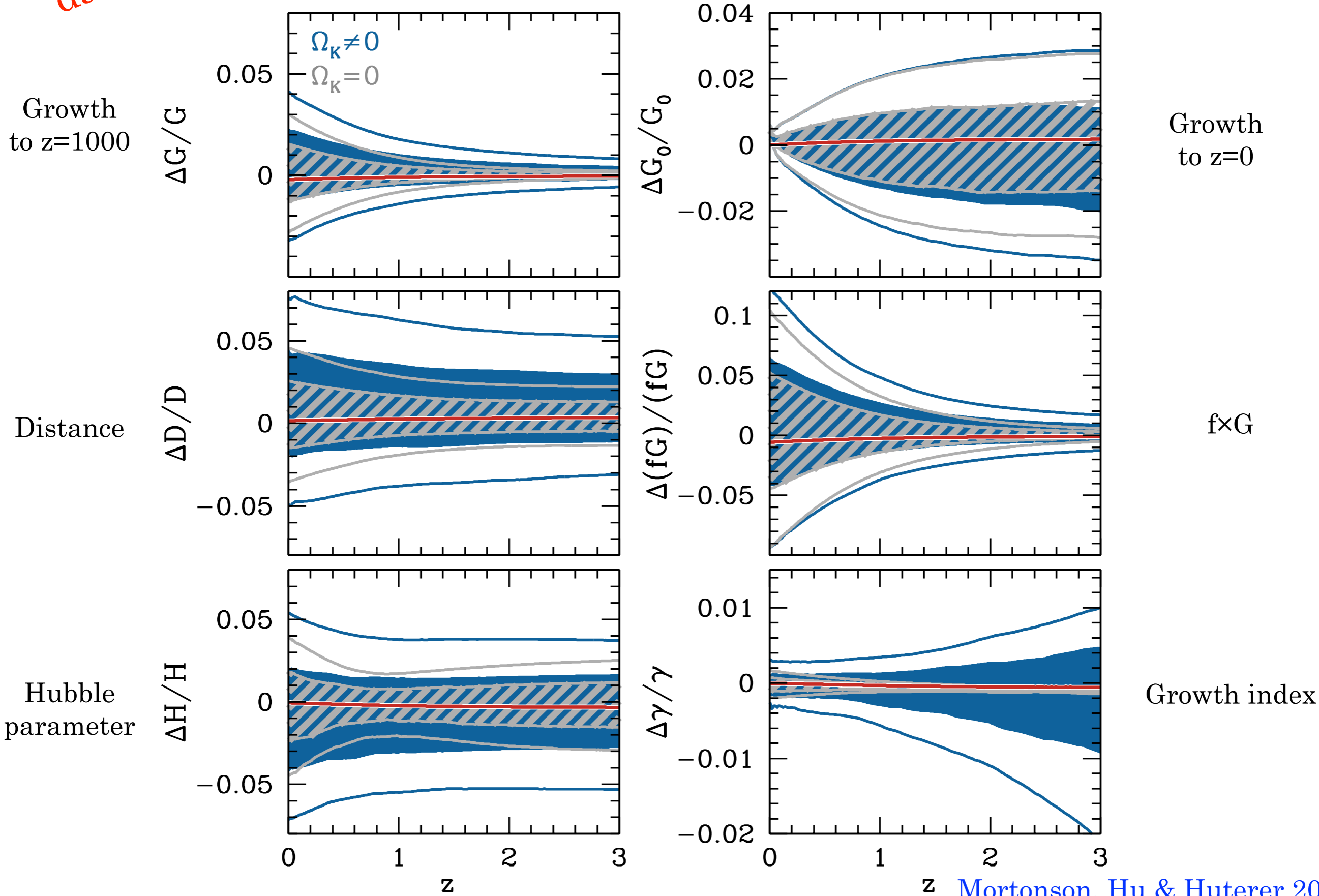
Prediction on observable
by SN+CMB

Pivot



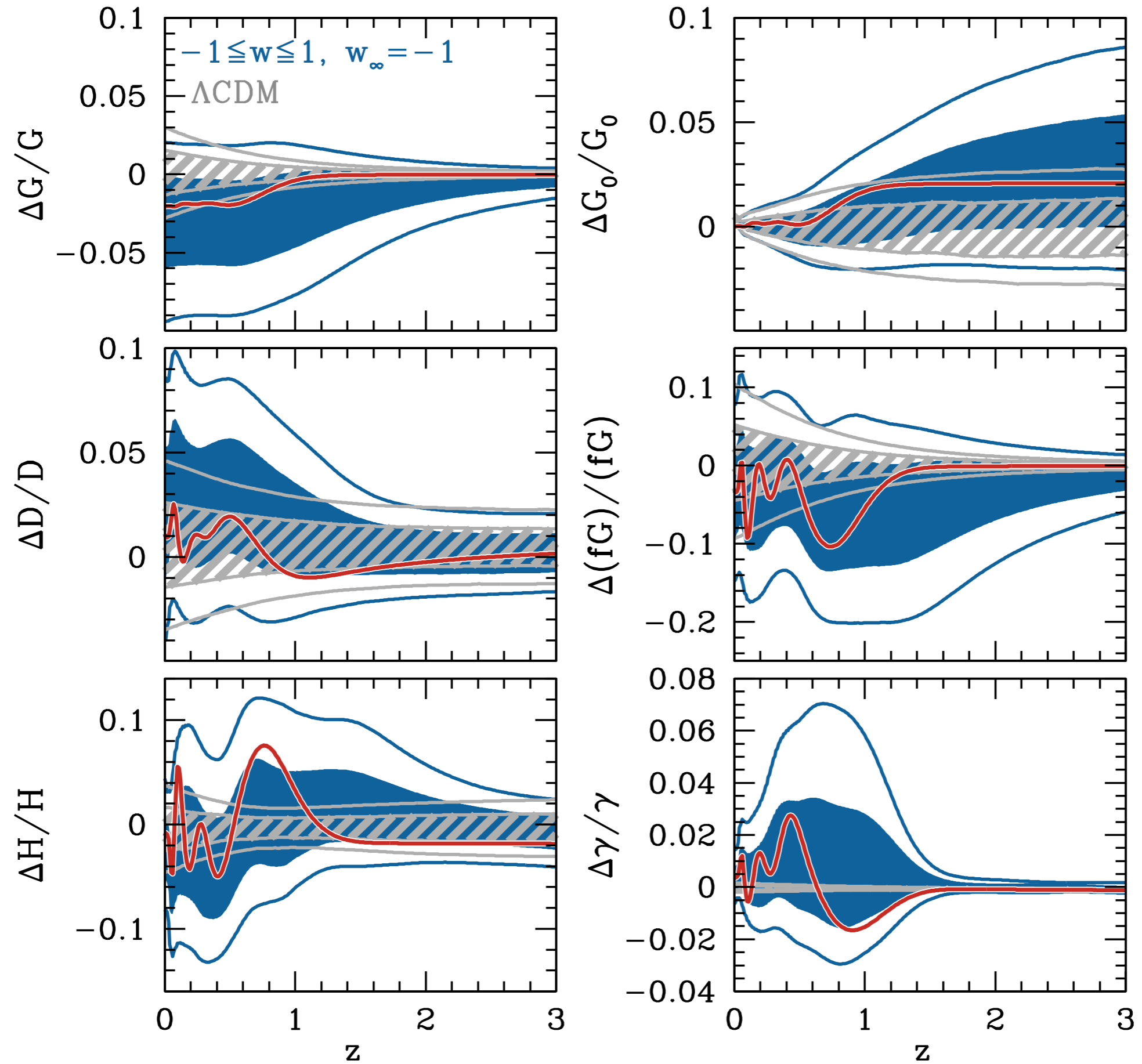
Current data

ΛCDM predictions - flat or curved



Current data

Quintessence predictions (flat, no Early DE)

