

X-ray Spectroscopy

A Critical Look at Past Accomplishments
and Future Prospects

James Penner-Hahn jeph@umich.edu

Lecture plan

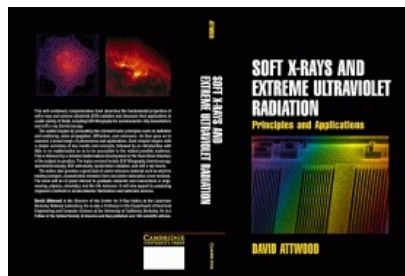
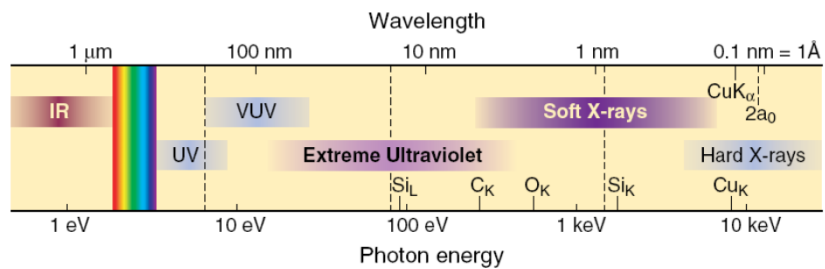
1. Fundamental principles of x-ray – matter interactions: x-ray absorption and emission
2. Principles of EXAFS and XANES data analysis
3. Applications of x-ray spectroscopy to inorganic chemistry
4. Advanced methods in x-ray spectroscopy

Fundamental principles

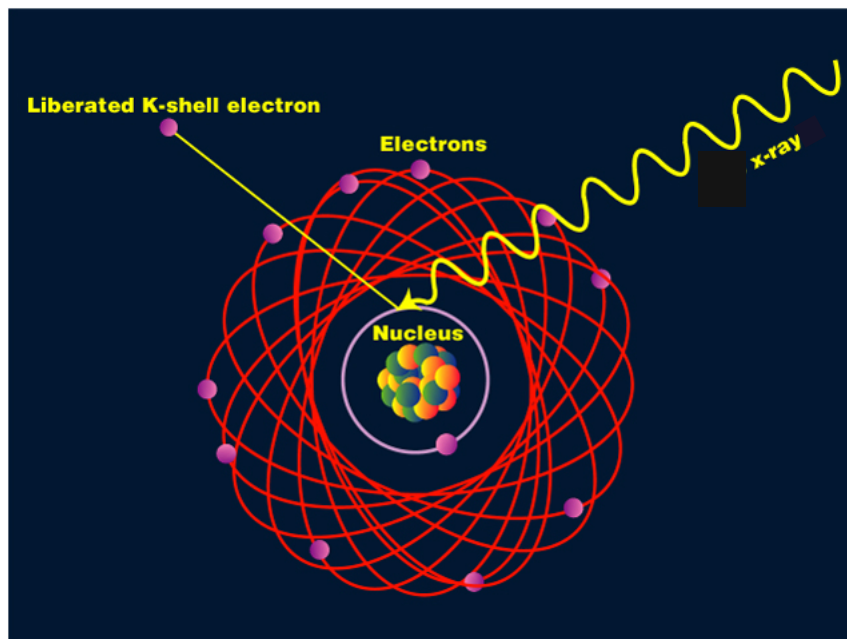
1. Techniques for studying metals
2. Interactions of x-rays with matter
3. XAS – EXAFS and XANES
4. Data collections
 - a) Generation of x-rays
 - b) Measurement of x-rays
 - c) Transmission vs. Fluorescence measurements
 - d) Sensitivity

Techniques for studying metal sites (proteins, materials, etc.)

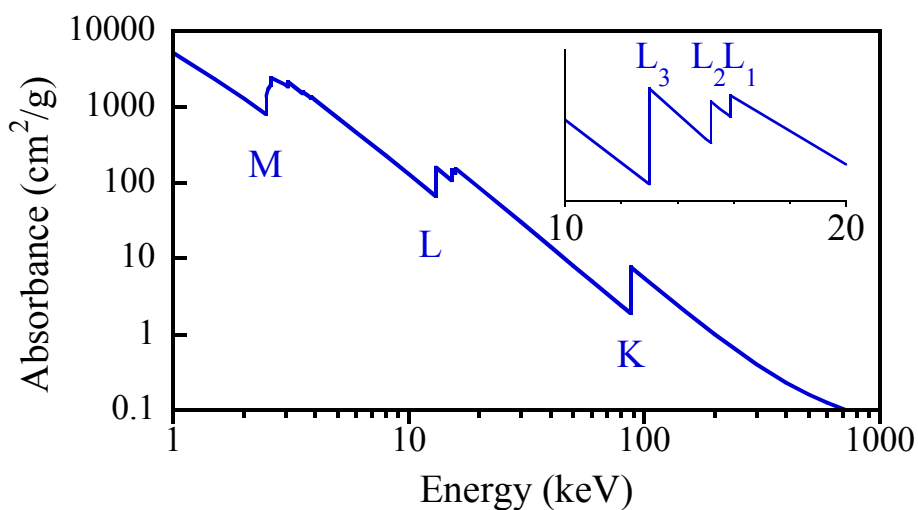
- UV-visible spectroscopy
 - EPR spectroscopy
 - Magnetic susceptibility
 - MCD
 - NMR spectroscopy
 - X-ray crystallography
- Require open d shell
- Requires $I=1/2$ nucleus
- Requires crystals
- X-ray spectroscopy



<http://www.coe.berkeley.edu/AST/sxreuv>



Absorption of x-rays by Pb



Electron binding energies of the elements

Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}	M ₄ 3d _{3/2}	M ₅ 3d _{5/2}
1 H	13.6								
2 He	24.6 ^b								
3 Li	54.7 ^b								
4 Be	111.5 ^b								
5 B	188 ^b								
6 C	284.2 ^b								
7 N	409.9 ^b	37.3 ^b							
8 O	543.1 ^b	41.6 ^b							
9 F	696.7 ^b								
10 Ne	870.2 ^b	48.5 ^b	21.7 ^b	21.6 ^b					
11 Na	1070.8 ^c	63.5 ^c	30.4 ^c	30.5 ^b					
12 Mg	1303.0 ^c	88.6 ^b	49.6 ^c	49.2 ^c					
13 Al	1559.6	117.8 ^b	72.9 ^b	72.5 ^b					
14 Si	1838.9	149.7 ^b	99.8 ^b	99.2 ^b					
15 P	2145.5	189 ^b	136 ^b	135 ^b					
16 S	2472	230.9 ^b	163.6 ^b	162.5 ^b					
17 Cl	2822.4	270.2 ^b	202 ^b	200 ^b					
18 Ar	3205.9 ^b	326.3 ^b	250.6 ^b	248.4 ^b	29.3 ^b	15.9 ^b	15.7 ^b		
19 K	3608.4 ^b	378.6 ^b	297.3 ^b	294.6 ^b	34.8 ^b	18.3 ^b	18.3 ^b		
20 Ca	4038.5 ^b	438.4 ^c	349.7 ^c	346.2 ^c	44.3 ^c	25.4 ^c	25.4 ^c		
21 Sc	4492.8	498.0 ^b	403.6 ^b	398.7 ^b	51.1 ^b	28.3 ^b	28.3 ^b		
22 Ti	4966.4	560.9 ^c	461.2 ^c	453.8 ^c	58.7 ^c	32.6 ^c	32.6 ^c		
23 V	5465.1	626.7 ^c	519.8 ^c	512.1 ^c	66.3 ^c	37.2 ^c	37.2 ^c		
24 Cr	5989.2	695.7 ^c	583.8 ^c	574.1 ^c	74.1 ^c	42.2 ^c	42.2 ^c		
25 Mn	6539.0	769.1 ^c	649.9 ^c	638.7 ^c	82.3 ^c	47.2 ^c	47.2 ^c		
26 Fe	7112.0	844.6 ^c	719.9 ^c	706.8 ^c	91.3 ^c	52.7 ^c	52.7 ^c		
27 Co	7708.9	925.1 ^c	793.3 ^c	778.1 ^c	101.0 ^c	58.9 ^c	58.9 ^c		
28 Ni	8332.8	1008.6 ^c	870.0 ^c	852.7 ^c	110.8 ^c	68.0 ^c	66.2 ^c		
29 Cu	8978.9	1096.7 ^c	952.3 ^c	932.5 ^c	122.5 ^c	77.3 ^c	75.1 ^c		
30 Zn	9658.6	1196.2 ^b	1044.9 ^b	1021.8 ^b	139.8 ^b	91.4 ^b	88.6 ^b	10.2 ^b	10.1 ^b