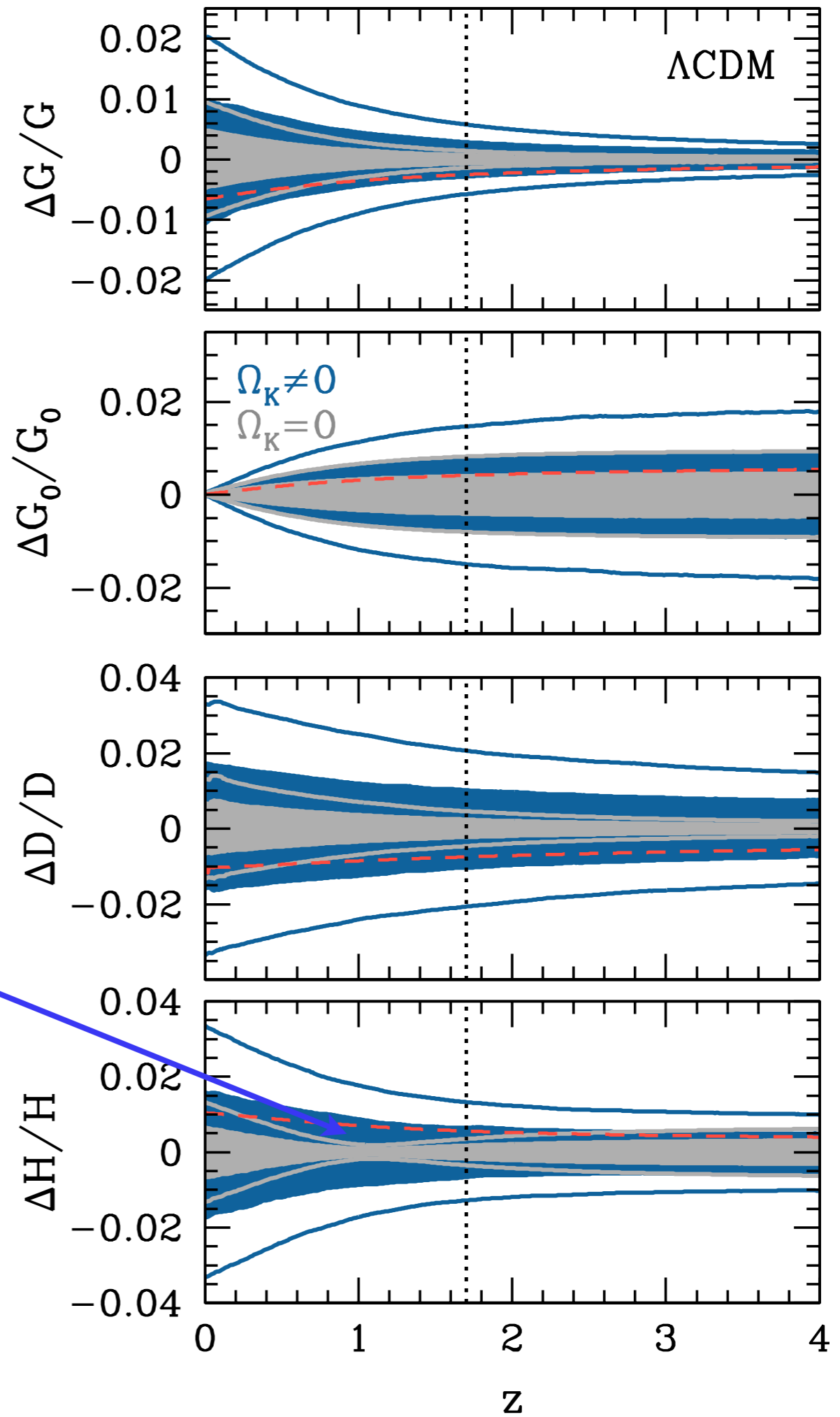


Future data

ΛCDM predictions (flat or curved)

Grey: flat
Blue: curved

D, G to <1% everywhere
H(z=1) to 0.1% for flat ΛCDM

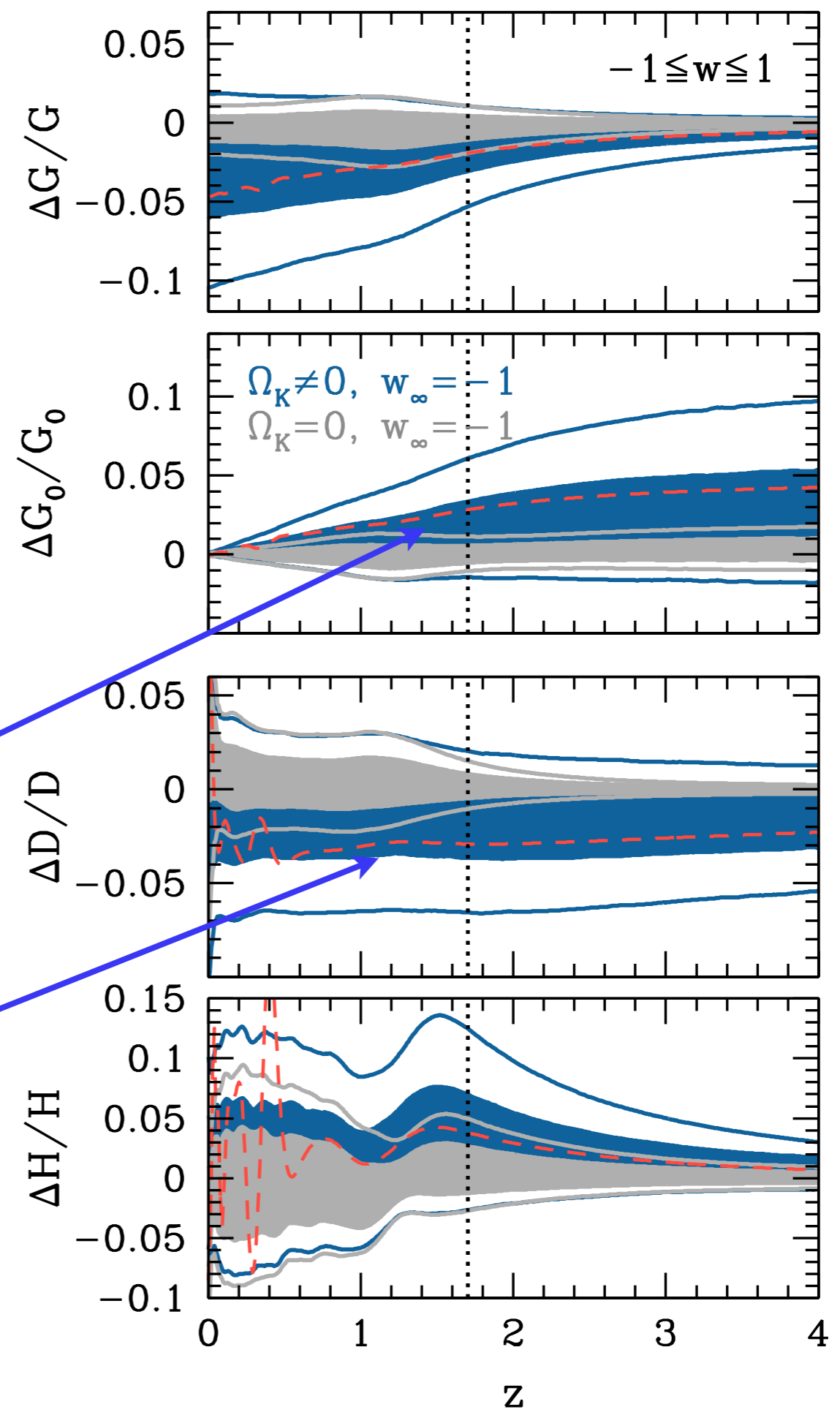


Future data

Quintessence predictions

Grey: flat
Blue: curved

Smoking Gun of curvature:
1. Shift in G_0
2. Negative const offset in D



Therefore:

Whole classes of DE models
are highly falsifiable

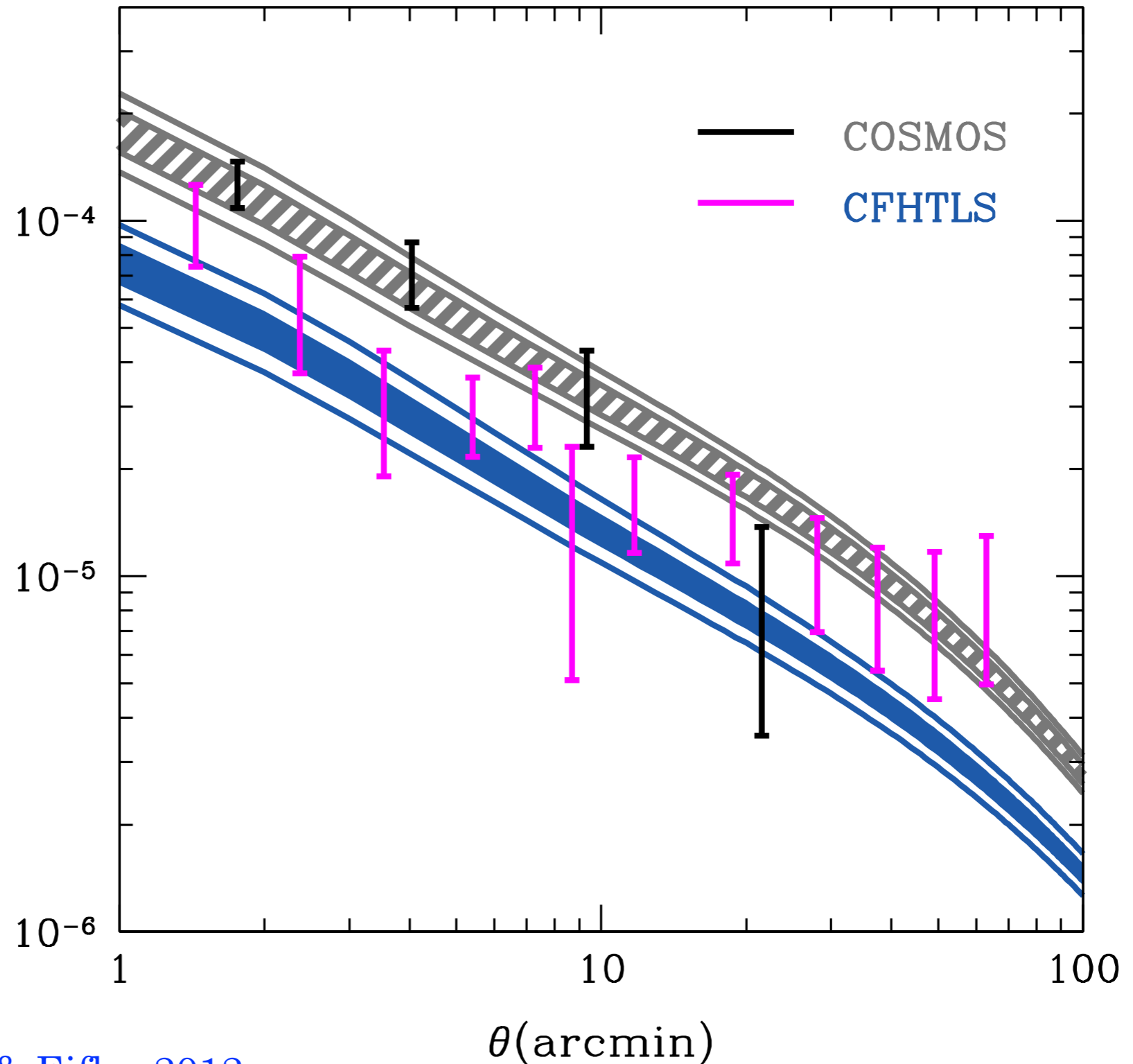
Therefore:

Whole classes of DE models
are highly falsifiable

Straightforward to make predictions for **actually observable quantities** for a given survey, given the class of DE models

Two-pt function
of shear
in real space

ξ^+



Dark Energy Survey Instrument (DESI)



- Huge spectroscopic survey on Mayall telescope (Arizona)
- ~5000 fibres, ~15,000 sqdeg, ~20 million spectra
- LRG in $0 < z < 1$, ELG in $0 < z < 1.5$, QSO $2.2 < z < 3.5$
- Great for **dark energy** (RSD, BAO)
- Great for primordial non-Gaussianity - $P(k, z)$, bispectrum...
- Start ~2018, funding DOE + institutions

Conclusions

▶ So far, all measurements are in excellent agreement with Lambda (i.e. $w = -1$)...

▶ ...despite occasional alarms to the contrary:

▶ Planck + BAO + SN + high H_0^{local}

▶ Separating growth from geometry is a good way to get
a) constraints b) insights into DE constraints; it now
indicates a 3-sigma growth \neq geometry discrepancy

▶ We now have accurate, tight predictions for $D(z)$, $G(z)$,
 $H(z)$ and the observable quantities for each class of DE
models \Rightarrow way to rule them out.

EXTRA SLIDES

To shed light on dark energy: search for ‘something else’ in the data

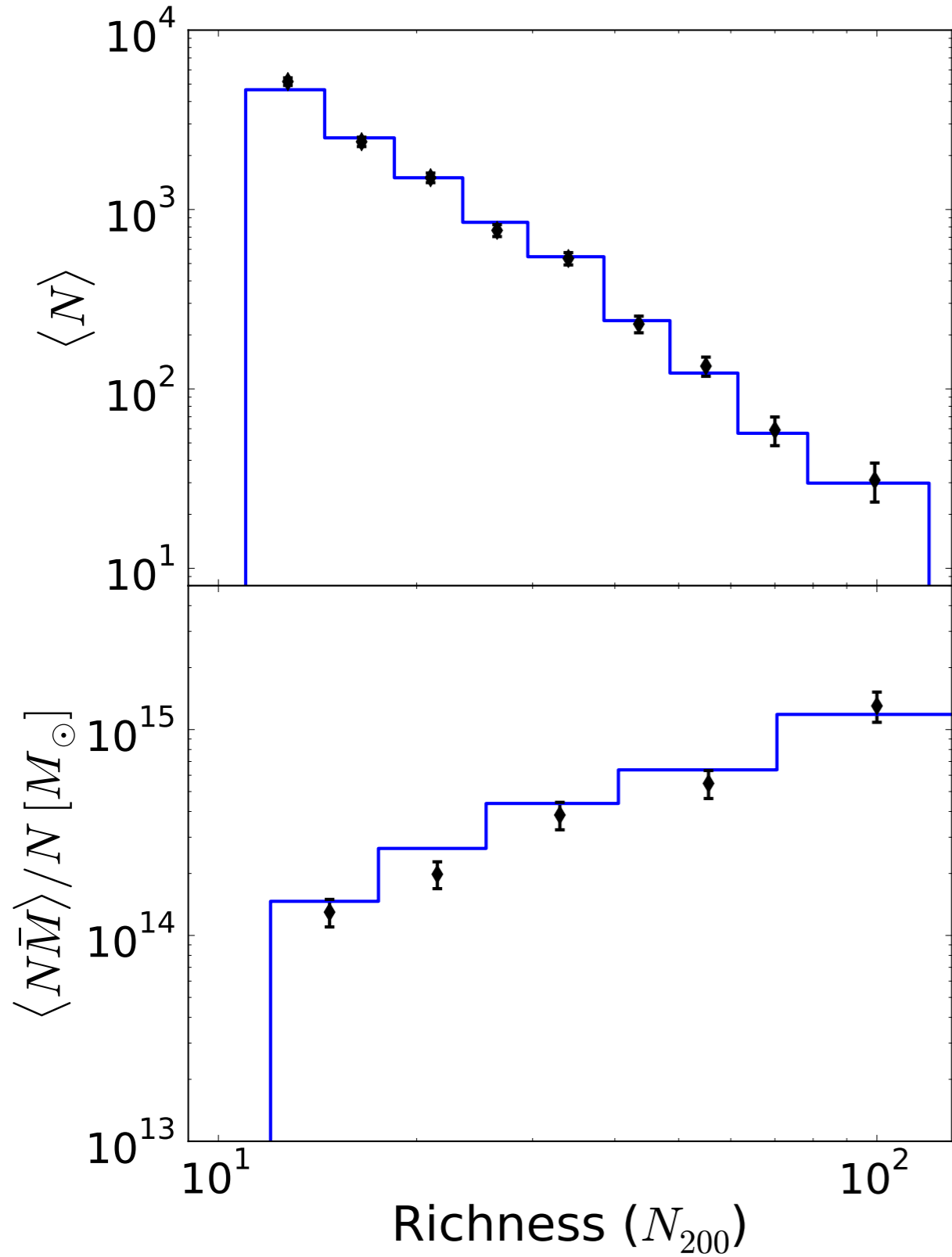
- Variation of eq. of state w → (none yet)
- Clustering of DE → (super hard)
- DM-DE interactions → (none yet)
- Early dark energy → (none yet)
- Modified gravity (MG) → (none yet)

BAO data

Survey	z_{eff}	Parameter	Measurement
6dFGS [33]	0.106	r_s/D_V	0.336 ± 0.015
SDSS LRG [34]	0.35	D_V/r_s	8.88 ± 0.17
BOSS CMASS [35]	0.57	D_V/r_s	13.67 ± 0.22

TABLE III. BAO data measurements used here, together with the effective redshift for the corresponding galaxy sample.