International XAFS Society

<http://www.ixasportal.net/ixas/>

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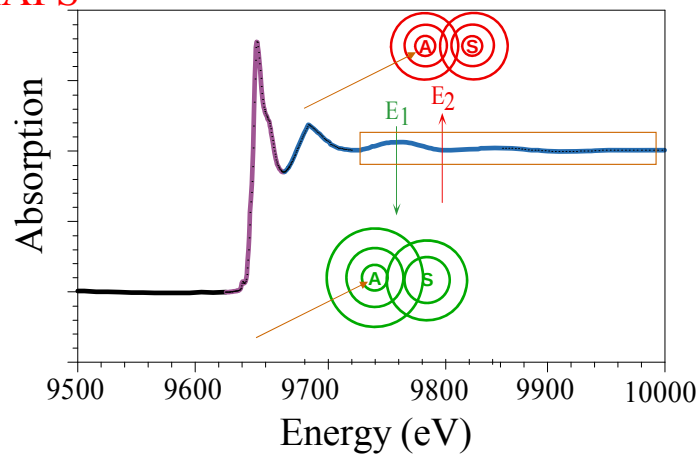
Links	
Facilities America • ALS - Advanced Light Source, USA • APS - Advanced Photon Source, USA • CAMD - Center for Advanced Microstructures & Devices, USA • CHESS - Cornell High Energy Synchrotron Source, USA • CLS - Canadian Light Source, Canada • CTST - UCSB Center for Terahertz Science and Technology, U • DFELL - Duke Free Electron Laser Laboratory, USA • Jlab - Jefferson Lab, USA • LCLS - Linac Coherent Light Source, USA • LNLS - Laboratorio Nacional de Luz Sincrotron, Brazil • NSLS - National Synchrotron Light Source, USA • SRC - Synchrotron Radiation Center, USA • SSRL - Stanford Synchrotron Radiation Lightsource, USA • SURF - Synchrotron Ultraviolet Radiation Facility, USA • VU FEL - W. M. Keck Vanderbilt Free-electron Laser Center, U • US DOE Nanoscale Science Research Centers • CFN - Center for Functional Nanomaterials, USA • CNM - Center for Nanoscale Materials, USA • FOUNDRY - The Molecular Foundry, USA	Asia • BSRF - Beijing Synchrotron Radiation Facility, P.R. China • CANDLE, Armenia • HSRC - Hiroshima Synchrotron Radiation Center, Japan • iFEL - Institute of Free Electron Laser, Japan • INDUS 1/INDUS 2, India • IR FEL Research Center - FEL-SUT, Japan • Medical Synchrotron Radiation Facility, Japan • NSRL - National Synchrotron Radiation Laboratory, P.R. China • NSRR - National Synchrotron Radiation Research Center, Taiwan • NSSL - Nagoya University Small Synchrotron Radiation Facility, Japan • KSR - Nuclear Science Research Facility, Japan • PAL - Pohang Accelerator Laboratory, Korea • PF - Photon Factory, KEK, Japan • Ritsumeikan University (Rits) Synchrotron Radiation Center, Japan • SAGA-LS - Saga Light Source, Japan • SESAME, Jordan • SLRI - Synchrotron Light Research Institute, Thailand • SPRING-8, Japan • SSSL - Singapore Synchrotron Light Source, Singapore • SSRC - Siberian Synchrotron Research Center, Russian Federation • SSRF - Shanghai Synchrotron Radiation Facility, P.R. China • SuperSOR - SuperSOR Synchrotron Radiation Facility, Japan

X-ray absorption spectroscopy

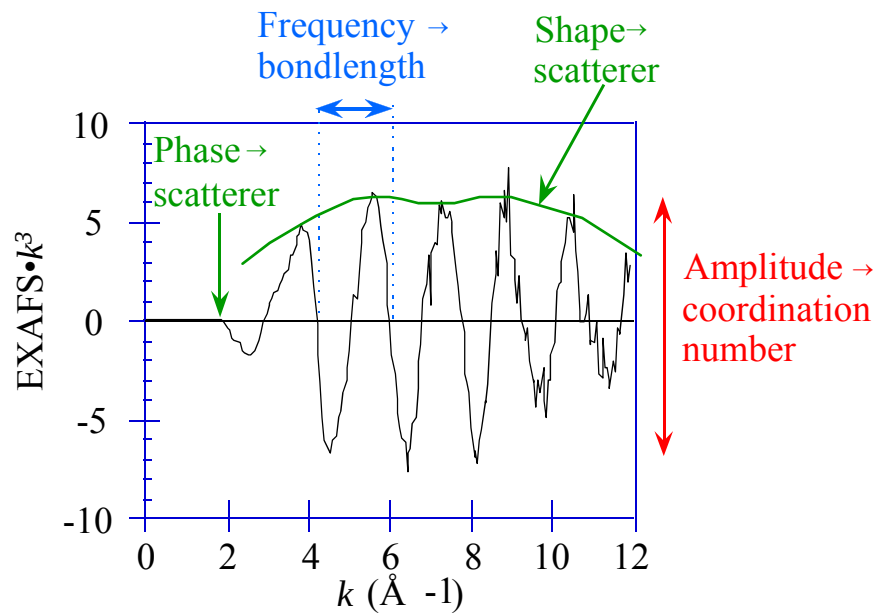
XAS
XAFS
NEXAFS

XANES

EXAFS



X-ray absorption spectroscopy



Information Content of EXAFS

- Bond length $\pm 0.02 \text{ \AA}$ (accuracy)
- Bond length $\pm 0.005 \text{ \AA}$ (precision)
- Coordination number (lower limit) ± 1
- Ligation type (Z) ± 10

$$R_{\text{max}} < \sim 4 \text{ \AA}$$

Scott, R. A. "Measurement of Metal-Ligand Distances by EXAFS" *Methods Enzymol.* **1985**, 117, 414-459.

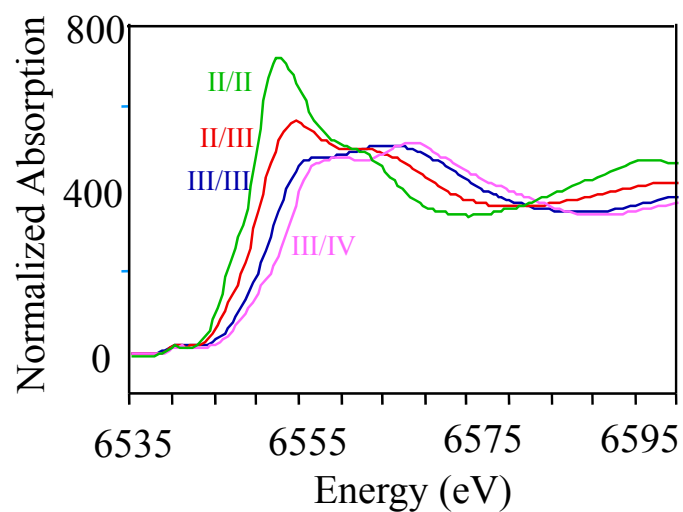
Teo, B. K. *EXAFS: Basic Principles and Data Analysis*; Springer-Verlag: New York, **1986**.