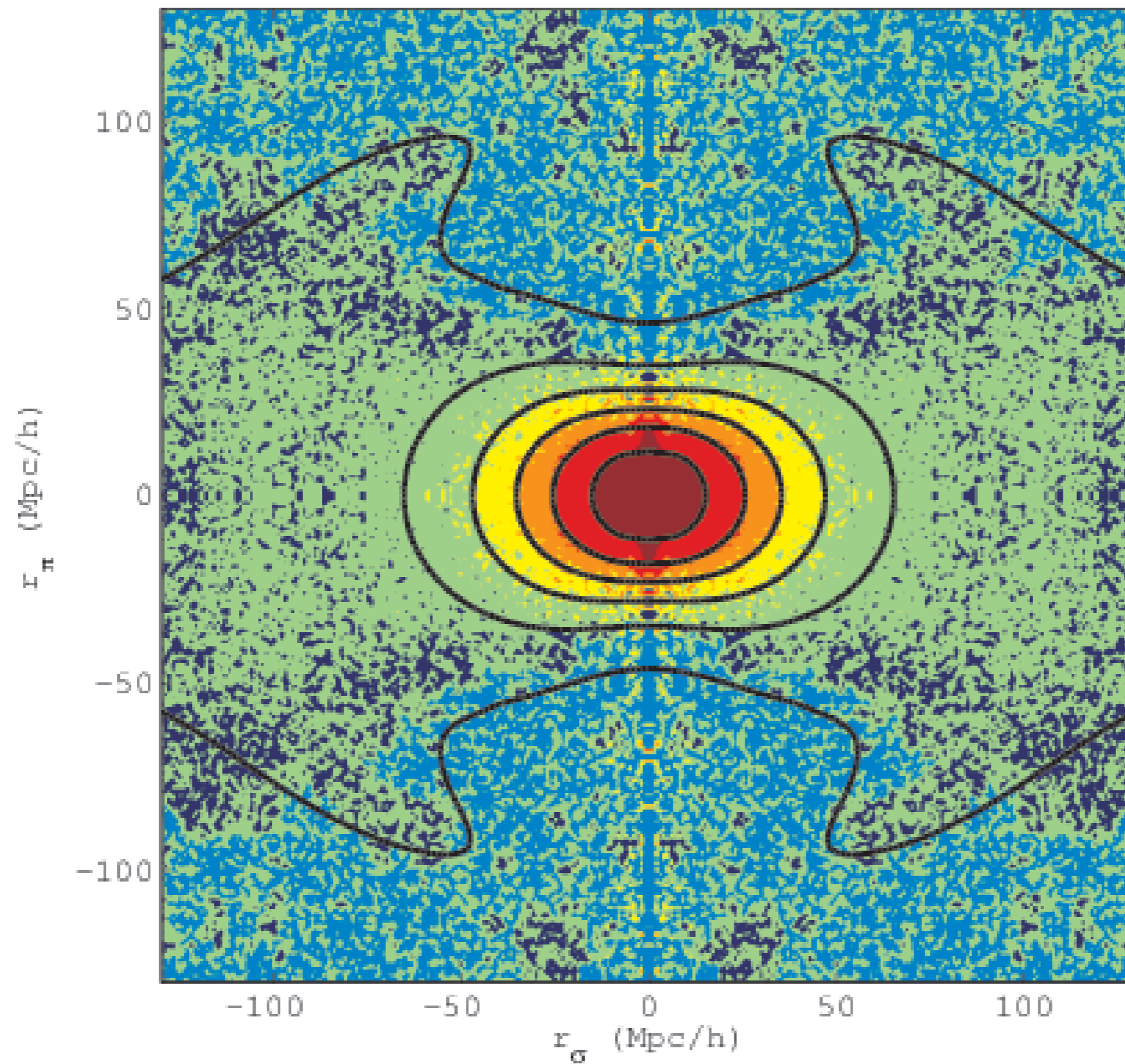
Cluster data



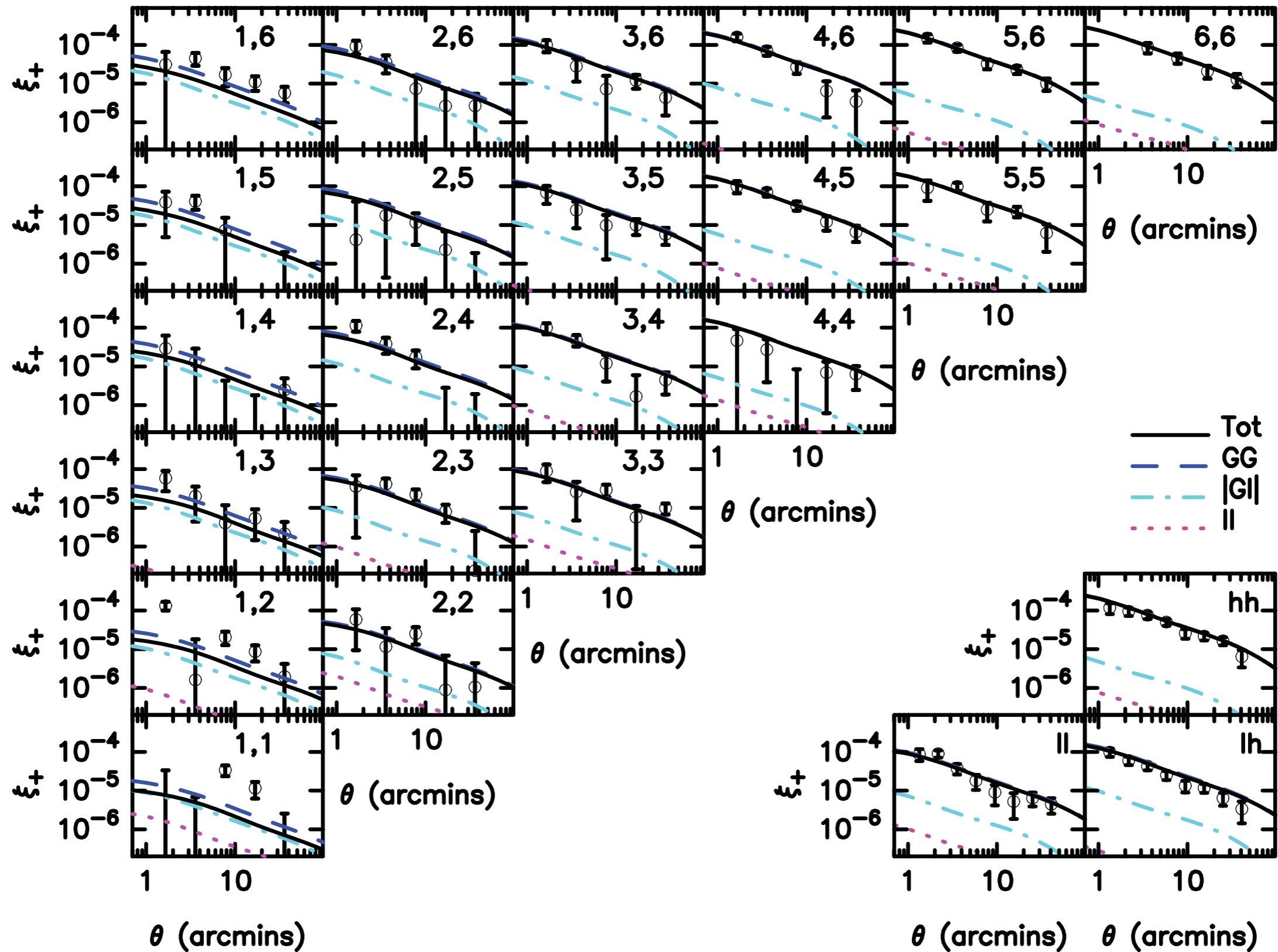
Richness bin	No. of Clusters	$\langle M_{200b} \rangle [10^{14} M_{\odot}]$
12-17	5651	1.298
18-25	2269	1.983
26-40	1021	3.846
41-70	353	5.475
71+	55	13.03

TABLE IX. Mean mass (and their number) of clusters with a richness within the given bin.

RSD (BOSS paper)