Scott, R.A., "X-Ray Absorption Spectroscopy" in *Physical Methods in Bioinorganic Chemistry*, Que, L. (Ed)., **2000**, University Science Books.

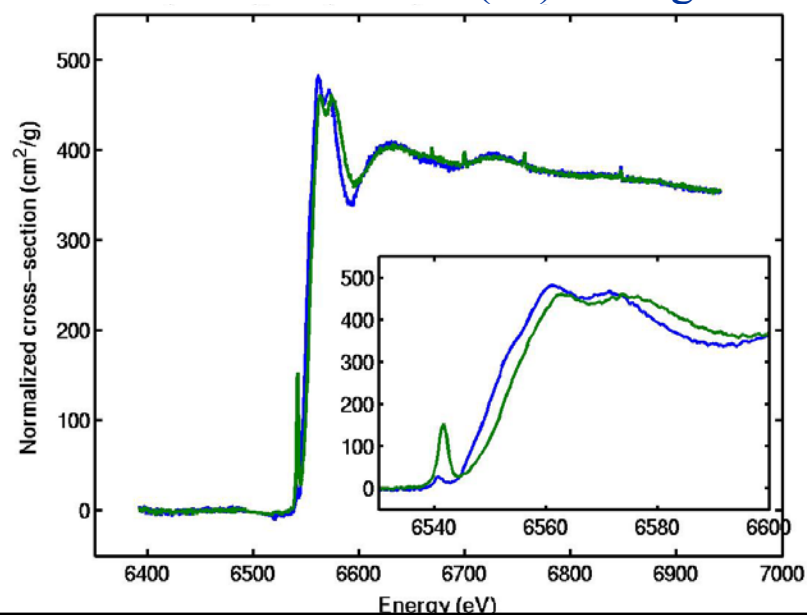
Penner-Hahn, J.E., "X-Ray Absorption Spectroscopy", in *Comp. Coord. Chem. II*, Vol. 2, **2004**.

Levina A, Armstrong R.S., Lay P.A., "Three-dimensional structure determination using multiple-scattering analysis of XAFS: applications to metalloproteins and coordination chemistry" *Coord. Chem. Rev.* **2005**, 249, 141-160.

Dependence of XANES on Oxidation State



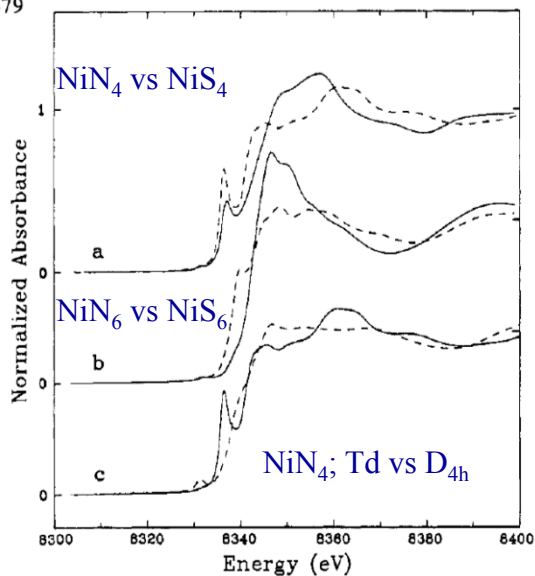
Mn(V)=O has intense pre-edge transition,
not seen in Mn(III) analog



X-ray Absorption Spectroscopic Evidence for a Unique Nickel Site in *Clostridium thermoaceticum* Carbon Monoxide Dehydrogenase

Stephen P. Cramer,^{*1a,b} Marly K. Eidsness,^{1c,d} W.-H. Pan,^{1a} Thomas A. Morton,^{1e} Steve W. Ragsdale,^{1e,f} Daniel V. DerVartanian,^{1e} Lars G. Ljungdahl,^{1e} and Robert A. Scott^{*1g}

Inorg. Chem. **1987**, *26*, 2477–2479



Advantages of XAFS

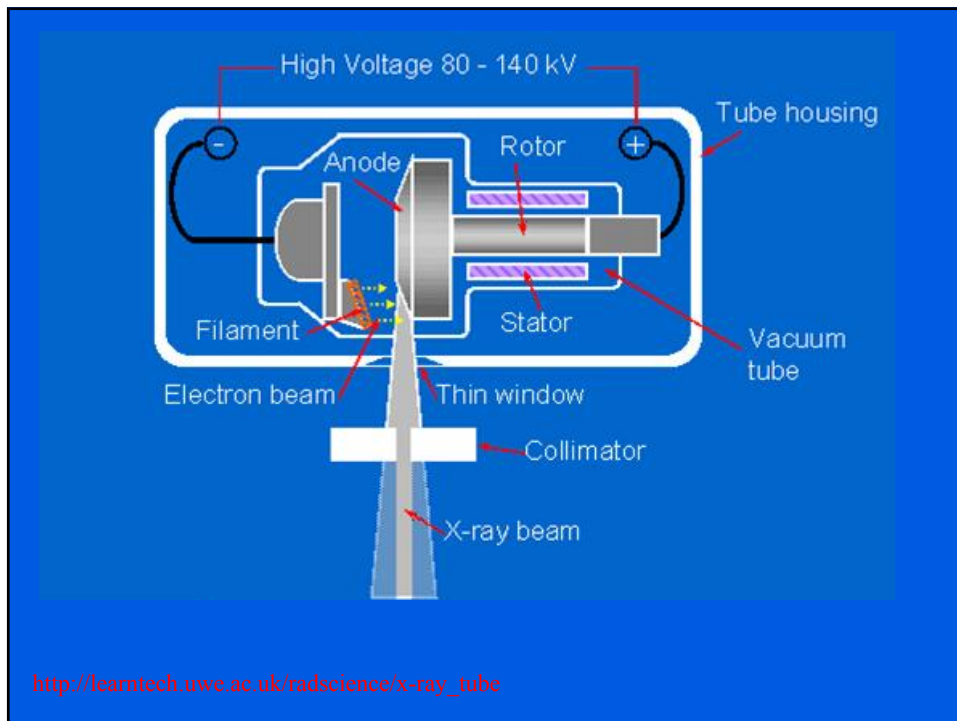
Direct structural determination for:

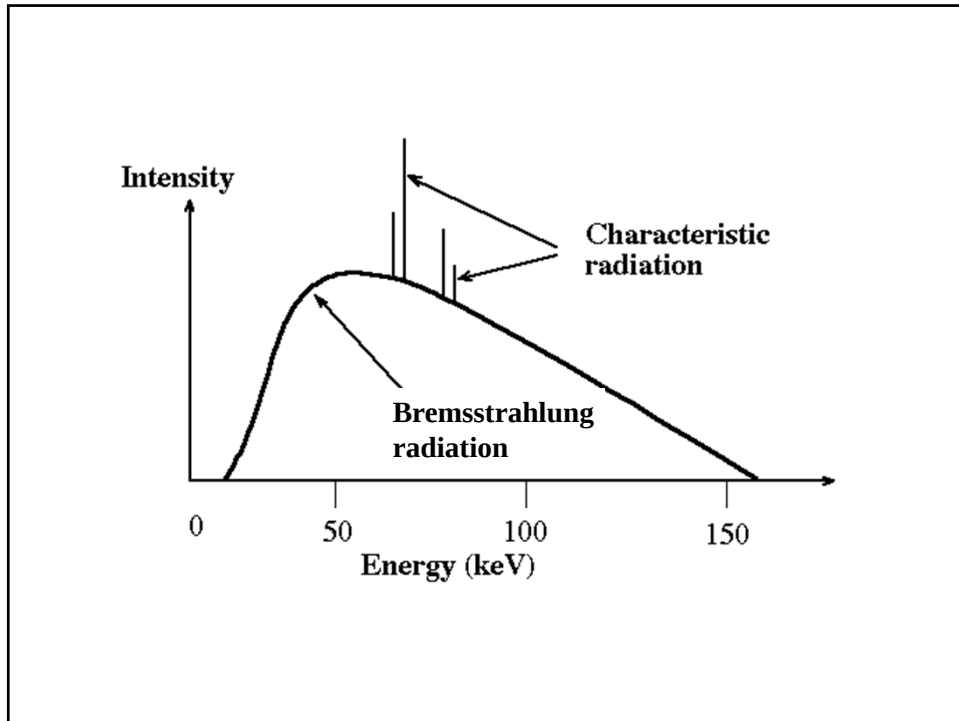
- Any form of matter
- Any isotope
- Any spin state