Measured 2-pt correlation func from CFHTLenS

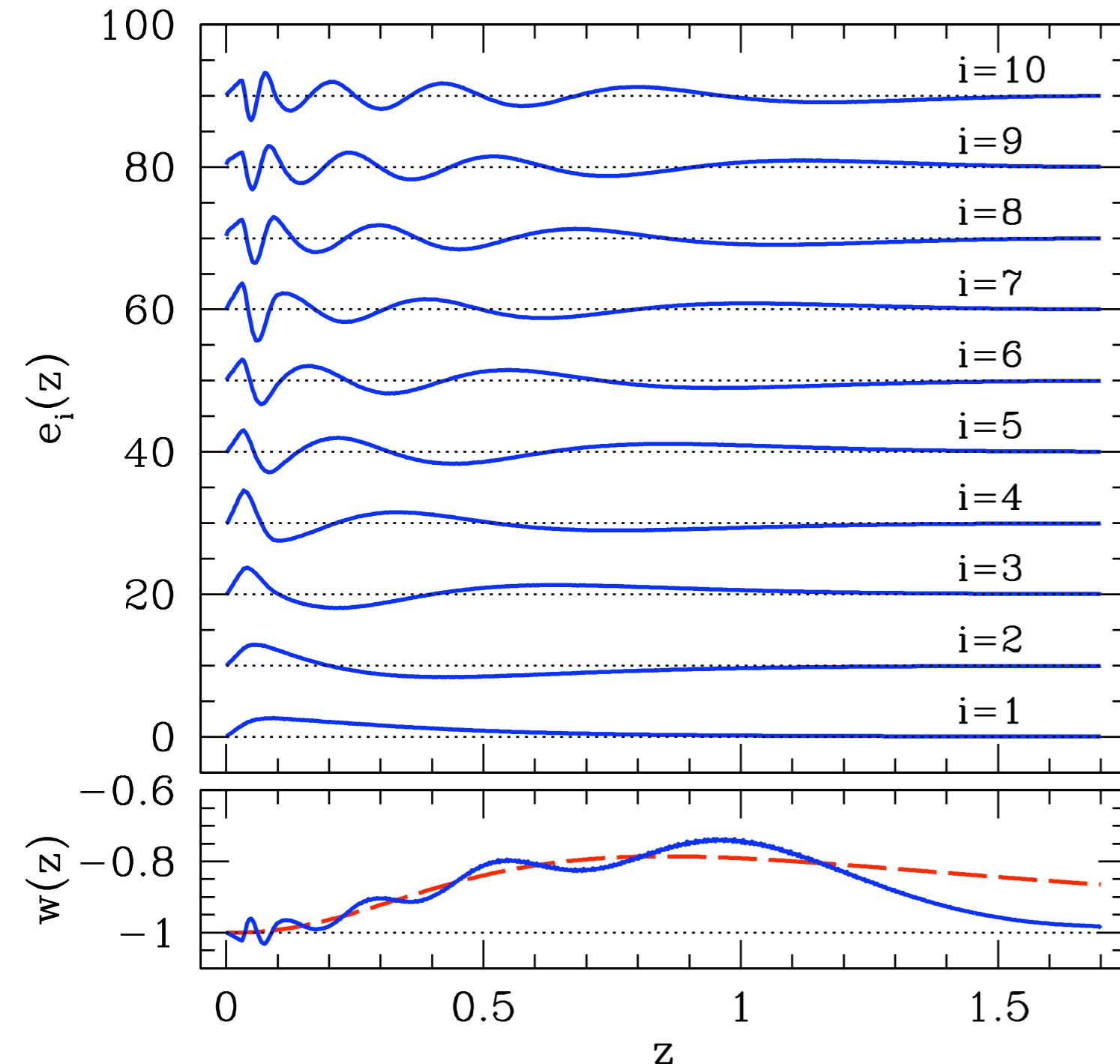


Parameter	Unsplit, $w = -1$	Unsplit, w free	Split, $w = -1$	Split, w free
Ω_M $\left\{ \begin{array}{l} \Omega_M^{\text{geom}} \\ \Omega_M^{\text{grow}} \end{array} \right.$	0.303 ± 0.008	0.299 ± 0.010	0.302 ± 0.008	0.283 ± 0.011
$\Omega_M h^2$	0.140 ± 0.001	0.141 ± 0.002	0.140 ± 0.001	0.142 ± 0.002
$\Omega_b h^2$	0.0221 ± 0.0002	0.0220 ± 0.0003	0.0221 ± 0.0002	0.0221 ± 0.0003
w $\left\{ \begin{array}{l} w^{\text{geom}} \\ w^{\text{grow}} \end{array} \right.$	—	-1.03 ± 0.05	—	-1.13 ± 0.06
$10^9 A$	1.95 ± 0.09	1.91 ± 0.10	1.96 ± 0.09	2.17 ± 0.13
n_s	0.961 ± 0.005	0.959 ± 0.006	0.962 ± 0.005	0.961 ± 0.006
σ_8	0.786 ± 0.015	0.788 ± 0.016	0.782 ± 0.016	0.771 ± 0.017
h	0.680 ± 0.006	0.687 ± 0.012	0.661 ± 0.017	0.677 ± 0.018
α_s	1.44 ± 0.11	1.44 ± 0.11	1.44 ± 0.11	1.44 ± 0.11
β_c	3.26 ± 0.11	3.26 ± 0.11	3.26 ± 0.11	3.27 ± 0.11
$\ln(N M_1)$	2.36 ± 0.06	2.37 ± 0.06	2.29 ± 0.08	2.33 ± 0.08
$\ln(N M_2)$	4.15 ± 0.09	4.16 ± 0.09	4.09 ± 0.11	4.15 ± 0.11
σ_{NM}	0.359 ± 0.057	0.357 ± 0.057	0.378 ± 0.059	0.367 ± 0.060
β	1.041 ± 0.050	1.045 ± 0.051	1.018 ± 0.054	1.036 ± 0.055
σ_{MN}	0.462 ± 0.081	0.459 ± 0.082	0.486 ± 0.085	0.464 ± 0.084

Modeling DE

Modeling of low- z $w(z)$:
Principal Components

$$w(z_j) = -1 + \sum_{i=1}^N \alpha_i e_i(z_j)$$



500 bins (so 500 PCs)
 $0.03 < z < 1.7$

We use first ~ 10 PCs;
(results converge $10 \rightarrow 15$)

Fit of a **quintessence**
model with **PCs**

Cosmological Functions

Expansion Rate (BAO):

$$H(z) = H_0 \left[\Omega_{\text{M}}(1+z)^3 + \Omega_{\text{DE}} \frac{\rho_{\text{DE}}(z)}{\rho_{\text{DE}}(0)} + \Omega_{\text{K}}(1+z)^2 \right]^{1/2}$$

Distance (SN, BAO, CMB):

$$D(z) = \frac{1}{(|\Omega_{\text{K}}|H_0^2)^{1/2}} S_{\text{K}} \left[(|\Omega_{\text{K}}|H_0^2)^{1/2} \int_0^z \frac{dz'}{H(z')} \right]$$

Growth (WL, clusters):

$$G'' + \left(4 + \frac{H'}{H} \right) G' + \left[3 + \frac{H'}{H} - \frac{3}{2} \Omega_{\text{M}}(z) \right] G = 0$$

$$G = D_1/a$$

Methodology

1. Start with the parameter set:

$$\Omega_M, \Omega_K, H_0, w(z), w_\infty \text{ (early DE eq of state)}$$

2. Pre-compute PCs of $w(z)$ based on future data

3. Using either the current data
or future (SNAP+Planck) data...

4. ...employ the likelihood machine...

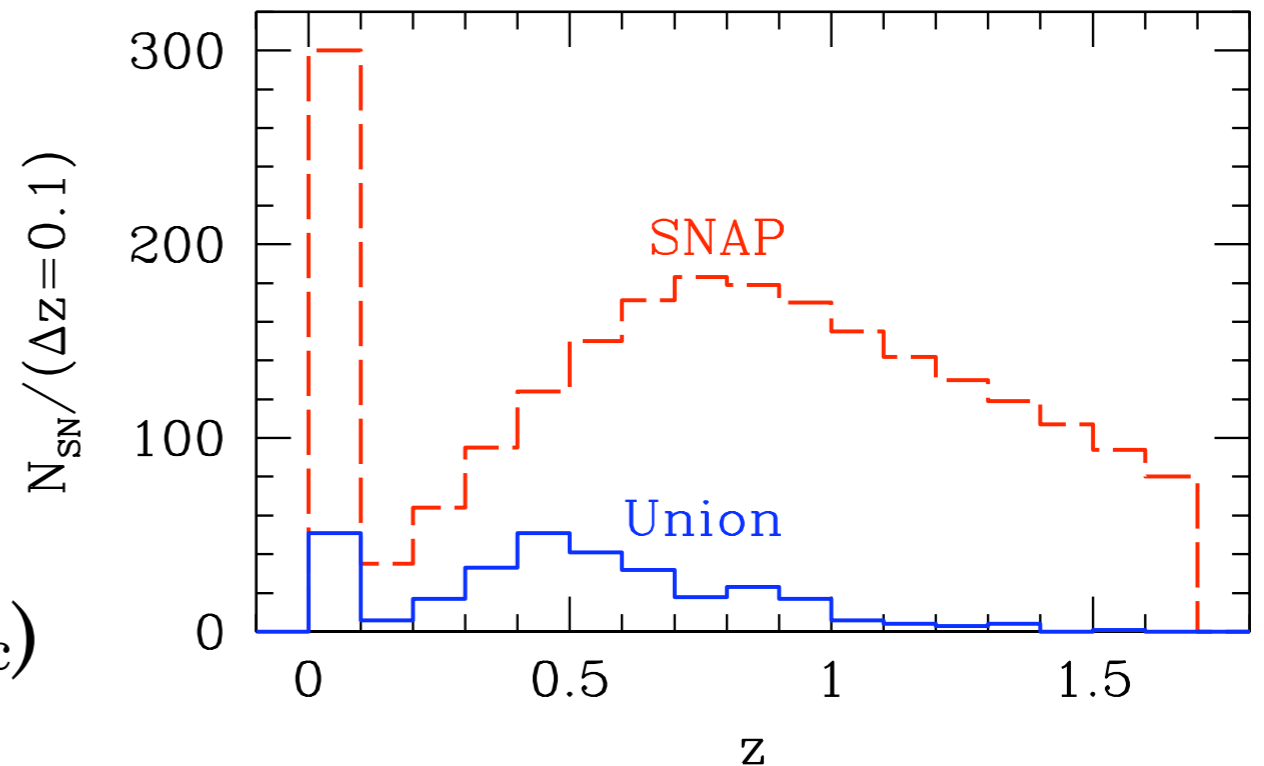
Markov Chain Monte Carlo likelihood calculation,
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5. and compute predictions for $D(z)$, $G(z)$, $H(z)$ etc