Direct determination of oxidation state

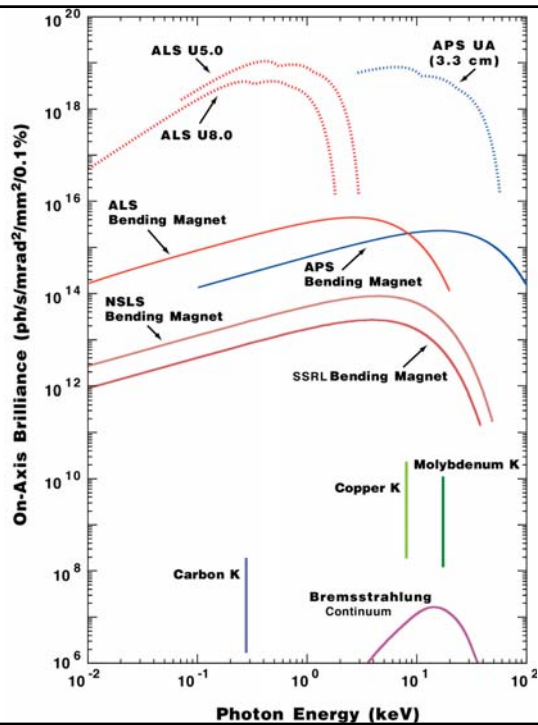
Disadvantages of XAFS

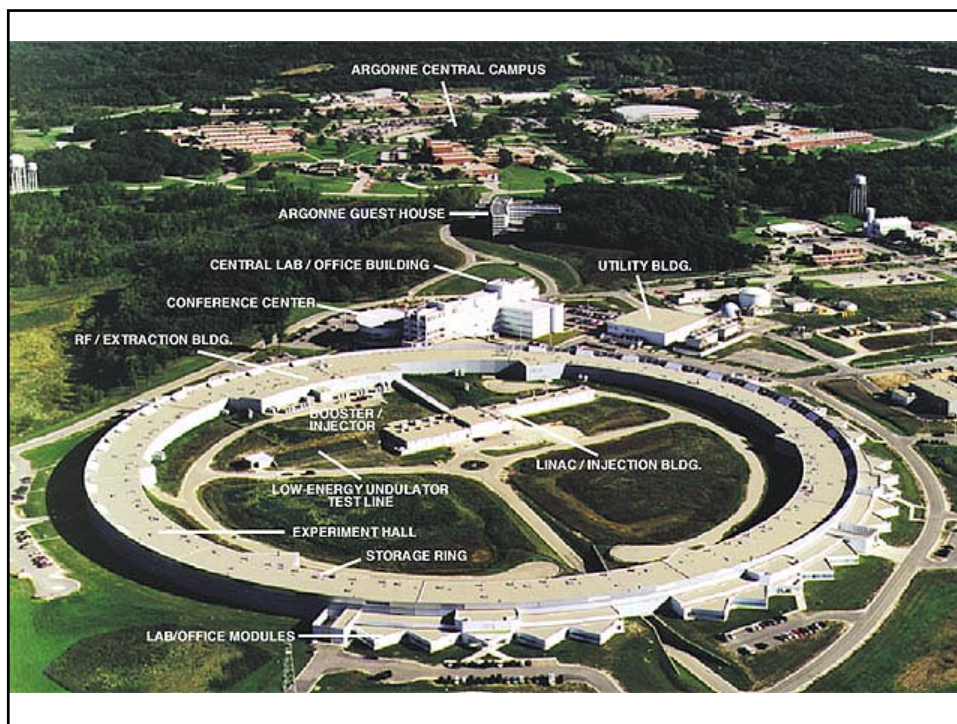
- Bulk spectroscopy (average structure)
- Little angular information
- Gives only *local* structural information
- Limited sensitivity
- Requires synchrotron x-ray source





Synchrotrons
produce intense,
tunable x-ray
beams





SSRF Shanghai Synchrotron Radiation Facility

3-10-18

What's New?

SSRF Operation Status

Since December 6, 2012, the Shanghai Synchrotron Radiation Facility (SSRF) has operated in top-up mode for user experiments, which was a milestone of