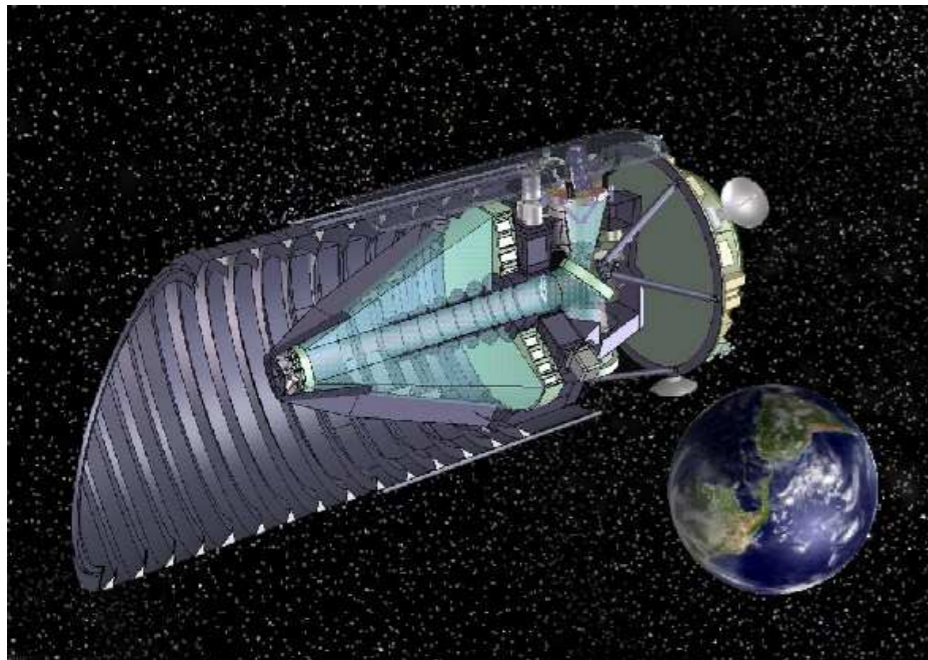
Predictions from **Future** Data

Assumed “data”:

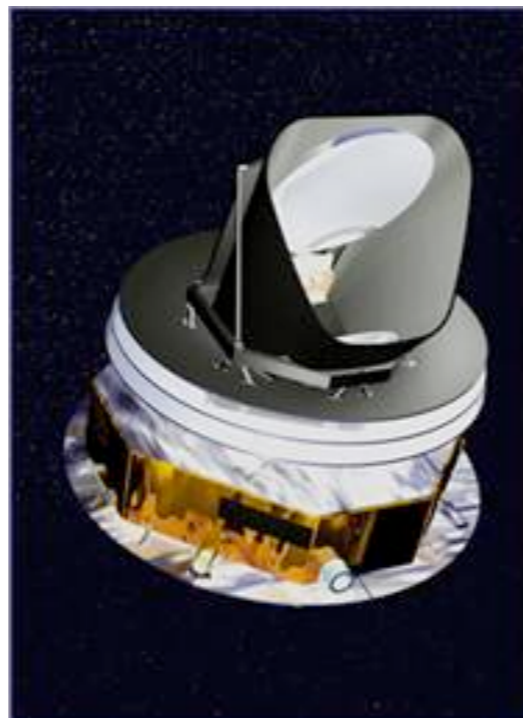
1. SNAP 2000 SNe, $0.1 < z < 1.7$
(plus 300 low- z SNe);
converted into distances
2. Planck info on $\Omega_m h^2$ and $D_A(z_{\text{rec}})$



Dead



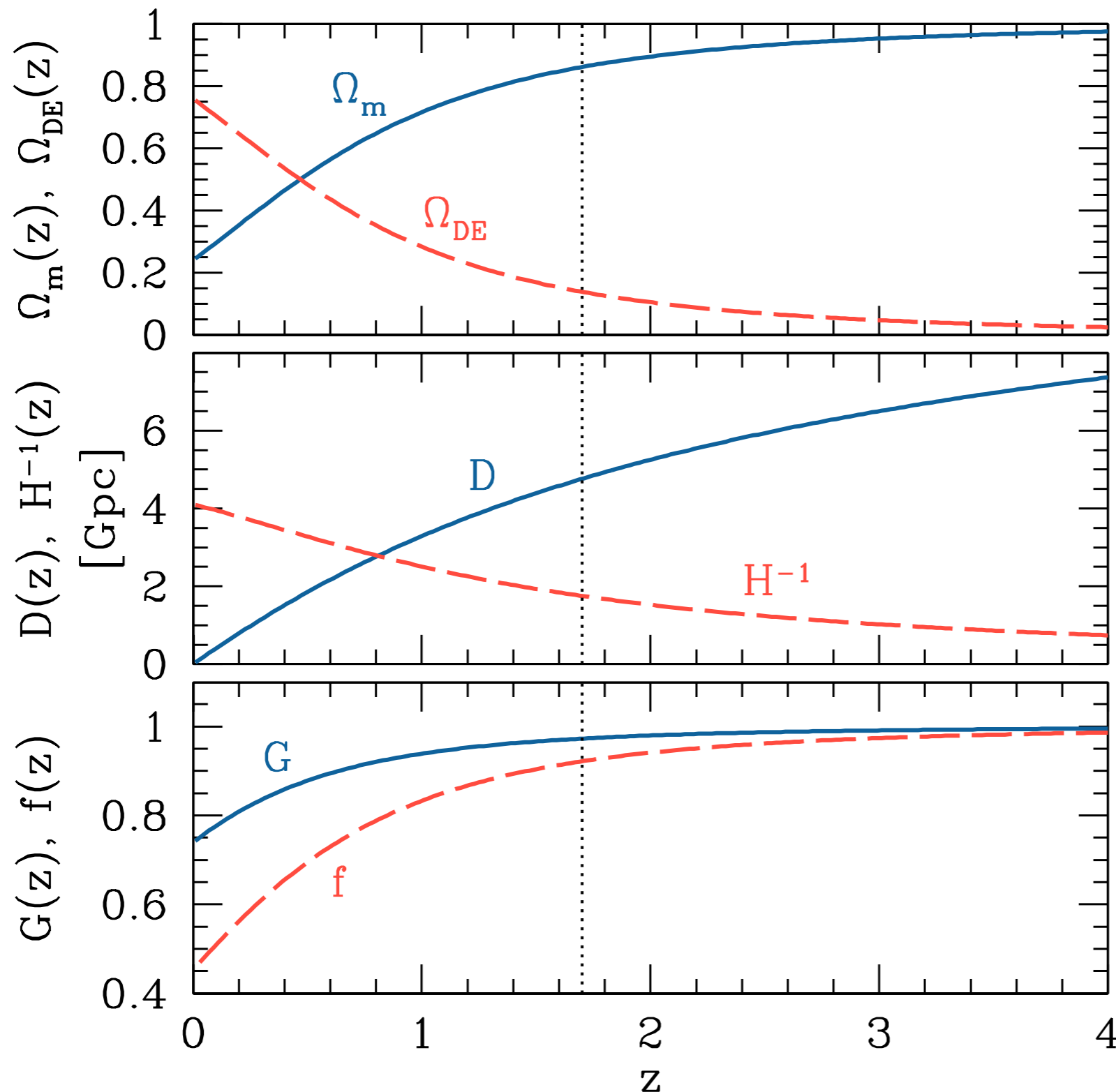
Alive



$$\sigma_{\alpha}^2 = \left(\frac{0.1}{\Delta z_{\text{sub}}} \right) \left[\frac{0.15^2}{N_{\alpha}} + 0.02^2 \left(\frac{1+z}{2.7} \right)^2 \right]$$

Predictions below shown
around:
fiducial model

Cosmological “observable” functions



Matter and DE
energy density
(relative to critical)

D = distance
H = expansion rate

G = growth of density
fluctuations
(ignore f)

Modeling of **Early** DE



$$\rho_{\text{DE}}(z > z_{\text{max}}) = \rho_{\text{DE}}(z_{\text{max}}) \left(\frac{1+z}{1+z_{\text{max}}} \right)^{3(1+w_{\infty})}$$

de Putter & Linder 2008

Modeling of **modified** Gravity



$$G(a) = \exp \left(\int_0^a d \ln a' [\Omega_M^\gamma(a') - 1] \right)$$

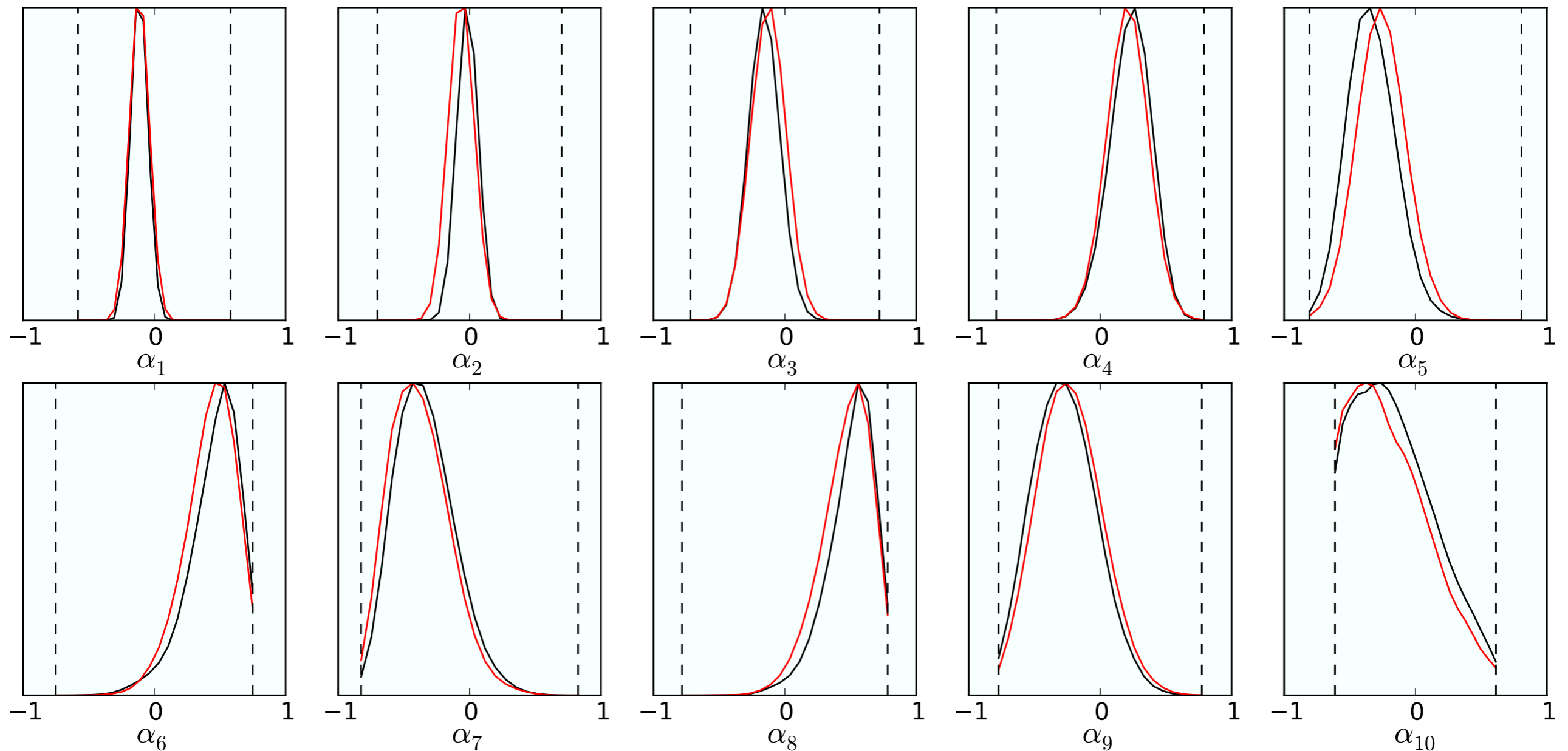
Linder 2005

In *principal*, constraints are good...

(components....)