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- News & Events
- Contacts

Galleries

<http://ssrf.sinap.ac.cn>





SSRF
Shanghai Synchrotron Radiation Facility

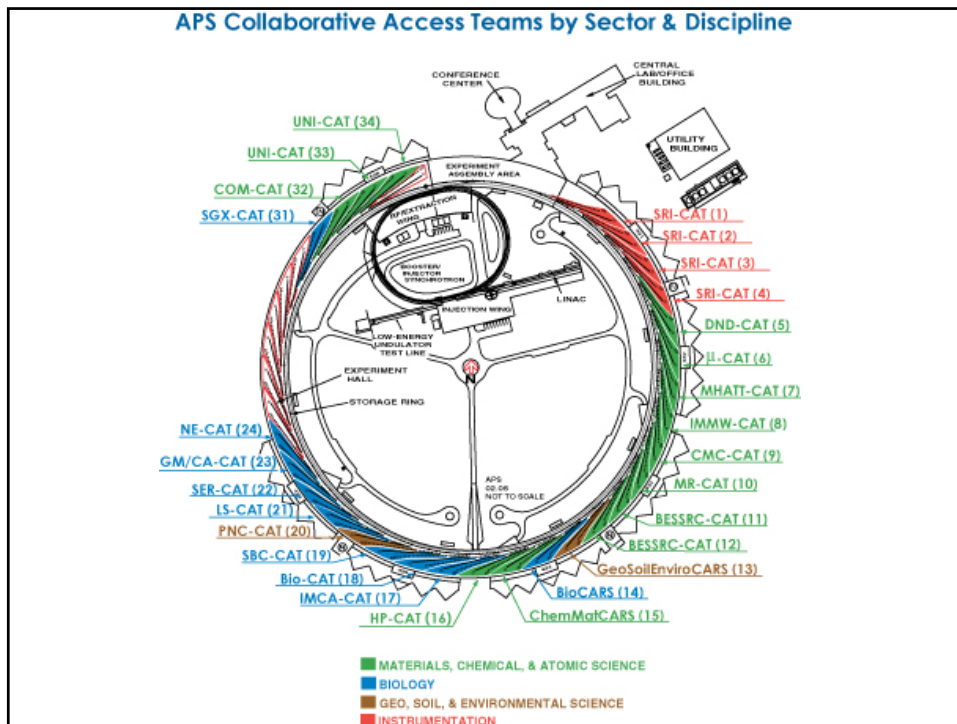
HOME
Introduction | Current Beamlines

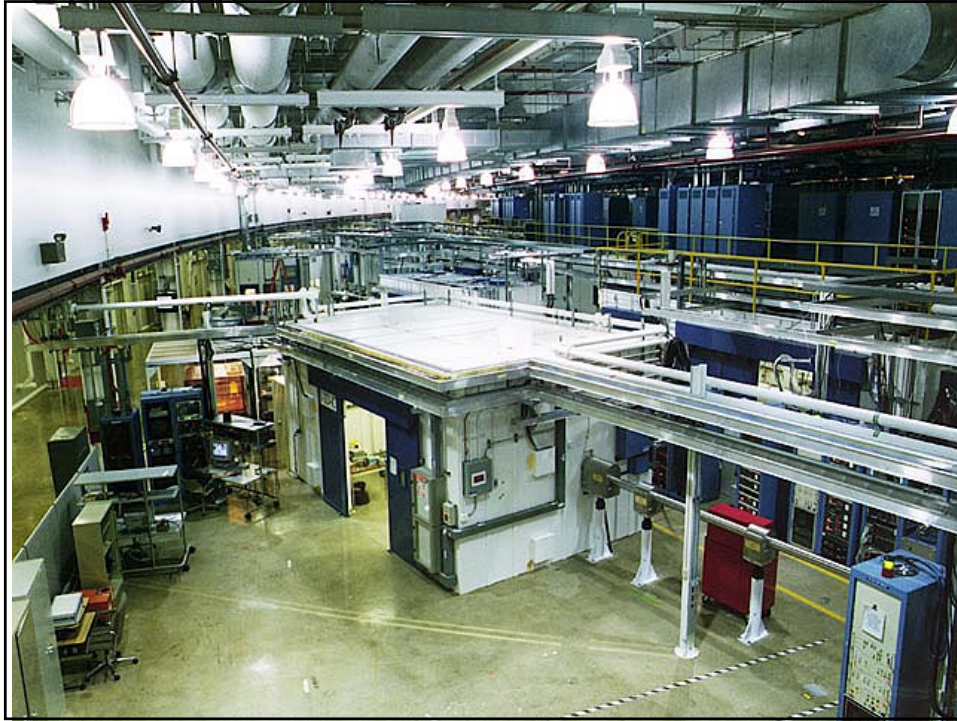
HOME>>Beamlines>>Current Beamlines



◆ Current Beamlines

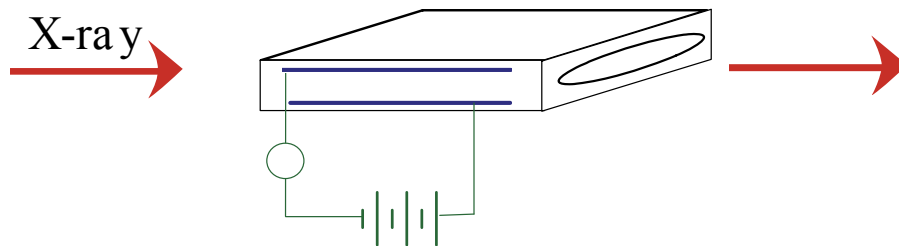
- ◆ BL08U1-A Soft X-ray Spectromicroscopy
- ◆ BL08U1-B Soft X-ray Interference Lithography (XIL)
- ◆ BL13W1 X-ray Imaging and Biomedical Applications
- ◆ BL14W1 X-ray Absorption Fine Structure Spectroscopy (XAFS)
- ◆ BL14B1 X-ray Diffraction
- ◆ BL15U1 Hard X-ray Micro-Focusing
- ◆ BL16B1 Small Angle X-ray Scattering (SAXS)
- ◆ BL17U1 Macromolecular Crystallography





Detection of x-rays

X-rays are ionizing radiation – need to collect (and count) ionizations



Transmission measurements

Beer-Lambert law I_0 =incident, I_t =transmitted

$$I_t = I_0 10^{-\varepsilon C l} \quad I_t = I_0 e^{-\mu t}$$

$$I_t = I_0 e^{-\mu_m \rho t}$$

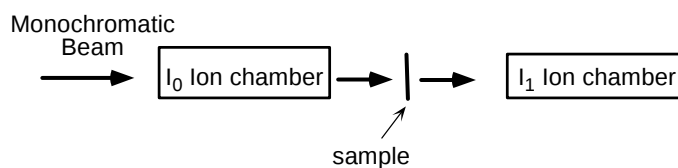
t sample thickness (cm)

μ absorption coefficient (cm^{-1})

μ_m mass absorption coefficient (cm^2g^{-1})

ρ Density (g cm^{-3})

Absorbance



$$A = \varepsilon C l = \log\left(\frac{I_0}{I_t}\right) \quad A = \mu t = \ln\left(\frac{I_0}{I_t}\right)$$

X-ray absorption coefficients

<http://csrri.iit.edu/periodic-table.html>

<http://physics.nist.gov/PhysRefData/XrayMassCoef/cover.html>

<http://csrri.iit.edu/periodic-table.html>

Periodic Table

Click on any button with element name to get its x-ray properties. If you give an energy value in the box at the top of the table then you also get x-ray cross-sections at that energy. The original subroutine (mucal f or mucal c) used to calculate x-ray cross-sections is available from [here](#).

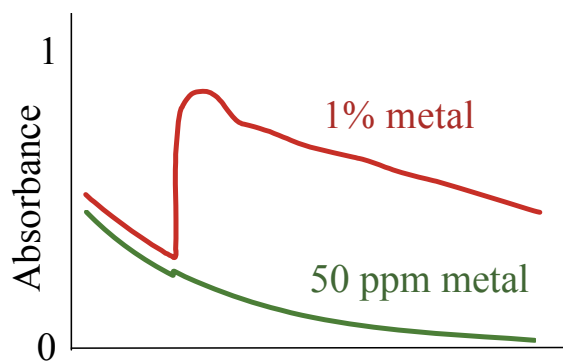
Energy: keV

1																	2
H																	He
3	4											5	6	7	8	9	10
Li	Be											B	C	N	O	F	Ne
11	12											13	14	15	16	17	18
Na	Mg											Al	Si	P	S	Cl	Ar
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe

Element		Edge Energies (keV)		Edge jumps		Fluorescence yield	
Symbol	Fe	K	7.11199999	K	8.0714798	K	0.340000004
Z	26	L1	0.842000008	L1	1.1567719	L1	0.00100000005
Atomic Weight	55.8499985	L2	0.719900012	L2	2.09867859	L2	0.0939999968
Density	7.86000013	L3	0.706799984	L3	0.	L3	6.40299988
		M	0.0939999968				
		K-alpha	6.40299988				
		K-beta	7.05700016				
		L-alpha	0.				
		L-beta	0.				

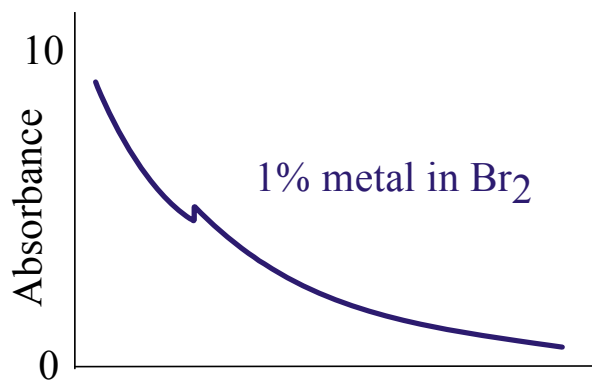
Cross-sections at E = 7.19999981 keV (cm^2/gm)			
Photoelectric	393.506775		
Coherent	1.797014		
Incoherent	0.0686381012		
Total	395.372406		
Conversion factor (C) {(Barns/Atom) = C * (cm^2/gm)}	92.7399979		
Absorption coefficient	3107.6272	1/cm	
1/mu (element)	3.21788907	microns	

Absorbance is great for
concentrated samples,

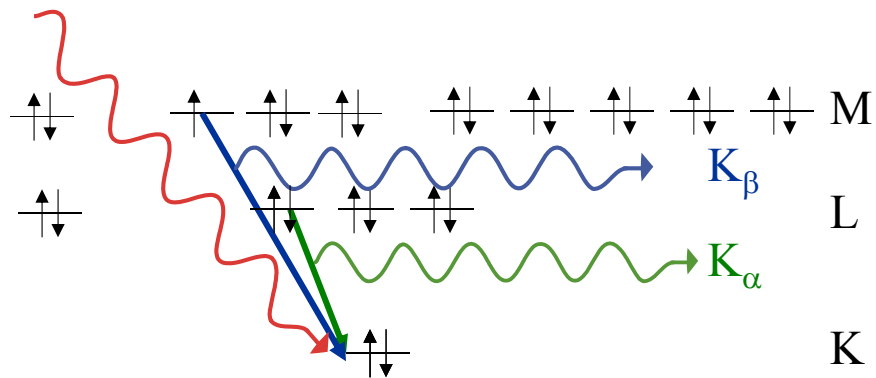


but not for dilute samples.

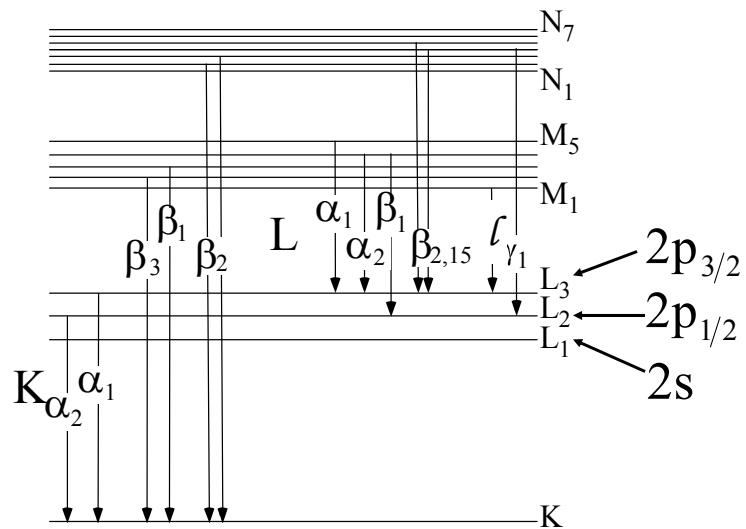
Transmission is also sensitive to
background absorption



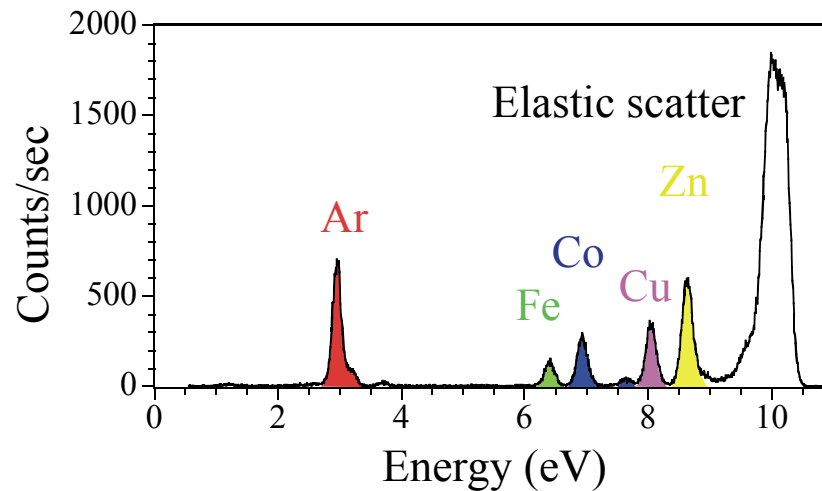
X-ray Fluorescence



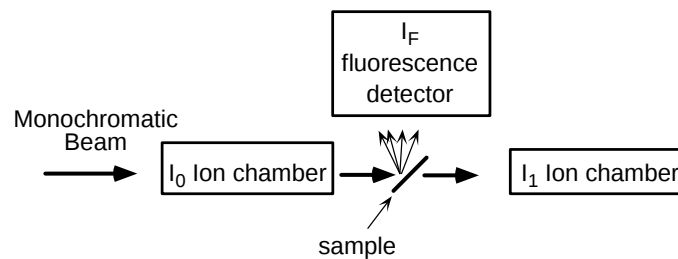
X-ray fluorescence lines



X-ray fluorescence spectra give element sensitivity



Fluorescence excitation spectra



Measure fluorescence intensity as excitation energy is scanned

Self-absorption

$$I_F = I_0 \frac{\Omega}{4\pi} \varepsilon \frac{\mu_X(E)}{\mu_T(E) + \mu_T(E_{fl})} \left(1 - e^{-[\mu_T(E) + \mu_T(E_{fl})]t} \right)$$

$$\mu_T = \mu_X + \mu_B$$

Reduces to $I_f \propto \mu_X$ if $\mu t \ll 1$ (thin)

If $\mu t \gg 1$ (thick)

$$I_F \approx \frac{\mu_X(E)}{\mu_T(E) + \mu_T(E_{fl})} = \frac{\mu_X(E)}{\mu_X(E) + \mu_B(E) + \mu_T(E_{fl})}$$

Goulon J, et al. "On Experimental Attenuation Factors Of The Amplitude Of The EXAFS Oscillations In Absorption, Reflectivity And Luminescence Measurements", *J de Physique* **43**, 539-548 1982

Self-absorption continued

$$\frac{\mu_X(E)}{\mu_X(E) + \mu_B(E) + \mu_T(E_{fl})} \approx \mu_X(E)$$

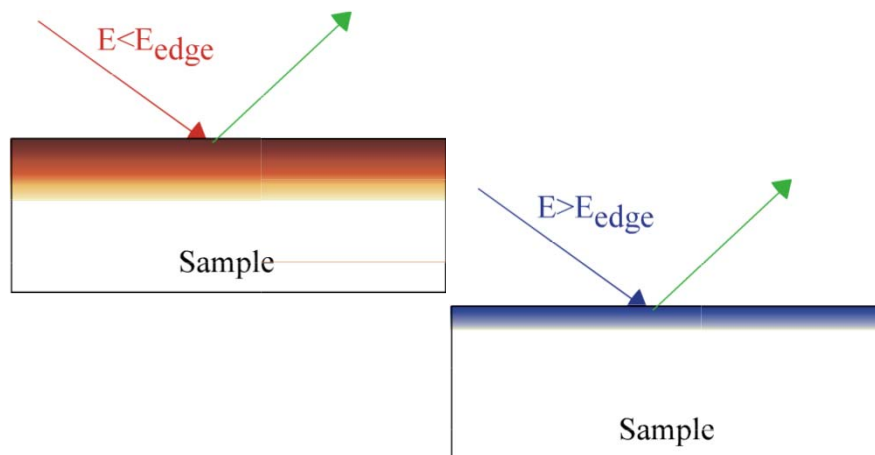
Only if $\mu_X \ll \mu_B$ (dilute)

Fluorescence excitation spectra only give accurate μ_X if samples are thin or dilute.

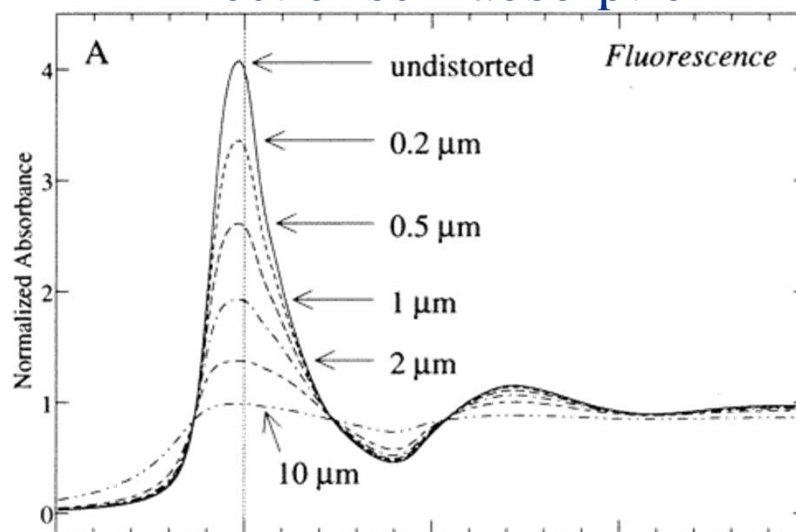
Otherwise, need to correct.