$$w(z_j) = -1 + \sum_{i=1}^N \alpha_i e_i(z_j)$$

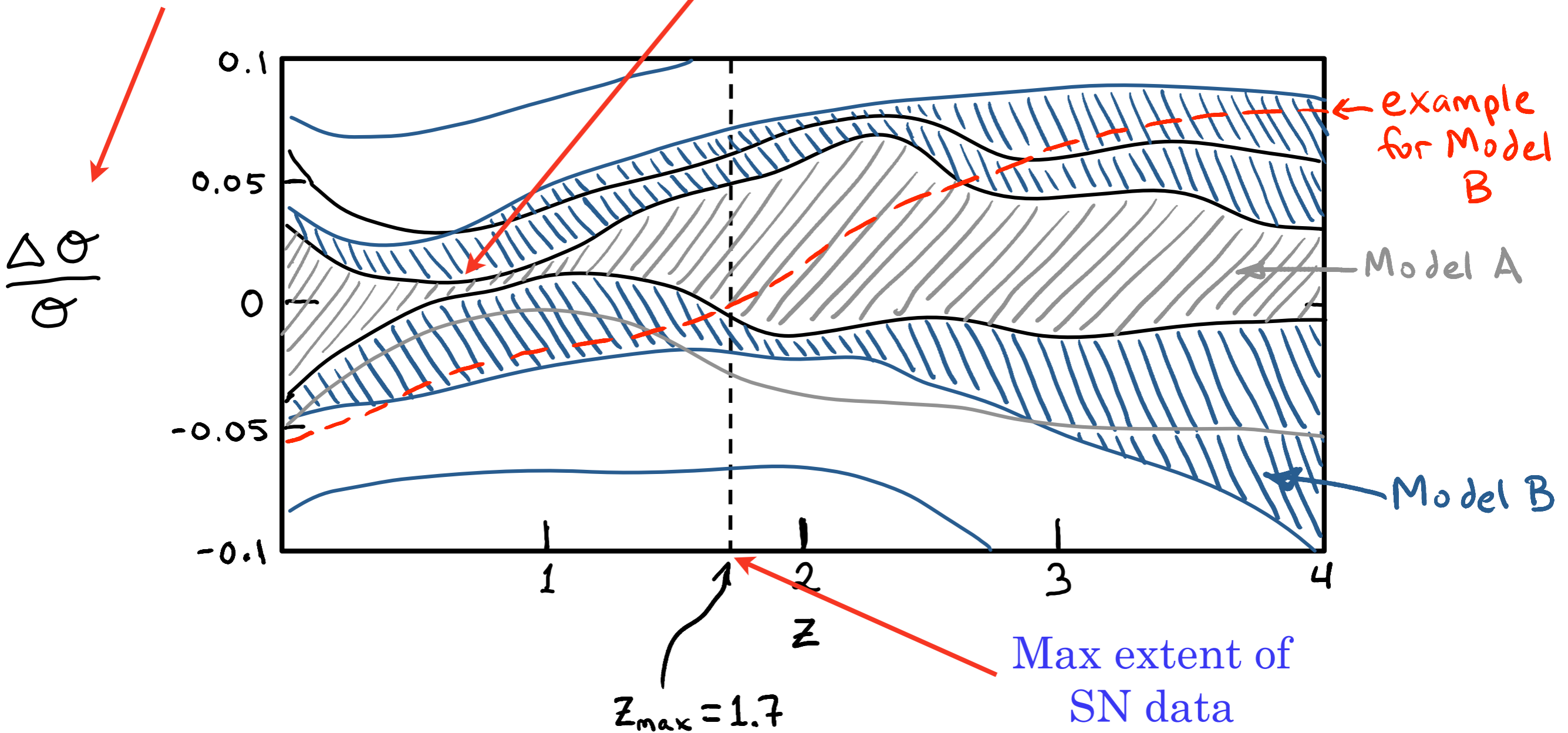
α_i = PC amplitude
 $e_i(z)$ = PC shape



Structure of graphs to follow

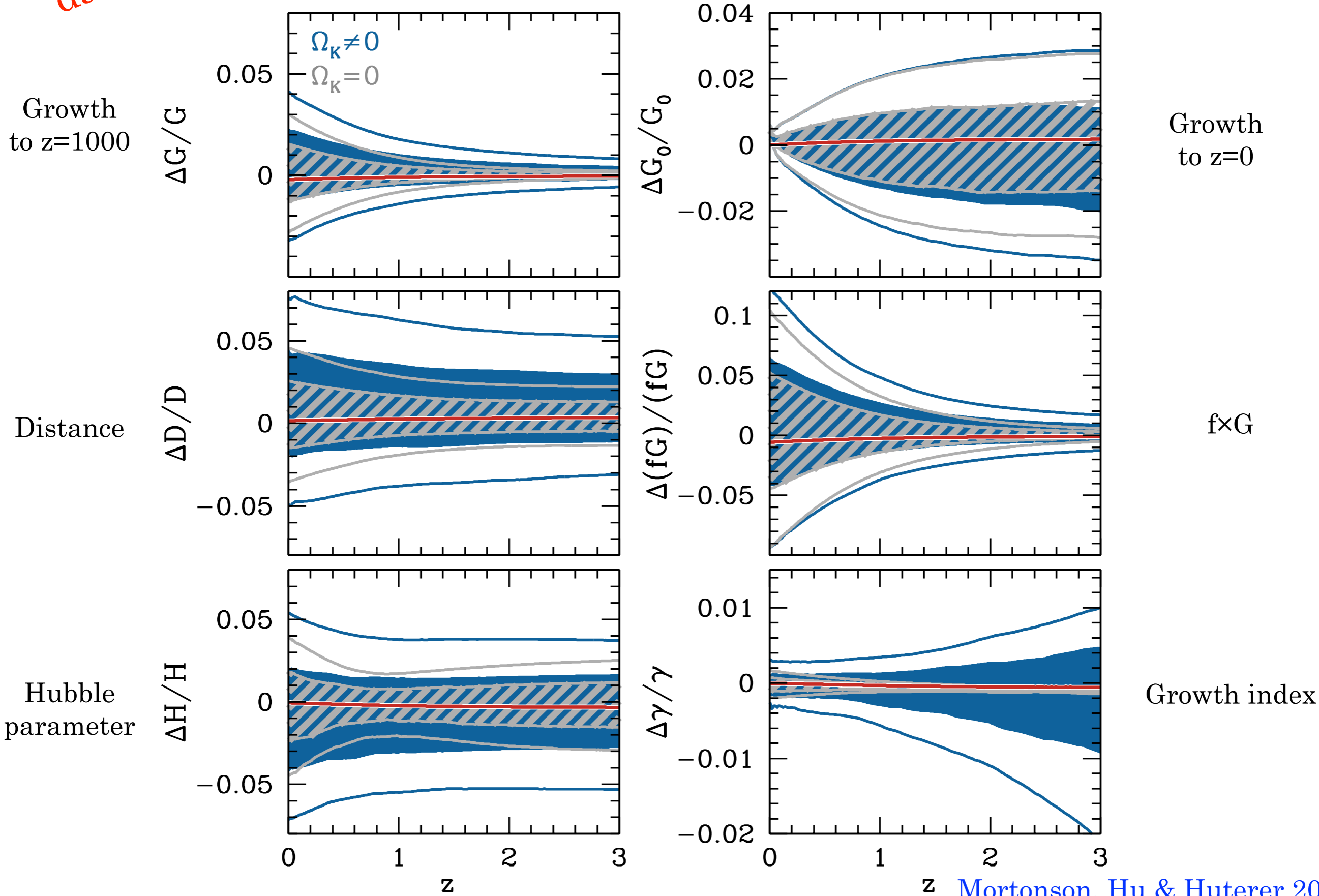
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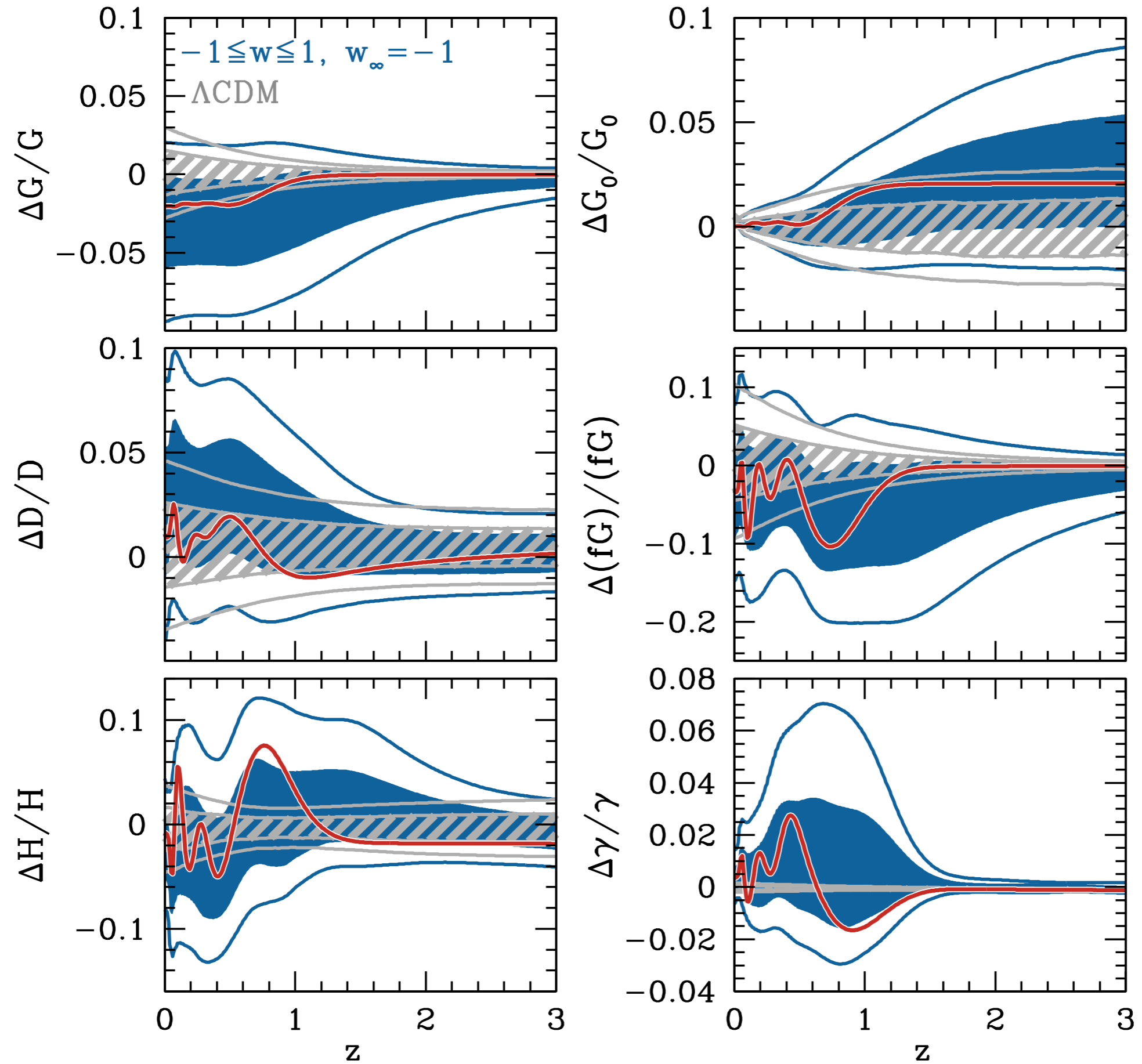
Current
data

ΛCDM predictions - flat or curved



Current data

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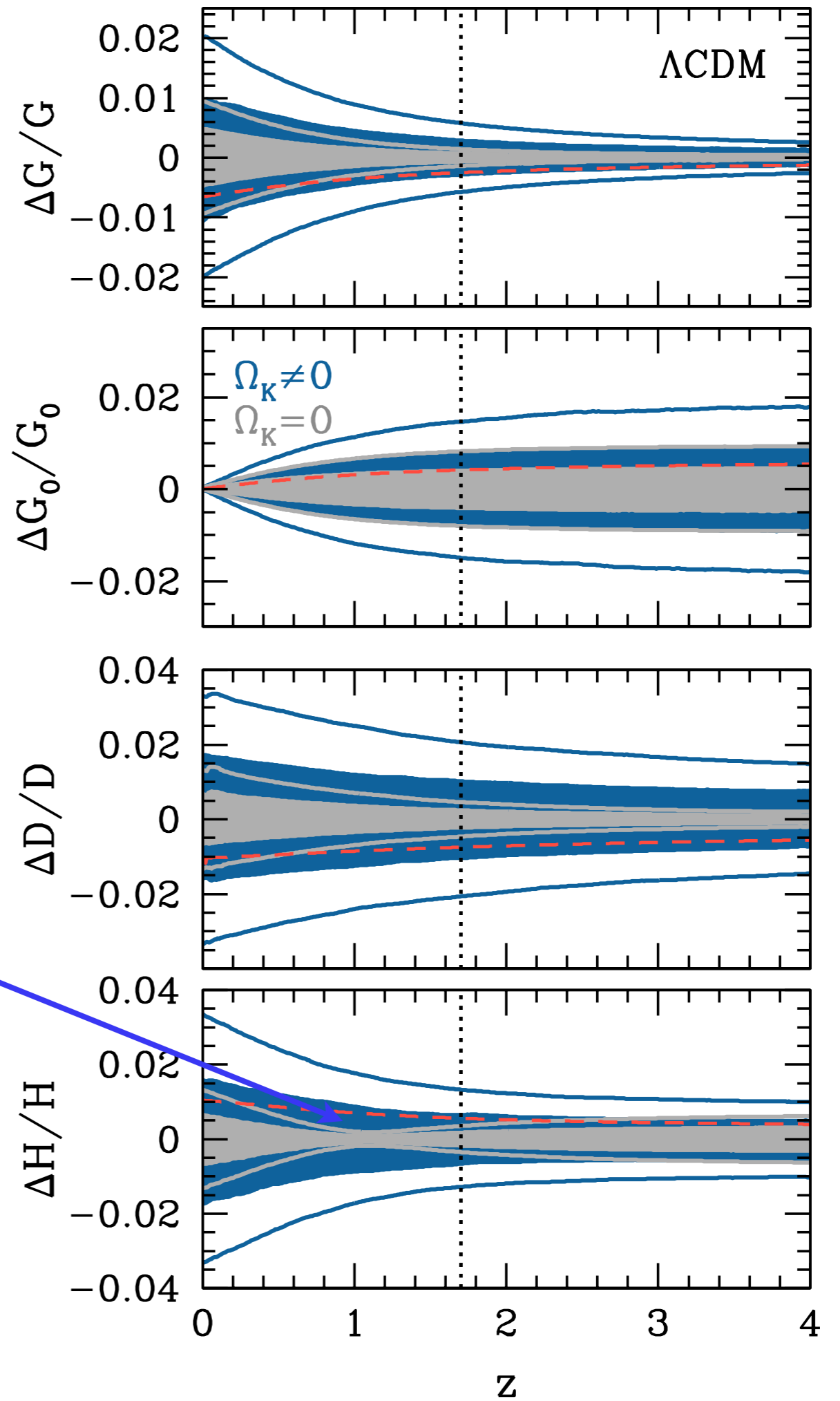


Future data

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H(z=1) to 0.1% for flat ΛCDM



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Quintessence predictions

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Smoking Gun of curvature:
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