Waldo GS, Carlson RMK, Moldowan JM, Peters KE, Penner-Hahn JE
"Sulfur Speciation In Heavy Petroleums - Information From X-ray
Absorption Near-edge Structure " *Geochim Cosmochim Acta* **55** 801-
814 (1991)

If samples are not either thin or dilute, will have self-absorption



Effect of self-absorption



Pickering IJ, et al. "Analysis of sulfur biochemistry of sulfur bacteria using X-ray absorption spectroscopy" *Biochemistry* **40** 8138-8145 (2001)

Self-absorption

If a sample gives a reasonable transmission signal, it is too concentrated to measure by fluorescence (unless sample is very thin)

Signal/Noise concerns in XAS

Counting statistics – uncertainty $\sim (\text{counts})^{1/2}$

If there is no background, $S/N = (\text{counts})^{1/2}$

Typical fluorescence 10^4 sec^{-1} to 10^5 sec^{-1}

Transmission ion-chambers – typical
currents $\geq 10 \text{ nA} \sim 10^{10} \text{ electrons/s}$
Negligible noise from counting
statistics.

Important noise sources: electronic,
microphonic, beam problems (below)

Sensitivity

EXAFS amplitude falls of $\approx 1/k^3$

10% effect at $k=2 \text{ \AA}^{-1}$; 0.03% at $k=14 \text{ \AA}^{-1}$

For EXAFS $S/N=3$ at $14 \text{ \AA}^{-1}$ need
absorption $S/N=3/0.0003=10^4$

Therefore need 10^8 counts at $k=14 \text{ \AA}^{-1}$

What is required to have 10^8 fluorescent photons

Incident flux $\approx 2 \cdot 10^{13} \text{ sec}^{-1}$ in 10^{-8} m^2

Fluorescence yield $\approx 0.5 \rightarrow$ need

absorbance of 10^{-5} to give 10^8 fluorescent
photons in 1 second

Absorbance $= 3 \cdot 10^4 \text{ barns/atom}$
 $= 3 \cdot 10^{-16} \cdot N$

Need $N \approx 3 \cdot 10^{10}$

50 fmole, 50 μM if sample is $(100 \mu\text{m})^3$

Reality

Detected solid angle is 1-5% (i.e., 10^6 sec^{-1})
but – count times of 100 sec/pt are realistic →
total measurement time ~6 hrs (vs. 3 minutes)

However

Effective count rate is often detector-limited:
if scatter:fluorescence is 100:1, $N_{\text{max}} \sim 10^4$
(10^2 -fold lower than optimum).

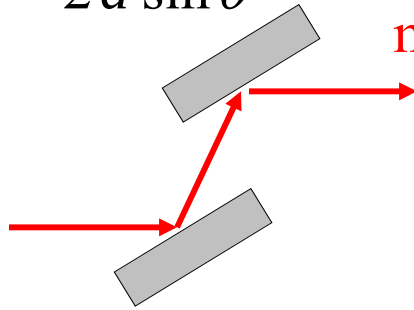
- Solids
 - If absorbance of element of interest > background absorbance use transmission
 - If absorbance of element of interest << background absorbance use fluorescence
 - Samples need to be optically thin – often requires dilution
- Solutions
 - If concentrated, treat like a solid
 - If dilute (negligible edge jump) use fluorescence
 - Typical limits
 - ~ 100 μM Zn in 50 μL aqueous solution (5 nmole)
 - ~1.0 mM V in 10 μL aqueous solution (10 nmole)
 - 10 μM Mo in 200 μL aqueous solution (2 nmole)

Bragg's Law

$$n\lambda = 2d \sin \theta; E = hc/\lambda$$

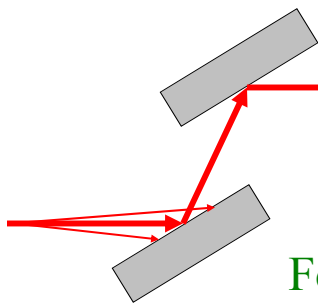
$$E = \frac{nhc}{2d \sin \theta}$$

Double-crystal
monochromator



Energy resolution

$$n\lambda = 2d \sin \theta$$



Angular divergence gives spread in energy. Vertical slits decrease $\Delta\theta$, and thus ΔE .

For many 3rd generation sources, angular divergence of beam is small compared to intrinsic width of reflection

Energy calibration

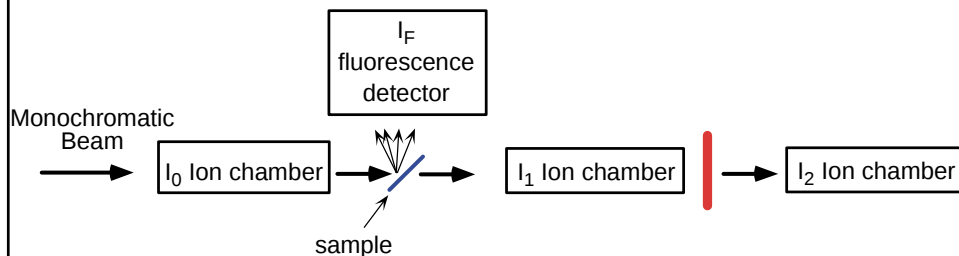
$$n\lambda = 2d \sin \theta$$

Want to know E to ~ 0.1 eV (1 part in 10^5)
Accurate absolute energy determination is hard. Typically, settle for precise relative energy.

For absolute calibration, see:

Pettifer RF, Hermes C “Absolute energy calibration of x-ray-radiation from synchrotron sources” *J Appl Crystallogr* **18**, 404-412 (1985)

Internal energy calibration



$$A_{\text{sample}} = \ln\left(\frac{I_0}{I_1}\right) \qquad A_{\text{foil}} = \ln\left(\frac{I_1}{I_2}\right)$$

Harmonic contamination

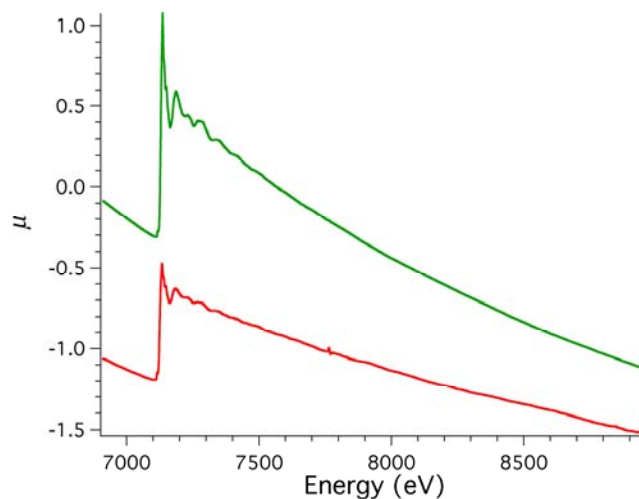
$$n\lambda = 2d \sin \theta$$

$$I_0 = I_0 + \beta I_{0,2E}$$

$$I_t = e^{-\mu t} I_0 + \beta I_{0,2E}$$

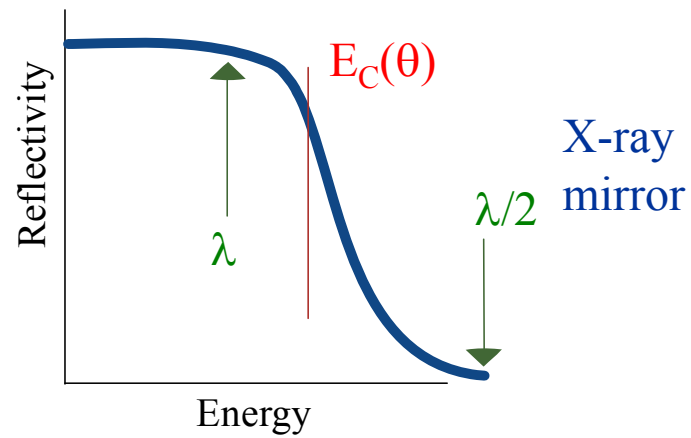
$$A = \ln\left(\frac{I_0}{I_1}\right) = \ln\left(\frac{I_0 + \beta I_{0,2E}}{e^{-\mu t} I_0 + \beta I_{0,2E}}\right)$$

Experimental consequence of harmonic contamination

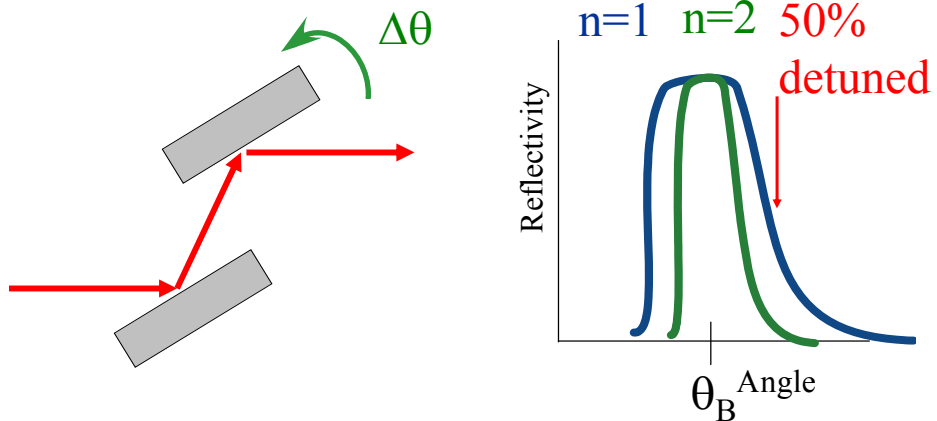


pinholes and self-absorption cause similar effect –
amplitudes are too small

Harmonic rejection mirror



“Detuning” monochromator



Fluorescence Detectors

- Energy resolving
 - Energy dispersive – Ge or Si(Li)
 - Wavelength dispersive
 - Exotic
- Non-energy resolving
 - Ion chamber
 - PIN diode

Energy-dispersive detectors

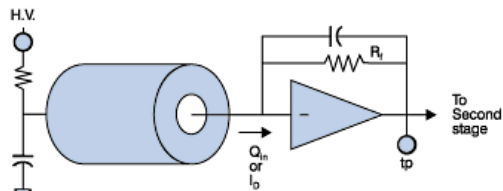
Charge carriers produced by Ge per unit energy deposited = $1/2.98$

$$\text{Detector Current} = \text{Energy Rate} \left(\frac{\text{eV}}{\text{s}} \right) \times \frac{\text{charge (Q)}}{\text{energy (eV)}} \times 1.6 \times 10^{-19} \frac{\text{Coulombs}}{\text{Q}}$$

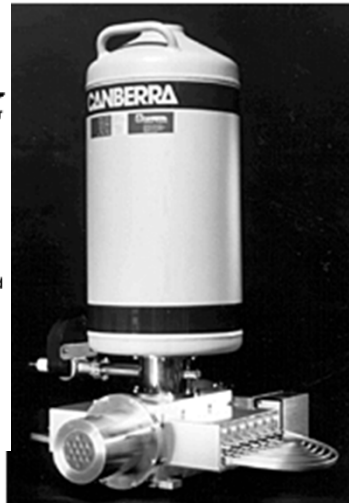
Charge per charge carrier

$$\frac{\text{Detector Current (A)}}{\text{Energy Rate (MeV/s)}} = 10^6 \times \frac{1.6 \times 10^{-19}}{2.98}$$

$$= 5 \times 10^{-14} = 0.05 \text{ pA/(MeV/s)}$$

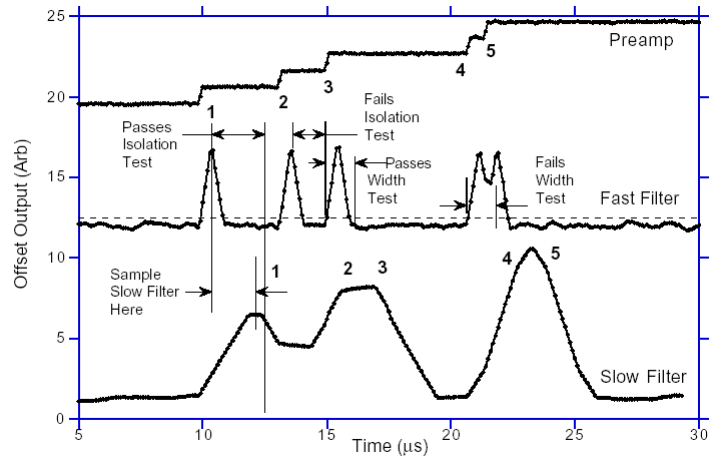


The energy rate limit of RC preamplifiers is a function of feedback resistor value (R_f) and dynamic range.



<http://www.canberra.com/products/491.asp>

Solid-state detectors have relatively low maximum count rates

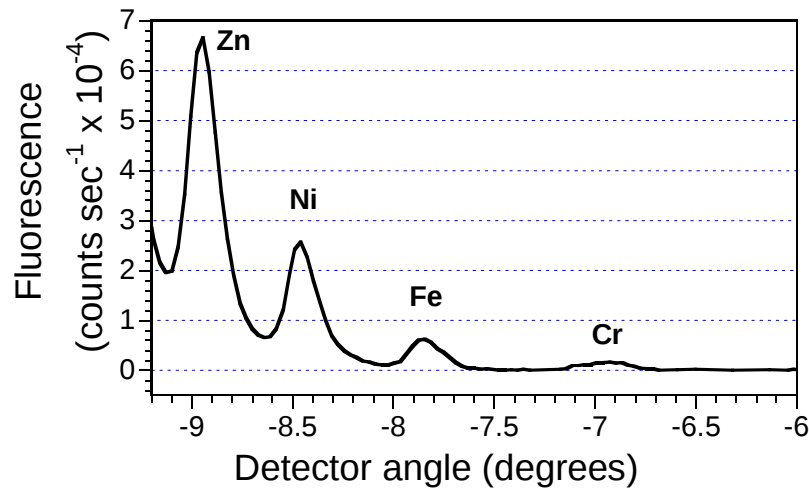


http://www.xia.com/AppNotes/DXP_Pile.pdf

Wavelength-dispersive detectors



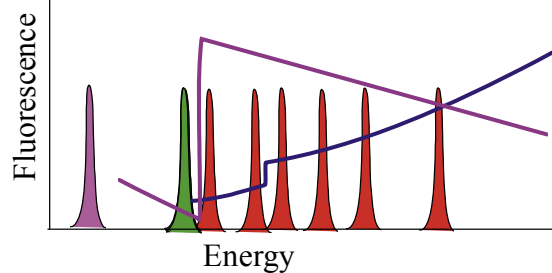
Reasonable solid angle results in low resolution, but unlimited count rate



Non-energy resolving detectors

Z-1 element functions as

low-pass filter, but filter fluorescences



Fluorescence

Excitation

Soller slits + Z-1 filter improve
fluorescence

